



Calhoun: The NPS Institutional Archive DSpace Repository

Theses and Dissertations

1. Thesis and Dissertation Collection, all items

1989

Extension of aggregation and shrinkage techniques used in the estimation of Marine Corps Officer attrition rates.

Misiewicz, John M.

Monterey, California. Naval Postgraduate School

<http://hdl.handle.net/10945/25936>

Downloaded from NPS Archive: Calhoun



<http://www.nps.edu/library>

Calhoun is the Naval Postgraduate School's public access digital repository for research materials and institutional publications created by the NPS community.

Calhoun is named for Professor of Mathematics Guy K. Calhoun, NPS's first appointed -- and published -- scholarly author.

Dudley Knox Library / Naval Postgraduate School
411 Dyer Road / 1 University Circle
Monterey, California USA 93943

NAVAL POSTGRADUATE SCHOOL

Monterey, California



THESIS

M63653

EXTENSION OF AGGREGATION AND SHRINKAGE
TECHNIQUES USED IN THE ESTIMATION OF
MARINE CORPS OFFICER ATTRITION RATES

by

John M. Misiewicz

September 1989

Thesis Advisor: Robert R. Read

Approved for public release; distribution is unlimited

T245995

REPORT DOCUMENTATION PAGE

1a Report Security Classification Unclassified		1b Restrictive Markings	
2a Security Classification Authority		3 Distribution Availability of Report Approved for public release; distribution is unlimited.	
2b Declassification Downgrading Schedule			
4 Performing Organization Report Number(s)		5 Monitoring Organization Report Number(s)	
6a Name of Performing Organization Naval Postgraduate School	6b Office Symbol (if applicable) 30	7a Name of Monitoring Organization Naval Postgraduate School	
6c Address (city, state, and ZIP code) Monterey, CA 93943-5000		7b Address (city, state, and ZIP code) Monterey, CA 93943-5000	
8a Name of Funding Sponsoring Organization	8b Office Symbol (if applicable)	9 Procurement Instrument Identification Number	
8c Address (city, state, and ZIP code)		10 Source of Funding Numbers Program Element No Project No Task No Work Unit Accession No	
11 Title (include security classification) EXTENSION OF AGGREGATION AND SHRINKAGE TECHNIQUES USED IN THE ESTIMATION OF MARINE CORPS OFFICER ATTRITION RATES			
12 Personal Author(s) John M. Misiewicz			
13a Type of Report Master's Thesis	13b Time Covered From To	14 Date of Report (year, month, day) September 1989	15 Page Count 114

16 Supplementary Notation The views expressed in this thesis are those of the author and do not reflect the official policy or position of the Department of Defense or the U.S. Government.

17 Cosati Codes			18 Subject Terms (continue on reverse if necessary and identify by block number) aggregation, attrition rate estimation, empirical Bayes
Field	Group	Subgroup	

19 Abstract (continue on reverse if necessary and identify by block number)

In this thesis we treat the "small cell" problem encountered when building an attrition rate generator for large-scale manpower flow models, specifically for the USMC Officer Corps. Such models have a large number of low-inventory (i.e. small) personnel cells. This presents a dilemma: on one hand we want to preserve as much fidelity as possible in our work by preserving a great deal of detail in each cell; on the other hand our statistical estimation techniques require larger cell sample sizes than intrinsically occur cell-by-cell in actual sample data. Our approach to producing stable attrition rates for such cells involves two efforts: (i) the aggregation of cells into groups that exhibit homogeneity of attrition behavior, and (ii) the development of "shrinkage" estimation techniques for use in the individual groups. A heuristic algorithm is developed and tested to treat the aggregation problem. Empirical Bayes methods are developed to serve the multi-cell estimation requirements needed to preserve the fidelity. Cross validation techniques are used to verify these methods.

The present work builds upon the results of previous studies; we integrate what was learned into a coherent package that is ready for use.

20 Distribution Availability of Abstract <input checked="" type="checkbox"/> unclassified unlimited <input type="checkbox"/> same as report <input type="checkbox"/> DTIC users	21 Abstract Security Classification Unclassified	
22a Name of Responsible Individual Robert R. Read	22b Telephone (include Area code) (408) 646-2382	22c Office Symbol 55Re

Approved for public release; distribution is unlimited.

Extension of Aggregation and
Shrinkage Techniques Used in
the Estimation of Marine Corps
Officer Attrition Rates

by

John M. Misiewicz
Major, United States Marine Corps
B.S., Pennsylvania State University, 1976
M.S., University of Southern California, 1983

Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN OPERATIONS RESEARCH

from the

NAVAL POSTGRADUATE SCHOOL
September 1989

ABSTRACT

In this thesis we treat the “small cell” problem encountered when building an attrition rate generator for large-scale manpower flow models, specifically for the USMC Officer Corps. Such models have a large number of low-inventory (i.e. small) personnel cells. This presents a dilemma: on one hand we want to preserve as much fidelity as possible in our work by preserving a great deal of detail in each cell; on the other hand our statistical estimation techniques require larger cell sample sizes than intrinsically occur cell-by-cell in actual sample data. Our approach to producing stable attrition rates for such cells involves two efforts: (i) the aggregation of cells into groups that exhibit homogeneity of attrition behavior, and (ii) the development of “shrinkage” estimation techniques for use in the individual groups. A heuristic algorithm is developed and tested to treat the aggregation problem. Empirical Bayes methods are developed to serve the multi-cell estimation requirements needed to preserve the fidelity. Cross validation techniques are used to verify these methods.

The present work builds upon the results of previous studies; we integrate what was learned into a coherent package that is ready for use.

110013
M63653
C.1

THESIS DISCLAIMER

The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

TABLE OF CONTENTS

I.	INTRODUCTION	1
A.	GENERAL	1
B.	BACKGROUND	2
C.	ORGANIZATION	3
D.	SMALL CELL PROBLEM	4
E.	DATA BASE	5
II.	CELL AGGREGATION	7
A.	GENERAL	7
B.	BACKGROUND	7
C.	EXPANSION METHOD	9
D.	AGGREGATION METHOD	14
III.	ESTIMATION METHODS	16
A.	GENERAL	16
B.	EMPIRICAL BAYES	17
1.	Transformed Scale	17
2.	Original Scale	20
C.	EFRON-MORRIS METHOD	23
D.	VECTOR METHOD	25
IV.	CROSS VALIDATION	28
A.	GENERAL	28
B.	MEASURES OF EFFECTIVENESS	28
1.	Mean Absolute Deviation	28
2.	Chi Square	29
3.	Mean Squared Error	30
4.	Vector Method MOEs	31
C.	TEST CASES	31
D.	RESULTS	35

V. CONCLUSIONS AND RECOMMENDATIONS	45
A. CONCLUSIONS	45
B. RECOMMENDATIONS	46
APPENDIX A. AGGREGATION ALGORITHMS	47
A. HEURISTIC ALGORITHM	47
B. INTEGER LINEAR PROGRAM	47
APPENDIX B. COMPUTER PROGRAMS	49
A. GENERAL	49
B. MAIN PROGRAM AND AGGREGATION SUBROUTINES	51
C. ESTIMATION SUBROUTINES	73
D. VECTOR METHOD SUBROUTINE	88
E. EXEC PROGRAM	94
F. SAMPLE DATA FILE	95
APPENDIX C. SAMPLE OUTPUT	98
A. GENERAL	98
B. SAMPLE OUTPUT (TEST CASES 1-30)	98
C. SAMPLE OUTPUT (VECTOR TEST CASES)	101
REFERENCES	102
INITIAL DISTRIBUTION LIST	104

LIST OF TABLES

Table 1.	MOS GROUPS	11
Table 2.	YCS EXPANSION BOUNDS	12
Table 3.	TEST CASES FOR METHODS 1-5	33
Table 4.	TEST CASES FOR VECTOR METHOD	34
Table 5.	SUMMARY OF RESULTS (CASES 1-10)	40
Table 6.	SUMMARY OF RESULTS (CASES 11-20)	41
Table 7.	SUMMARY OF RESULTS (CASES 21-30)	42
Table 8.	SUMMARY OF RESULTS (CASES 7 AND 9 EXPANDED)	43
Table 9.	SUMMARY OF RESULTS (VECTOR METHOD)	44

I. INTRODUCTION

A. GENERAL

The Officer Planning and Utility System (OPUS), a comprehensive and fully integrated manpower management system, is currently being implemented by the U.S. Marine Corps (Decision System Associates, 1986). This system contains a set of computer-based manpower planning models and is used by the Officer Plans Section (MPP-30), Headquarters, U.S. Marine Corps, to produce several manpower planning documents. The system must be able to accurately predict personnel attrition, i.e., officers leaving the service for purposes such as resignation, retirement, discharge, disability, or release. The forecasting of attrition is accomplished by the Marine Corps Officer Rate Projector (MCORP), developed by the Navy Personnel Research and Development Center (NPRDC), San Diego, California (NPRDC, 1985).

The attrition rate generator developed by NPRDC calculates empirical attrition rates using historical data with user-defined weights and threshold parameters (Siegel, 1983). This subjective input makes the current generator susceptible to unintentional misuse.

In support of MCORP, Professor Robert R. Read of the Naval Postgraduate School has been working on the "small cell" problem: applying multiparameter statistical estimation schemes to estimating attrition when there is low personnel inventory, or small cells, which generally exhibit unstable empirical rates.

A comment on terminology is in order. By attrition rate generator we mean methodology for estimating attrition probabilities for the various cells. The expression "empirical rates" refers to the ratio of leavers to inventory for each cell, unmodified by any information contained in "neighboring" cells. In contrast to this, the expression "empirical Bayes" refers to Bayes estimators whose prior parameters are estimated from data.

Accurate forecasting of losses is extremely important to the manpower planner. Overestimating losses causes excess accessions, promotion delays, underutilized personnel and increased costs, while underestimation causes personnel shortages and decreased readiness. The problem is compounded in that all but a few accessions must start at the bottom, i.e., Second Lieutenant, and work their way up to the higher ranks only after many years of service. For example, if a shortage of Lieutenant Colonels arises, it can

only be remedied by promoting more Majors, which has a rippling effect down the rank structure.

B. BACKGROUND

There have been seven Master's theses over the past four years which have studied various aspects of the attrition estimation problem. A concise summary of these works is given by Read (NPS Report NPS55-88-006, 1988, pp.16-23). These studies can be grouped into three general areas: shrinkage methods, cell aggregation and peripheral studies.

The application of a shrinkage method begins by identifying a number of personnel inventory cells, followed by the development of the empirical rates for individual cells and a weighted grand mean of these empirical rates. The final estimate for a cell is a convex combination of its empirical rate and the grand mean. There are numerous methods for accomplishing this, several of which have been applied in previous studies.

Tucker was the first to investigate the application of these methods to attrition estimation. He compared traditional estimators to the James-Stein estimator and the minimax estimator for a few selected grades and occupational fields. His results gave strong support to the James-Stein estimator; minimax was discarded as being too conservative for small cell use. However, there remained pockets of instability for which goodness-of-fit tests failed. (Tucker, 1985)

Following Tucker was Robinson, who introduced the Efron-Morris limited translation shrinkage alternative to augment the James-Stein estimator. These methods were evaluated with a broader set of test cases. Robinson was able to confirm Tucker's results, but the limited translation option failed to provide any consistent relief in the unstable areas. (Robinson, 1986)

The final application of shrinkage methods to estimating officer attrition rates was undertaken by Dickinson. He applied the previously used methods and an empirical Bayes estimator to a new and refined data base. Improved results were obtained, but the instability remained. Dickinson also performed some exploratory side studies dealing with the Freeman-Tukey transform and the use of empirical Bayes methods that allow non-uniform shrinkage, both of which provided the impetus for the present study. (Dickinson, 1988)

These three studies used ad hoc methods to deal with the second general area of study--cell aggregation. Aggregation of cells with low personnel inventory into sets of cells, often of larger inventory, is required when applying these shrinkage methods. The

desire is to use cells which exhibit similar attrition behavior. Two previous studies have investigated this area.

Amin Elseramegy used the Classification and Regression Trees (CART) program, which at the time was newly acquired by the Naval Postgraduate School, in an attempt to form aggregates of cells that exhibited homogeneous attrition behavior. Several difficulties in using this program were encountered, e.g., because of insufficient memory allocation he found it necessary to partition the data base into nine sets and apply CART to each. The resulting aggregations were generally unusable. (Amin Elseramegy, 1985)

Major breakthroughs in cell aggregation were made by Larsen. He applied a hierarchical clustering algorithm to the new data base. The resulting rules for building aggregates are well defined and especially viable from an intuitive point of view. Larsen's work provides the framework for the cell aggregation method developed in Chapter II of this thesis. (Larsen, 1987)

The remaining two theses of the seven were peripheral studies which applied alternate methods to attrition estimation. Hogan attempted multi-year forecasting using exponential smoothing; the smoothing constants were rather unusual and extreme and his results inconsistent (Hogan, 1986). Yacin applied logistic regression in the attempt to develop an attrition rate scheme; the only new results were the identification of some areas that exhibited similar attrition behavior (Yacin, 1987).

This thesis is the first to integrate the two main areas of study. Whereas previous studies of shrinkage methods have used ad hoc aggregation schemes, we now combine the implementation of a defensible aggregation method with empirical Bayes estimators. Moreover, these are applied to a larger and more refined data base. The results have been quite promising in that we have achieved greater stability in attrition rate estimation; we have defined guidelines for a heuristically appealing aggregation scheme; and we have acquired an increased understanding of the data base and developed more efficient ways to use it.

C. ORGANIZATION

The remainder of this introductory chapter provides a more detailed description of the small cell problem and the data base. The aggregation problem is discussed and the proposed aggregation method is presented in Chapter II.

The shrinkage estimation methods, generally classified as empirical Bayes type estimators, are described in Chapter III. Several variations are presented to allow

comparison and to gain further insight into their performance. Testing of these methods is important but for practical purposes must be carried out using sampling methods. The rationale used to select test cases, the cross validation techniques, and the measures of effectiveness used to evaluate the results are discussed in Chapter IV. A discussion of the results of the cross validation is also included in this chapter.

Finally, conclusions and recommendations based on these results are contained in Chapter V.

D. SMALL CELL PROBLEM

Marine Corps officers can be classified and thus partitioned by several attributes. The major partitioning of officers is by grade, years commissioned service (YCS), and military occupational specialty (MOS). Grade describes the position an officer holds in the service. The numbers of officers in each higher grade have a pyramid structure, i.e., there are more officers in the lower grades than in the higher grades. YCS is the total number of years served since becoming a commissioned officer. There is a strong correlation between grade and YCS since an officer generally moves up the grade structure as he gains in YCS. MOS is a four-digit code identifying the specific skill for which a Marine is trained. MOS need not remain constant over an officer's career, although most changes in MOS occur in the early years of commissioned service. An officer has a single primary MOS, however as he develops new job skills he may be assigned one or more additional MOSSs.

For many purposes, partitioning by grade, YCS and MOS is sufficient. However in some applications additional refinement by service component, commissioning source, sex, race or education level may be necessary. Service component consists of three categories: regular officers, reserve officers, and reserves who have augmented to become regulars. It is strongly correlated with commissioning source, i.e., an officer receives a regular or reserve commission depending upon the commissioning source. Both affect an officer's initial service obligation, which is generally three to five years (except aviators, whose obligation is dependent upon the amount of flight training). Officers who receive a reserve commission normally serve three to four years active duty (except aviators), by the end of which they must have either augmented into the regular force or are then separated from active service.

These cross-classifications may be viewed as breaking the officer population into a multidimensional array, with each specific intersection of the classifications called a cell. The total number of possible cells is quite large, on the order of 10^6 . Many of these cells

are structurally infeasible in that no officer could possibly fit the cell characteristics, e.g., there are no Majors with two years commissioned service. The total officer inventory of approximately 20,000 officers is partitioned by the remaining feasible cells; some cells have inventory as large as 50, however most have less than five. An officer's characteristics are dynamic, i.e., as an officer moves through the grade, YCS and MOS structure he moves from one cell to another. As a result, the inventory of the feasible cells is also dynamic and fluctuates between zero and low inventory (less than five) over time.

These sparsely populated cells have very unstable empirical attrition rates. For example, a cell whose inventory is two officers of which one leaves the service during a given time period yields a 50% empirical attrition rate, whereas a cell whose inventory is one officer who remains in service during the same time period yields a 0% attrition rate. It is obvious that neither of these empirical estimations provides a usable attrition rate. Furthermore, these two rates could change dramatically during the next time period, typifying their instability.

Even when more modern estimation techniques (e.g. shrinkage) are applied, these small cells can still create statistical instability, thereby producing intolerably variable attrition rate estimates. The problem then is how to deal with these low inventory cells, or "small cells" in order to achieve stability.

E. DATA BASE

In this thesis we benefit from a refined data base compiled by NPRDC and made available to the Naval Postgraduate School in 1987. This data base, used by Larsen in his aggregation work (Larsen, 1987), was not available for the previous estimation studies at NPS.

The new data base provides more detailed information about the officer population. The grade structure now allows separation of Limited Duty Officers (LDO) as well as Warrant Officers (WO) from unrestricted officers. Officers who have failed selection to the next higher grade can also be identified. YCS is listed instead of length of service (LOS), which became ambiguous when dealing with officers who have prior enlisted service. MOS can now be broken out completely into 236 MOSs or summarized by the 39 occupational fields. Service component and commissioning source are both new categories. Other new categories that are not considered here are education level, race, additional MOSs, and military schools completed. Larsen gives a complete description of the classifications (Larsen, 1987, pp.66-82).

The data base also allows attrition to be broken out by retirement, release, discharge, resignation, etc., but for our immediate purpose we are only concerned with the total number of losses for any reason.

This refinement of the data presents a dichotomy: we can now break the data into more definitive cells to search for homogeneous attrition behavior and stability in estimation, but this leads to an even greater number of low inventory cells.

The new data base contains ten years of inventory and attrition data from the period 1977-1986, a significant improvement from the previous seven year data base covering the period 1977-1983. The inventory data is now obtained from quarterly vice yearly snap-shots of the officer population. The attrition data is annualized, i.e., the attrition count for a cell reflects the number of personnel who leave the service at any time during the year. Attritions are credited to the cell which the officer occupies at the time he leaves.

Two problems arise from this quarterly versus annualized data. First, it is possible for a cell to record zero inventory via the snap-shots, yet be credited with one or more attritions. To avoid this situation, the cell inventory used in all calculations is defined to be the larger of the inventory and the attrition count. This ensures that the inventory for a cell is as least as large as its recorded number of leavers. (This override occurs infrequently; a more sophisticated treatment would require significant model enhancement.) Second, to use the inventory and attrition data together we must divide the inventory data by four. This poses a philosophical problem when invoking a binomial model: the sample size may not be integral. However, for our application the usual mean and variance formulas are usable and can still serve in the interpolative sense.

II. CELL AGGREGATION

A. GENERAL

The aggregation problem takes on new meaning with the use of shrinkage estimators. Originally, aggregation had only one concern: how to pool cells together into a single cell in order to meet a user-defined minimum inventory threshold. This single aggregated cell was then used to determine the attrition rate estimate for the original, unaggregated cell. In this way an estimated value for a cell is obtained by using the grand mean for many cells.

The empirical Bayes multiparameter estimation techniques provide a way to compromise, using both the stability of a grand mean and the specific information of an individual cell. Now we pool cells together and obtain a number of cells that meet the user-defined minimum inventory threshold. It is important to note that we should be able to use a lower inventory threshold with empirical Bayes, thus retaining individual cell behavior to a greater extent. It is also important to use cells with homogeneous attrition behavior in the aggregation process.

B. BACKGROUND

The aggregation method currently used by MCORP is called the Small Cell Override Methodology (NPRDC, 1985, Appendix H). It is used to solve the original aggregation problem, i.e., if a cell is below the user-defined threshold, then cells are adjoined to the original cell until the threshold is met. The process for selecting cells for adjunction is rather crude, and large-scale with only a few levels (prior to using the entire officer corps). The attrition rate estimate for the original cell is the empirical rate from this aggregated cell.

To begin the process, the user defines a cell for which an attrition rate estimate is required by grade, YCS and MOS. The user also defines the minimum cell inventory threshold (and other parameters which are not relevant here). If the cell he identifies meets the threshold, no aggregation is required and the empirical attrition rate is determined. If the cell is below the threshold, additional cells must be added until the threshold is met.

This search for additional cells occurs by expanding by YCS and MOS, with grade remaining fixed throughout. Expanding in this sense means changing the YCS or MOS parameter to identify the additional cells to be added to the original cell. Initially, the

single cell is expanded by YCS. For example, if the original cell's grade/YCS/MOS was Capt/7/0802, the cells identified by Capt/6/0802, Capt/8/0802, etc., are added sequentially until the threshold is met. This YCS expansion has an upper bound at the 20 YCS point; an obvious boundary for attrition behavior due to retirement eligibility. If the original cell's YCS is above 20, then 20 would serve as the lower YCS bound.

If the threshold is not met after the YCS expansion, the override method starts over with the original cell and expands by MOS. Each MOS belongs to one of nine MOS groups which are defined along traditional Marine Corps functional areas, e.g., all helicopter pilot MOSs are grouped together as are all combat support MOSs. MOS expansion adds those cells identified by the MOSs in the same MOS group as the MOS of the original cell for the original YCS and grade. If the threshold is not met, all the MOSs in the MOS group are expanded by YCS in the same manner as the YCS expansion discussed previously.

If this MOS group and YCS expansion is unsuccessful, the override method starts over with the original cell and expands by all MOSs for the original grade and YCS. If necessary, all the MOSs are expanded by YCS as before.

Cell aggregation using this expansion method can potentially include all MOSs and YCS bounded only at the 20 year point. The desire to aggregate using cells with homogeneous attrition behavior is obviously compromised. Larsen provides a more comprehensive description of the current method (Larsen, 1987, pp.16-22).

Larsen examined attrition behavior in the MOS and YCS structure. He applied a hierarchical clustering algorithm in an attempt to find MOSs and YCSs that displayed homogeneous attrition behavior. He confirmed the belief that YCS is an important factor. The YCS expansion bounds he proposed reflect points at which officers reach the end of their initial service obligation as well as when they are eligible for retirement, which makes them especially viable from an intuitive point of view. Larsen also found that some MOSs did not cluster strictly by functional areas. This was especially significant in the aviation community. Whereas the previous data base allowed aviators to be considered only as one occupational field, the refined MOS information was able to identify six distinct homogeneous groups of aviators.

Larsen uses these results to define more refined MOS groups and YCS boundaries. To avoid the giant expansion leap from MOS group to all MOSs, he proposed a hierarchy of small MOS groups, large MOS groups and major MOS groups developed by observing which MOSs tend to exhibit similar attrition behavior. Homogeneity is greatest within the MOS group, and becomes successively worse as we move to the large

MOS group and then the major MOS group. Each MOS is assigned to a small MOS group. Small MOS groups combine to make a large MOS group, and large MOS groups combine to make a major MOS group.

Each small MOS group is assigned a set of YCS expansion bounds. Due to the different attrition behavior of the small MOS groups with respect to YCS, three different sets of YCS expansion bounds are proposed.

Initial expansion is by YCS within the specified boundaries, with grade and MOS held constant. If more expansion is required, we retain this aggregated cell and expand by small MOS group for the original grade and YCS. If the aggregated cell is still below the threshold, the MOSSs in the small MOS group are expanded by YCS. Subsequent expansion to large MOS group and YCS, and major MOS group and YCS is accomplished until the threshold cell inventory is met.

Unlike the current expansion method, expansion using Larsen's proposed method will not cross defined MOS groups or YCS bounds to ever include all MOSSs and YCSs bounded only at the 20 year point. Larsen provides a more detailed description of his recommended expansion rules (Larsen, 1987, pp.45-61).

C. EXPANSION METHOD

We now address the methods used to obtain the cells required for use with empirical Bayes estimation techniques. Expansion continues to mean finding more cells to be used, however we no longer simply add these cells to the original cell to form a single aggregated cell. The cells identified by the expansion process are now aggregated together to produce a number of cells. After the discussion of the expansion process in this section, an actual aggregation scheme is introduced in the next section.

To begin the estimation process, the manpower planner defines a specific cell by grade, YCS and MOS. The attributes service component and commissioning source are also included as possible cell descriptors for the purposes of this study. All other descriptors listed in the data base--sex, education level, additional MOSSs, race and military schools--are ignored. Loss types are considered as a combined total, i.e., in this study we do not discriminate among the various types of losses. The first three user-defined descriptors--grade, YCS and MOS--are single-value inputs. The last two descriptors, service component and commissioning source, can be single values, or either one of them can be treated as a vector of values for each single cell. This vector is collapsed (total the components) during the aggregation process, i.e., all records which meet any of the vector's values are included in the same cell. As in the previously described expansion

methods, only YCS and MOS change during expansion, the remaining cell descriptors remain constant.

To use shrinkage techniques, the amount of expansion required not only depends upon the minimum cell inventory threshold but also upon a new input parameter: the threshold number of cells. These two parameters are denoted:

1. T_0 - cell inventory threshold. The minimum average inventory for a cell obtained by averaging the cell inventory over the ten years of data.
2. K_0 - threshold number of cells. The minimum number of aggregated cells whose inventory exceeds T_0 . These aggregated cells are the input cells for the empirical Bayes techniques.

For example, if $T_0 = 5.0$ and $K_0 = 10$, the expansion algorithm continues until at least ten aggregated cells, each with average inventory 5.0 or larger are obtained. Since we are concerned primarily with the small cell problem the values of T_0 and K_0 used are selected to range from five to 30. It is also presumed that T_0 is less than or equal to K_0 . These threshold values can certainly exceed 30 for other applications, however the resulting cells are not considered small and their attrition behavior most likely would not be as unstable, therefore not requiring special attention.

Prior to explaining the expansion process, we first define the MOS groups and YCS bounds. We have adopted much of Larsen's work in this area; many of the changes are minor but are necessary for implementation purposes.

The general idea of a hierarchy of MOS groups is repeated, as shown in Table 1. Each MOS belongs to a small MOS group, a large MOS group and a major MOS group. Listed are 14 small MOS groups, which combine to make six large MOS groups, which combine to make four major MOS groups. For example, small MOS groups one and two form large MOS group one, and small MOS groups three through six form large MOS group two. Large MOS groups one and two, which collectively contain small MOS groups one through six, make up major MOS group one. Major MOS group one contains only ground MOSSs, and major MOS group two contains only aviation MOSSs. Major MOS groups three and four are special cases as discussed below.

A subjective decision was made to keep the ground MOSSs in groups defined along the more traditional functional areas. This is reflected in small MOS groups one through six. For estimation purposes it is advantageous if the cell inventories are not too variable in size (Carter and Rolph, 1974, p.882). It is also desirable to avoid having too many MOSSs in each small MOS group. This allows the expansion to occur more gradually, and is especially important for small values of T_0 and K_0 . As a result, MOS 0302

Table 1. MOS GROUPS

Group Name	MOSs	Small MOS Group	Large MOS Group	Major MOS Group
Combat	0302	1		
Combat Support	0802 1302 1802 1803	2	1	
Combat Service 1	0180 0202 2502 2602	3		
Combat Service 2	3415 4002 4302 5803	4	2	
Combat Logistics	0402 3002 3060 3502 6002	5		
Air Control	7204 7208 7210 7320	6		
Fixed Wing Pilots	7501 7511 7522 7542 7543 7545 7576	7	3	
F-18 Pilots	7521 7523	8		
Rotary Wing Pilots +	7556 7557 7562 7564 7565 7566 7587	9	4	
Naval Flight Officers +	7508 7509 7563 7581 7583 7584 7585 7586 7588	10		
Basic Ground	0101 0201 0301 0401 0801 1301 1801 2501 2601 3001 3401 3501 4001 4301 4401 5801 6001 7201 7301 9901	11	5	3
Student Aviators	7580 7597 7598 7599	12		
Basic Pilots	7500 7510 7520 7540 7550 7560 7575	13		
Lawyers	4402	14	6	4

(infantry) is placed alone in a small MOS group. This MOS contains approximately 15% of the total officer population, and therefore its respective cells normally contain large inventory. The MOSSs in small MOS group two also contain fairly large inventory, therefore are grouped together and their first expansion is with MOS 0302. The remaining ground MOSSs in small MOS groups three through six have similarly small inventory.

The aviation small MOS groups (seven through ten) remain relatively unchanged from Larsen's recommendations. MOS 7564 (CH-53 pilot), was removed from a ground MOS group and added to small MOS group nine, which reflects its functional area. MOSSs 7551 (C-9 pilot), 7552 (TC-4C pilot), 7555 (UC-12B pilot) and 7559 (CT-39 pilot)

were deleted since they are not primary MOSs. MOS 7530 (basic pilot VMFA (F-4)) was deleted since it is not a current MOS. (MCO P1200.7G, 1988)

Officers who have not acquired sufficient schooling or field experience to qualify for a primary MOS listed in small MOS groups one through ten are gathered together as basic officers or students in small MOS groups 11-13. These officers are generally second lieutenants or junior first lieutenants with three or fewer YCS. They are disregarded for the remainder of the study because their attrition rates are extremely low; probably because none of the officers in these groups have reached the end of their initial obligations.

MOS 4402 (lawyers) is considered a special case and is not addressed in this study.

All MOSs listed in Table 1 are primary MOSs for unrestricted officers as listed in the current Military Occupational Specialties Manual (MCO P1200.7G, 1988). It would be a logical and relatively simple extension of this table to create additional groups containing LDO and WO MOSs. These grades are not considered in this study and therefore their respective MOSs are excluded from the table.

Several of these seemingly ad hoc decisions to alter Larsen's recommended MOS groups are due to the YCS expansion bounds shown in Table 2. Every effort was made to group MOSs with similar YCS expansion bounds to allow for feasible implementation of the expansion algorithm. This is especially applicable when expanding to large and major MOS groups.

Table 2. YCS EXPANSION BOUNDS

MOS Group	Small MOS Groups	Bounded YCS Groups
Fixed Wing Pilots, F-18 Pilots, Lawyers	7, 8, 14	(1-6, 8-19) (7) (20-25) (26)
Rotary Wing Pilots, Naval Flight Officers	9, 10	(1-5, 8-19) (6,7) (20-25) (26)
All Others	1-6, 11-13	(1-3, 6-19) (4,5) (20-25) (26)

The YCS expansion bounds reflect the maximum expansion allowed from the initial YCS defined by the user. For example, if the original cell's grade/YCS/MOS is Capt/9/7501, we see from Table 1 that this MOS belongs to small MOS group seven. Thus its YCS expansion bounds are listed on the first line of Table 2. The value of nine

for YCS falls in the first YCS range, thus we could expand using all YCSs from one through 19, excluding seven. If the YCS for this original cell had been seven, no YCS expansion would be allowed.

These YCS expansion bounds are used with the MOS groups to define the additional cells which can be used with the original cell to obtain the required number of cells, K_0 , each with minimum average inventory, T_0 . The expansion stages are:

1. Stage 1 - Locate the small MOS group which contains the user-defined MOS. The initial cells are those specified by the MOSs in this group for the user-defined YCS, grade, service component and commissioning source (grade, service component and commissioning source remain fixed throughout the expansion process and thus are not repeated). These cells are aggregated to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 2.
2. Stage 2 - Expand by incrementing YCS (YCS-1, YCS+1, YCS-2, YCS+2, etc.) within the YCS bounds listed in Table 2 for all MOSs in the small MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 and 2 and go to Stage 3.
3. Stage 3 - Expand to the large MOS group for the single user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 4.
4. Stage 4 - Expand by incrementing YCS for the large MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 through 4 and go to Stage 5.
5. Stage 5 - Expand to the major MOS group for the single user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise go to Stage 6.
6. Stage 6 - Expand by incrementing YCS for the major MOS group. After each YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to T_0 . After aggregation, if the number of cells is greater than K_0 , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, stop. No more expansion is allowed. Inform the user that the thresholds are unattainable. Do not cross any major MOS group or YCS bounds.

Two points about the expansion process are emphasized. First, we retain the cells identified by all previous stages as we progress to the next stage. As stated before, the degree of homogeneity decreases as we move from small to large to major MOS groups.

Thus we want to locate as many cells from the small MOS group as possible before we expand to the large MOS group, and then locate as many cells from the large MOS group as possible before expanding to the major MOS group. The YCS expansion for each group may be different, e.g., the small MOS group may be expanded by all YCSs within the given YCS range, but the large MOS group may only be expanded by a few YCSs before the thresholds are attained.

The second point is that, when aggregating cells, any aggregation that was performed previously is discarded and all cells currently identified are pooled and made available for aggregation. This affords the aggregation algorithm greater flexibility and could create more aggregated cells than if the aggregated cells from previous stages were left intact, thereby keeping the amount of expansion to a minimum.

The aviation small MOS groups (seven through ten) make up the only major MOS group (two) that contains different YCS bounds, i.e., small MOS groups seven and eight have different YCS expansion with regard to year six than do small MOS groups nine and ten. To implement the expansion algorithm in a computer program, this difference is overcome by using the YCS bounds for the original user-defined MOS. For example, suppose MOS 7501 from small MOS group seven is the original MOS. If MOS expansion continues into the major MOS group, the MOSs in small MOS groups nine and ten would follow small MOS group seven's YCS expansion bounds.

In summary, this method of grouping MOSs should provide greater homogeneity among cells which are used in estimating attrition rates. Unlike the current method, ground and aviation MOSs are never used together. The YCS bounds provide a logical and effective way to treat periods of different attrition behavior. However, the greater the expansion the less homogeneous the cells become, which should be kept foremost in mind when setting the threshold parameters.

D. AGGREGATION METHOD

While the expansion steps are being undertaken in order to achieve the threshold levels specified by the user, those cells with inventory less than T_0 must be gathered up into larger, aggregated cells whose combined inventory exceeds T_0 . In order to limit the expansion to as few additional MOSs and YCSs as possible, we desire to maximize the number of aggregated cells obtained at any stage of the expansion.

The term maximization suggests the possible use of linear programming (LP). While an LP would ensure maximization, this would not be a trivial problem to solve, i.e., the LP relaxation would almost certainly fractionate cells, using their inventory in more than

one aggregated cell. This is not allowed since a cell may be assigned intact to only one aggregated cell. Thus an integer LP would be required which would typically contain 500 or more integer variables. This method would not be expedient in terms of computer usage, especially considering the potential number of integer LPs that may have to be solved for a single estimation cycle.

While we are trying to maximize the number of aggregated cells, it would be satisfactory to obtain close to the maximum if we could preclude the expense in computer time required by an integer LP. For this reason, a heuristic "greedy" algorithm was developed. Complete descriptions of the heuristic algorithm and the LP formulation are contained in Appendix A. The performance of this heuristic is discussed along with the results of the empirical Bayes methods in Chapter IV.

III. ESTIMATION METHODS

A. GENERAL

Once the cell aggregation phase is completed, we begin the attrition rate estimation process. The following notation is used to define the cell data

$$\begin{aligned} K &= \text{number of cells} \\ T &= \text{number of years of data.} \end{aligned} \quad (1)$$

Then for $i = 1, \dots, K$ and $t = 1, \dots, T$

$$\begin{aligned} N_i(t) &= \text{inventory of cell } i \text{ in year } t \\ Y_i(t) &= \text{number of attritions in cell } i \text{ in year } t. \end{aligned} \quad (2)$$

The cell data is assumed to be independent binomial, i.e., $Y_i(t) \sim \text{Bin}(N_i(t), p_i)$. A success is defined to be an attrition, i.e., an officer from that cell leaves the service during the year. The empirical attrition rate for cell i is given by the Maximum Likelihood Estimator (MLE)

$$\hat{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)}. \quad (3)$$

This estimate of p works well for cells with large inventory, but not those with small inventory, which is most often the case in our application.

The MLE has been shown to be dominated by shrinkage methods for $K \geq 3$ (Carter and Rolph, 1974; Efron and Morris, 1975; Casella, 1985). These methods find a grand mean or central attrition rate for the group of cells and a shrinkage factor for each cell. Previous theses have primarily used a common shrinkage factor for all cells; we now allow this shrinkage factor to vary from cell to cell. Each cell's MLE is shrunk towards the central rate by its shrinkage factor. In this way, attrition information from one cell "spills over" into other cells.

The shrinkage methods are developed under the theoretical assumption that the data is normally distributed. Most of the previous studies using empirical Bayes methods have used independent normal data with constant variance (Efron and Morris, 1972,

1973, 1975; Dickinson, 1988). Some applications have used binomial data, using a transformation to make it behave more like normal data (Carter and Rolph, 1974; Efron and Morris, 1975). In Carter and Rolph's estimation of fire alarm probabilities, transformation of the binomial data did not have a large effect on the results (Carter and Rolph, 1974). Our application allows us to investigate the impact of the transformation when applied with more extreme values of p .

Six variations of the empirical Bayes method are applied to the attrition rate estimation problem. The first four are similar in that they use the same iterative procedure to compute the amount of shrinkage for each cell. Of these four, two are on the transformed scale and two on the original scale. Each scale includes two methods of computing the cell variance: one method where the variance is time dependent and the other where it is time independent. The two variance calculations, if they produce like results, provide supporting evidence for the assumption that the data is independent and identically distributed over time. This assumption is certainly questionable, since an officer who remains in a given MOS will move through the YCS and grade cell structure in a predictable manner. As a result, variance that is constant in time (time independent) may not perform as well as one that allows for time variation. The fifth method uses a different iterative procedure to determine the amount of shrinkage and is addressed separately in paragraph III.C.. The final method breaks the cell data into its vector components (service component or commissioning source) before shrinkage techniques are applied and is addressed in paragraph III.D..

B. EMPIRICAL BAYES

1. Transformed Scale

We begin our application of empirical Bayes methods on the transformed scale in an effort to overcome some of the weaknesses in our assumptions. The transformation we use is the Freeman-Tukey transform, a modification of the basic arcsin transformation for binomial data. Its purpose is to stabilize the variance at one and make the data behave more like normal random variables. The form used is

$$X_i(t) = \frac{1}{2} \sqrt{N_i(t) + .5} \left\{ \arcsin\left(\frac{2Y_i(t)}{N_i(t) + 1} - 1\right) + \arcsin\left(2 \frac{Y_i(t) + 1}{N_i(t) + 1} - 1\right) \right\}. \quad (4)$$

Now, let

$$XT_i(t) = \frac{X_i(t)}{\sqrt{N_i(t) + .5}} \quad \text{for } t = 1, \dots, T_i \quad (5)$$

except when $N_i(t) = 0$ (no inventory in year t), in which case $XT_i(t)$ does not exist and we reduce T_i by one. The time average of the transformed values for cell i becomes

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t). \quad (6)$$

We now need to compute the variance of these time averages. Two methods are used: the first calculation is time dependent, i.e., the variance changes over time, the second is time independent.

The transform stabilizes the variance at one for large values of n and non-extreme values of p . These requirements on n and p are often violated in our application, therefore we have many combinations of n and p for which the variance is less than one. Dickinson was able to discover an interpolative formula which provides a good approximation for the variance of the transformed values, $X_i(t)$, for small values of n and p , and $K \geq 3$ (Dickinson, 1988, pp.8-11). This variance is given by

$$Var(X_i(t)) = \min\{1, V(X_i(t))\} \quad (7)$$

where $V(X_i(t))$ is found by solving

$$V(X_i(t)) = \alpha (X_i(t) + C)^{b_1} (X_i(t) + C - 1)^{b_2} \quad (8)$$

with

$$C = \sqrt{N_i(t) + .5} \left(\frac{\pi}{2} \right) \quad (9)$$

and

$$\alpha = 1.6835 \quad b_1 = -.8934 \quad b_2 = .9881. \quad (10)$$

Equation (8) obviously breaks down if $X_i(t) + C < 1$. When this occurs, we set $X_i(t) + C = 1.001$ and continue. The effect is to use a small but positive variance. The

value of one in Equation (7) dominates for about $X_i(t) + C \geq 2.2$. The variance of the time average is then

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_l(t)) = \frac{1}{T_i^2} \sum_t \frac{Var(X_i(t))}{N_i(t) + .5}. \quad (11)$$

The second method of computing the variance is the more familiar one. Continuing from Equation (6), the variance of the transformed values is given by

$$Var(XT_l) = \frac{1}{T_i - 1} \sum_t (XT_l(t) - XTB_i)^2. \quad (12)$$

The variance of their average is therefore

$$Var(XTB_i) = \frac{1}{T_i} Var(XT_l). \quad (13)$$

Regardless of which variance calculation we use, the same iterative algorithm is used to determine the empirical Bayes estimate for each cell. This estimate, XEB_i , is found by solving

$$XEB_i = \frac{A}{A + Var(XTB_i)} XTB_i + \frac{Var(XTB_i)}{A + Var(XTB_i)} XBB \quad (14)$$

where XEB_i , XTB_i and $Var(XTB_i)$ are cell specific, XBB is the (weighted) grand mean or central attrition rate, and A is the variance of the prior distribution of the cell means. These latter two values must be estimated simultaneously using the following iterative algorithm.

We initialize the algorithm with $A = 0$ and store the previous value of A by

$$A_0 \leftarrow A. \quad (15)$$

Now compute the (weighted) grand mean, XBB . Let

$$\alpha_i = \frac{1}{A + Var(XTB_i)} \quad (16)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} . \quad (17)$$

Then

$$XBB = \sum_{i=1}^K \gamma_i XTB_i . \quad (18)$$

The updated value of A becomes

$$A \leftarrow A - \frac{K - 1 - \sum_{i=1}^K \alpha_i (XTB_i - XBB)^2}{\sum_{i=1}^K \alpha_i^2 (XTB_i - XBB)^2} . \quad (19)$$

If $A \leq 0$, set $A = 0$ and exit. This represents the case when there is 100% shrinkage toward the grand mean. If $A > 0$, then check $|A - A_0| < \epsilon$ (e.g., $\epsilon = .0001$). If false, return to Equation (15) for another iteration. If true, the iterations have converged. Exit with the current values of A and XBB for use in Equation (14) to solve for the XEB_i .

Close study of Equation (14) shows that the amount of shrinkage changes from cell to cell since the variance terms are generally not equal. Specifically, cells with higher variance are shrunk more than those with lower variance. In addition, if A is small the shrinkage is greater towards XBB . As $A \rightarrow \infty$, the shrinkage is minimal and the individual cell means dominate.

Once the XEB_i are determined, these values must be transformed back to the original scale. We use

$$\hat{p}_i = \frac{1}{2} \{1 + \sin(XEB_i)\} . \quad (20)$$

2. Original Scale

We return to the assumption of binomial data for original scale calculations. As in the transformed scale, two methods to calculate the variance are used. We begin

with

$$XT_i(t) = \hat{p}_i(t) = \frac{Y_i(t)}{N_i(t)} . \quad (21)$$

As before, if $N_i(t) = 0$ (no inventory in year t), $XT_i(t)$ does not exist and we reduce T_i by one. This leads to the time average for cell i as

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t) = \frac{1}{T_i} \sum_t \hat{p}_i(t) . \quad (22)$$

The variance calculation which is time dependent, i.e., changes over time, is given by

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{1}{T_i^2} \sum_t \frac{\hat{p}_i(t)(1 - \hat{p}_i(t))}{N_i(t)} . \quad (23)$$

We return to Equation (15) with these variance values to perform the iterative algorithm for finding the empirical Bayes estimate, XEB_i , given by Equation (14). Since we are already in the original scale, the transformation given in Equation (20) is ignored, i.e., $\hat{p}_i = XEB_i$.

A problem arises while performing the iterations if a cell has $Y_i(t) = 0 \forall t$ (zero attrition for every year). In this case, the variance given by Equation (23) equals zero. When this value is used in Equation (16), the formula for α_i becomes undefined. We resolve this problem using the Laplace Law of Succession. Assume that $Y_i(t) \sim Bin(N_i(t), p_i)$ and let

$$p_i^* = \frac{Y_i(t) + 1}{N_i(t) + 1} \quad \text{and} \quad q_i^* = \frac{N_i(t) - Y_i(t)}{N_i(t) + 1} \quad (24)$$

be the estimates as prescribed by this law, i.e., Bayes estimator using uniform prior. Then

$$Var\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{p_i^* q_i^*}{N_i(t)} = \frac{\left(\frac{Y_i(t) + 1}{N_i(t) + 1}\right)\left(\frac{N_i(t) - Y_i(t)}{N_i(t) + 1}\right)}{N_i(t)} . \quad (25)$$

If $Y_i(t) = 0$, then

$$Var\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{\left(\frac{1}{N_i(t)+1}\right)\left(\frac{N_i(t)}{N_i(t)+1}\right)}{N_i(t)} = \frac{1}{(N_i(t)+1)^2}. \quad (26)$$

This value is used as the summand in Equation (23) whenever $Y_i(t) = 0$ (zero attrition in any year).

For comparison purposes we again compute an alternate variance which is time independent. Continuing from Equation (22), let

$$\tilde{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)}. \quad (27)$$

The alternate variance is given by

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{\tilde{p}_i(1-\tilde{p}_i)}{T_i^2} \sum_t \frac{1}{N_i(t)}. \quad (28)$$

The problem with cells that have $Y_i(t) = 0 \forall t$ (zero attrition for every year) also occurs here, since the variance given by Equation (28) would equal zero. Using the same concept as before, we obtain the formula

$$Var(XTB_i) = \frac{\sum_t N_i(t)}{\left(1 + \sum_t N_i(t)\right)^2} \frac{1}{T_i^2} \sum_t \frac{1}{N_i(t)}. \quad (29)$$

However in this case, this variance formula is necessary only if all years have zero attrition.

As before, we return to Equation (15) to perform the iterative algorithm for finding the empirical Bayes estimate, XEB_i , given by Equation (14).

C. EFRON-MORRIS METHOD

This method is a modification of the iterative algorithm used to estimate A and XBB given by Efron and Morris (Efron and Morris, 1973, pp.127-129). It differs from the method given by Equations (14) through (19) in that it allows the variance of the prior, A , to change from cell to cell. It also gives greater weight to the cells with low variance, and reduces to the James-Stein estimator when the cell variances are constant.

Only one scenario for this method is considered, corresponding to the initial transformed scale, time dependent variance case. Thus, Equations (4) through (11) are repeated, and we begin from the point where we are entering the iterative algorithm. To simplify the following equations, let $D_i = \text{Var}(XTB_i)$ as given by Equation (11).

We initialize the algorithm with $A_i = 0$ and $SP_i = 0$ (previous values of S) for $i = 1, \dots, K$. Let

$$\alpha_i = \frac{1}{A_i + D_i} \quad (30)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} . \quad (31)$$

Then

$$\hat{X} = \sum_{i=1}^K \gamma_i XTB_i \quad (32)$$

and

$$S_i = (XTB_i - \hat{X})^2 . \quad (33)$$

Now set $i = 1$ and let

$$SN_i = \sum_{j \neq i} \frac{S_j - D_j}{(A_j + D_j)^2} \quad (34)$$

and

$$SD_i = \sum_{j \neq i} \frac{1}{(A_j + D_j)^2}. \quad (35)$$

We then use the Newton-Raphson iteration method to solve

$$A_i = \frac{(S_i - 3D_i) + (A_i + D_i)^2 SN_i}{3 + (A_i + D_i)^2 SD_i} = g(A_i). \quad (36)$$

First set $AP_i \leftarrow A_i$ for $i = 1, \dots, K$ (previous values of A_i). The updated value for A_i becomes

$$A_i \leftarrow A_i - \frac{A_i - g(A_i)}{1 - g'(A_i)}. \quad (37)$$

If $A_i \leq 0$, set $A_i = 0$, let $i = i + 1$, and return to Equation (34). If $A_i > 0$, then test $|A_i - AP_i| > \varepsilon$. If true, return to Equation (36). If false, let $i = i + 1$ and return to Equation (34).

In either case after incrementing i , if $i = K + 1$, we exit and test $|S_i - SP_i| < \varepsilon \forall i$. If false, we update $SP_i \leftarrow S_i$ and return to Equation (30) with updated values of A_i . If true, the iterations have converged and we must finalize the estimators, XEM_i . Let

$$d_i^* = 3 + (A_i + D_i)^2 \sum_{j \neq i} \frac{1}{(A_j + D_j)^2} \quad (38)$$

and

$$B_i = \left(1 - \frac{4}{d_i^*}\right) \frac{D_i}{A_i + D_i}. \quad (39)$$

If $B_i > 1$, set $B_i = 1$, or if $B_i < 0$, set $B_i = 0$. Then

$$XEM_i = \hat{X} + (1 - B_i)(XTB_i - \hat{X}). \quad (40)$$

This equation is comparable to Equation (14), which was used to determine the transformed scale estimates, XEB_i , using the previous iterative algorithm. The quantity B_i is

the amount of shrinkage toward the grand mean, \hat{X} . The corresponding quantity in Equation (14) is $\frac{Var(XTB_i)}{A + Var(XTB_i)}$.

To obtain \hat{p}_i , the XEM_i must be transformed back to the original scale using XEM_i , in place of XEB_i in Equation (20).

D. VECTOR METHOD

This method is similar to the previous methods in the sense that it uses the aggregated cells produced to meet the defined threshold levels. However, prior to the estimation process, we now partition each aggregated cell by either service component or commissioning source, thus obtaining cells whose elements are vectors. The procedure given by Efron and Morris, modified to compensate for the assumed variance of the time averages, provides the framework for this method (Efron and Morris, 1972, pp.341-344).

The separation by service component or commissioning source requires us to define a third index: the components of the vector. Let

$$P = \text{number of service components/commissioning sources.} \quad (41)$$

Then for $i = 1, \dots, K$, $j = 1, \dots, P$ and $t = 1, \dots, T$

$$\begin{aligned} N_{ij}(t) &= \text{inventory of cell } i \text{ and vector component } j \text{ in year } t \\ Y_{ij}(t) &= \text{number of attritions in cell } i \text{ and vector component } j \text{ in year } t. \end{aligned} \quad (42)$$

Before we had K cells with scalar information, but now we need a $K \times P$ matrix where

$$\sum_{j=1}^P N_{ij}(t) = N_i(t) \quad \text{and} \quad \sum_{j=1}^P Y_{ij}(t) = Y_i(t). \quad (43)$$

A requirement for this method is that $K > P + 2$, for reasons that will soon become obvious.

We begin by defining $X_{ij}(t)$ as the transformed value for $N_{ij}(t)$ and $Y_{ij}(t)$ as given by Equation (4). Continuing in similar manner as the previous transformed scale methods, let

$$XT_{ij}(t) = \frac{X_{ij}(t)}{\sqrt{N_{ij}(t) + .5}} \quad \text{for } t = 1, \dots, T_{ij} \quad (44)$$

except when $N_{ij}(t) = 0$, in which case $XT_{ij}(t)$ does not exist and we reduce T_{ij} by one.

The time averages of the transformed values are then

$$XTB_{ij} = \frac{1}{T_{ij}} \sum_t X T_{ij}(t). \quad (45)$$

Here we obtain a vector of grand mean values, with each of the P grand means defined by

$$XBB_j = \frac{1}{K} \sum_{i=1}^K XTB_{ij}. \quad (46)$$

The transformed scale estimate, δ_{ji} , is then found by solving

$$\delta_{ji} = XBB_j + \{I_P - (K - P - 2)\tilde{S}^{-1}\}(XTB_{ji} - XBB_j) \quad (47)$$

where I_P is the identity matrix of order P , and \tilde{S}^{-1} is found as discussed below. Reversal of the ij index in this and subsequent equations simply means the transpose of the $K \times P$ matrix to a $P \times K$ matrix.

To solve for \tilde{S}^{-1} , we begin by defining

$$\tilde{S} = X_{ji} X_{ji}^T \quad (48)$$

where

$$X_{ji} = (XTB_{ji} - XBB_j)\sqrt{V_{ji}}. \quad (49)$$

The V_{ji} matrix is the modification required by our application. (The multiplication in Equation (49) is element-wise as opposed to normal matrix multiplication.) The Efron and Morris method was developed under the assumption that $XTB_{ij} \sim N(\theta_{ij}, 1)$, whereas we are using

$$XTB_{ij} \sim N\left(\theta_{ij}, \frac{1}{T_{ij}^2} \sum_t \frac{1}{N_{ij}(t) + .5}\right) \quad (50)$$

provided that $XT_{ij}(t)$ has variance of one. Therefore

$$V_{IJ} = \frac{1}{T_{IJ}^2} \sum_t \frac{1}{N_{IJ}(t) + .5} . \quad (51)$$

We use the requirement that the $P \times P$ matrix resulting from the operations within the brackets in Equation (47) must be nonnegative definite to solve for \tilde{S}^{-1} without having to actually compute its inverse. We proceed by doing an eigenanalysis of \tilde{S} , which is seen by Equation (48) to be a real symmetric matrix. We form the diagonal matrix E , which has the eigenvalues, e_j , as its diagonal elements, and the matrix Γ , which has the corresponding eigenvectors as its columns. For any $e_j < (K - P - 2)$, we replace it with the value $(K - P - 2)$. The eigenanalysis provides us with the solution to

$$\begin{aligned} \tilde{S} \Gamma_j &= \Gamma_j e_j \\ \text{or } \tilde{S} \Gamma &= \Gamma E. \end{aligned} \quad (52)$$

Post-multiplying by Γ^T , we obtain

$$\tilde{S} = \Gamma E \Gamma^T \quad (53)$$

since Γ is ortho-normal and therefore $\Gamma \Gamma^T = I_p$. We then have

$$\tilde{S}^{-1} = (\Gamma E \Gamma^T)^{-1} = \Gamma E^{-1} \Gamma^T \quad (54)$$

which is easily solved since E^{-1} is found by replacing the diagonal elements of E by their reciprocal. This solution for \tilde{S}^{-1} is then used in Equation (47) to solve for the transformed scale estimates, δ_{ji} . To obtain the attrition rate estimate for a cell, \hat{p}_{ji} , we use the inversion formula given by Equation (20) with δ_{ji} in place of XEB_i .

IV. CROSS VALIDATION

A. GENERAL

The six estimation methods discussed in Chapter III are evaluated using cross validation of the data base. This consists of successively holding out one year's data while the other nine years are used to estimate that year's attrition rates. Three measures of effectiveness (MOEs) are used to evaluate the validity of our assumptions and the performance of the estimation methods. Two of these are original scale MOEs--mean absolute deviation (MAD) and chi square statistic. The third is a transformed scale MOE--mean squared error (MSE). Test cases are chosen as input. The results of the cross validation are then discussed.

B. MEASURES OF EFFECTIVENESS

1. Mean Absolute Deviation

The MAD is probably the most useful MOE to the manpower planner. Our version is augmented to display overestimation and underestimation information. Along with the MAD we observe the magnitude of our errors in both directions, which is especially important since the cost of overestimating is generally not the same as the cost of underestimating. While it does not provide a specific value or standard to gauge the performance of our estimation methods, it does provide very useful insight into tendencies to consistently underestimate or overestimate.

For comparison of the estimation methods, we desire a MAD measure that does not depend upon cell inventories, yet still displays the overage/underage information. For these reasons, we use the attrition rate estimates, \hat{p}_i , as opposed to the estimated number of attritions, $(\hat{p}_i \cdot N_i(t))$ (where t = validation year), in our MAD calculations. For those estimates obtained in the transformed scale, the XEB_i are inverted back to the original scale using Equation (20) prior to calculating this MOE.

We define the empirical attrition rate for cell i in validation year t as

$$p_i^a = \frac{Y_i(t)}{N_i(t)} \quad (55)$$

except when $N_i(t) = 0$ (no inventory in cell i for the validation year). In this case we do not compute the cell's deviation from the estimated attrition rate since it would

artificially create an overage situation. Therefore, we reduce K by one and continue with the remaining cells (the reduced value of K is then used in the following formulas).

The MAD measures generated for each validation year are

$$\frac{K_u}{K} = \text{fraction of cells with underage} \quad (56)$$

where K_u is the number of cells which have underage,

$$\frac{\sum_i (p_i^a - \hat{p}_i)^+}{\sum_i |p_i^a - \hat{p}_i|} = \text{fraction of MAD due to underage} \quad (57)$$

and

$$MAD = \frac{1}{K} \sum_i |p_i^a - \hat{p}_i|. \quad (58)$$

We also calculate the average MAD over the validation years. Here we use a weighted average, since the number of cells may have been different in some validation years, i.e., a reduced value of K was used in these years. The weighted average takes the form

$$\text{Avg } MAD = \frac{\sum_t K_t MAD_t}{\sum_t K_t} \quad (59)$$

where K_t is the (possibly reduced) number of cells used in validation year t .

2. Chi Square

The chi square test is used as an indicator of how well the binomial model serves as a description of the attrition process. The test statistic is

$$X_{(K)}^2(t) = \sum_i \frac{(Y_i(t) - \hat{p}_i N_i(t))^2}{N_i(t) \hat{p}_i (1 - \hat{p}_i)} \quad (60)$$

where t is the validation year. As with the MAD calculations, if $N_i(t) = 0$ we reduce K by one and continue. Additionally, if $\hat{p}_i = 0$ or 1, the denominator equals zero and the summand is undefined. The same course of action is used if this occurs--reduce K by one and continue. Those estimates obtained in the transformed scale are inverted back to the original scale prior to using Equation (60).

This MOE can be used as a gauge. The chi square statistic given by Equation (60) has expected value K and variance $2K$. We are looking for a X^2 value that is less than two standard deviations to the right of the mean, or

$$X_{(K)}^2 \leq K + 2\sqrt{2K} . \quad (61)$$

A weighted average chi square is computed in the same manner as the weighted average MAD in Equation (59). However, if the number of cells and thus the degrees of freedom, K , are different over the validation years a problem arises in determining the degrees of freedom for the weighted average. We solve this dilemma by assuming that the weighted average chi square has the original value of K degrees of freedom.

3. Mean Squared Error

The MSE is used to check the validity of our theoretical basis. It is the average squared deviation of the estimated rate from the actual rate, both rates on the transformed scale. The actual rate used is the transformed validation year data. The MSE is defined as

$$L(\delta, \mu) = \frac{1}{K} \sum_i (\delta_i - \mu_i)^2 \quad (62)$$

where

$$\begin{aligned} \delta_i &= XEB_i \\ \mu_i &= XT_i(t) \quad (t = \text{validation year}) . \end{aligned} \quad (63)$$

Again, if $N_i(t) = 0$, we reduce K by one and continue. A weighted average MSE is also computed similar to Equation (59).

The MSE also has a standard to gauge our model. Using Equations (5) and (12) we can compute a baseline variance for any given validation cell. The MSE for that cell, when compared to the baseline value, provides a figure to gauge the value of using shrinkage estimators instead of the cell averages, XTB_i . There is considerable variability

in these ratios, ranging from 20% to 100%, but 80% appears to be a fair median figure. For example, for cell variances computed from Equation (12) running about 0.15, the MSE hovers about 0.12.

4. Vector Method MOEs

The MOEs discussed above require slight modification before being applied to the vector method described in paragraph III.D.. Recall that this method uses K cells with service component or commissioning source broken out into a vector of length P . An attrition rate estimate, δ_{ij} , is obtained for each of the $K \times P$ matrix components. Thus now we have KP estimates which are compared to the corresponding empirical rates for the validation year. Equations (55) through (63) are modified by replacing all i subscripts with ij , replacing all summations over i by double summations over i and j , and replacing all instances of K by the product KP .

C. TEST CASES

The selection of test cases takes on great importance since they provide the foundation for comparison of these methods. It would be impossible to test every permutation of input parameters; therefore we seek a representative fraction of these which would give an accurate account of the performance of our aggregation and estimation methods. Because we are using a different data base from previous theses on estimation methods, no attempt to duplicate their test cases was made.

An approach based upon Latin square experimental design principles was used to select 30 test cases for the first five estimation methods. The test cases for the vector estimation method are addressed later. In determining the test cases, we randomized when possible and intervened to force pairings only when necessary. To begin, we selected values for the input parameters-- T_0 , K_0 , grade, YCS and MOS. Service component and commissioning source are ignored for these test cases, i.e., all classifications of both are accepted.

To ensure proper representation from small MOS groups one through ten, one MOS from each group was randomly selected: 0302, 1802, 2502, 4002, 3060, 7204, 7545, 7523, 7557 and 7563. Since YCS and grade are strongly correlated, these parameters were selected jointly. To ensure each YCS range within the bounded YCS groups was represented along with a fair representation of grades, four grade/YCS pairs were selected: 1Lt/4 YCS, Capt/7 YCS, LtCol/20 YCS and LtCol(failed select)/26 YCS. The two threshold parameters were also selected jointly, resulting in ten pairs (T_0/K_0): 30.0/30, 20.0/30, 20.0/20, 10.0/30, 10.0/20, 10.0/10, 5.0/30, 5.0/20, 5.0/10 and 5.0/5.

With these choices in place, it was necessary to combine them to define the actual test cases. It was decided to limit the grade/YCS pairs for these cases to 1Lt/4 YCS and Capt/7 YCS due to the large values for the first five threshold pairs. With ten MOSs specified, we sought ten test cases. Thus, each of the first five threshold pairs was listed twice. Each of the four aviation MOSs was randomly assigned to one of the five threshold pairs; the six ground MOSs were then randomly assigned to the remaining pairs. The two grade/YCS pairs were then randomly assigned within a set of common threshold pairs, e.g., for the two cases with T_0 / K_0 of 30.0/30, one was randomly assigned 1Lt/4 YCS, the other was then assigned Capt/7 YCS.

All four grade/YCS pairs would be used with the five remaining threshold pairs. Thus 20 more test cases were generated, with each of the five threshold pairs listed four times. Each MOS was randomly assigned to two distinct threshold pairs, ensuring that the large and major MOS groups were evenly spread throughout the pairs. The four grade/YCS pairs were assigned in random order to each set of common threshold pairs, ensuring that they were evenly spread across large and major MOS groups. The 30 test cases are summarized in Table 3.

The input parameters for six vector test cases were selected from the 30 test cases: Nos. 2, 3, 6, 10, 11 and 20. A small number of vector test cases was initially chosen to investigate the possible advantages of the vector method. If this method appeared to be favorable, then further testing would be conducted.

The six test cases contain a cross section of the input parameters. They include three ground and three aviation MOSs, and use each of the first three grade/YCS pairs twice. The grade/YCS pair of LtCol(FS)/26 YCS was not used because of its extremely low inventory numbers, which when broken out into a vector would have been of little exploratory use. These cases also include six different T_0 / K_0 pairs.

Each of the vector test cases is used twice: first with service component and then with commissioning source as the vector component. All three service components--regular, augmented regular and reserve--were used as vector components. Rather than use all 15 commissioning sources (these 15 are listed below Table 4) as vector components (many of them would contain little or no inventory) five commissioning sources for the ground test cases and five for the aviation test cases were chosen. These five were determined to be the sources which contain the largest percentage of inventory for the respective ground or aviation MOSs. The specific commissioning sources selected along with the other vector test case input parameters are summarized in Table 4.

Table 3. TEST CASES FOR METHODS 1-5

No.	T_0	K_0	MOS	S : L : M	YCS	Grade
1	30.0	30	0302	1 : 1 : 1	4	1Lt
2	30.0	30	7523	8 : 3 : 2	7	Capt
3	20.0	30	3060	5 : 2 : 1	7	Capt
4	20.0	30	7563	10 : 4 : 2	4	1Lt
5	20.0	20	2502	3 : 2 : 1	7	Capt
6	20.0	20	7557	9 : 4 : 2	4	1Lt
7	10.0	30	7204	6 : 2 : 1	4	1Lt
8	10.0	30	1802	2 : 1 : 1	7	Capt
9	10.0	20	7545	7 : 3 : 2	7	Capt
10	10.0	20	4002	4 : 2 : 1	4	1Lt
11	10.0	10	2502	3 : 2 : 1	20	LtCol
12	10.0	10	7557	9 : 4 : 2	26	LtCol(FS)
13	10.0	10	7545	7 : 3 : 2	7	Capt
14	10.0	10	0302	1 : 1 : 1	4	1Lt
15	5.0	30	4002	4 : 2 : 1	4	1Lt
16	5.0	30	0302	1 : 1 : 1	20	LtCol
17	5.0	30	7204	6 : 2 : 1	26	LtCol(FS)
18	5.0	30	7563	10 : 4 : 2	7	Capt
19	5.0	20	3060	5 : 2 : 1	7	Capt
20	5.0	20	7545	7 : 3 : 2	20	LtCol
21	5.0	20	1802	2 : 1 : 1	26	LtCol(FS)
22	5.0	20	7563	10 : 4 : 2	4	1Lt
23	5.0	10	7204	6 : 2 : 1	20	LtCol
24	5.0	10	4002	4 : 2 : 1	26	LtCol(FS)
25	5.0	10	7523	8 : 3 : 2	4	1Lt
26	5.0	10	1802	2 : 1 : 1	7	Capt
27	5.0	5	2502	3 : 2 : 1	7	Capt
28	5.0	5	7557	9 : 4 : 2	20	LtCol
29	5.0	5	3060	5 : 2 : 1	4	1Lt
30	5.0	5	7523	8 : 3 : 2	26	LtCol(FS)

(S : L : M = Small MOS Group : Large MOS Group : Major MOS Group)

Table 4. TEST CASES FOR VECTOR METHOD

No.	T_0	K_0	MOS	YCS	Grade	Service Comp	Comm Source
2	30.0	30	7523	7	Capt	1 2 3	(all)
2	30.0	30	7523	7	Capt	(all)	1 2 3 5 11
3	20.0	30	3060	7	Capt	1 2 3	(all)
3	20.0	30	3060	7	Capt	(all)	1 3 7 10 11
6	20.0	20	7557	4	1Lt	1 2 3	(all)
6	20.0	20	7557	4	1Lt	(all)	1 2 3 5 11
10	10.0	20	4002	4	1Lt	1 2 3	(all)
10	10.0	20	4002	4	1Lt	(all)	1 3 7 10 11
11	10.0	10	2502	20	LtCol	1 2 3	(all)
11	10.0	10	2502	20	LtCol	(all)	1 3 7 10 11
20	5.0	20	7545	20	LtCol	1 2 3	(all)
20	5.0	20	7545	20	LtCol	(all)	1 2 3 5 11

Service Component:

- 1 - regular
- 2 - augmented regular
- 3 - reserve

Commissioning Sources used:

- 1 - U.S. Naval Academy
- 2 - Platoon Leader Class-Aviation
- 3 - Platoon Leader Class-Ground
- 5 - Aviation Officer Candidate
- 7 - Officer Candidate Course-Ground
- 10 - Enlisted Commissioning Program
- 11 - NROTC-Scholarship

Commissioning Sources not used:

- 4 - Platoon Leader Class-Law
- 6 - Marine Aviation Cadet
- 8 - Officer Candidate Course-Law
- 9 - Officer Candidate Course-Women
- 12 - NROTC-Ground College
- 13 - NROTC-Aviation College
- 14 - NESEP
- 15 - All Other

D. RESULTS

For each test case, we apply the aggregation method to meet the threshold levels and then execute the estimation methods. While the ultimate use of these methods is to obtain an attrition rate estimate for the original cell, inspection of these estimates would be of little value in evaluating and comparing the estimation methods. Thus the output from the program takes the form of the MOEs.

The inclusion of the entire output from every test case would not only be cumbersome but would provide an inadequate means of comparing the methods. Therefore the output is summarized in Tables 5 through 7. They contain the output from the first five estimation methods only; the output from the vector test cases is presented later. Sample output for the six methods is contained in Appendix C.

The results summaries list the test case number, the cell inventory threshold, T_0 , and the actual number of cells used, K . The level of expansion required to achieve these parameter levels is also listed. For example, test case one had a cell inventory threshold of 30.0, and 24 aggregated cells were obtained by expanding the small, large and major MOS group by YCSs four and five. The value for K is often different from the threshold number of cells, K_0 , listed in Table 3. When K is less than K_0 , maximum expansion occurred and the threshold was unattainable. When K is greater than K_0 , the expansion was the least amount possible to remain above the thresholds. From these test cases we can see that it is difficult to meet the threshold number of cells exactly.

The results summaries then list the weighted average MOEs for each of the five estimation methods. The first row within each test case contains the MAD values, the second row the chi square values and the third row the MSE values. The maximum desired chi square value as given by Equation (61) is listed in parentheses, e.g., for test case one this value is 37.9. This affords easier comparison of the chi square values for the different methods. The values of MSE for both original scale methods are blank because MSE is a transformed scale MOE only.

Before discussing the results in general, some additional comments about specific test cases are necessary. Test case four could not be executed by the Efron-Morris method. This is because one of the aggregated cells contains zero attrition for all ten years of data. As a result, the iterative algorithm does not converge.

Test case 12 was not possible because not even one aggregated cell meeting the cell inventory threshold was obtained with maximum expansion in major MOS group two. This extremely low inventory problem was generally true for all test cases involving the LtCol(FS)/26 YCS pair. Test cases 17, 21 and 24 obtained only three aggregated cells

with maximum expansion in major MOS group one. Test case 30 was also from major MOS group two, and obtained only one aggregated cell meeting the cell inventory threshold. As a result, test case 30 was changed to Major(FS)/18 YCS so that results for these low thresholds could be obtained.

As the thresholds became low (test cases 23-30) cells with inventory much larger than T_0 were being obtained prior to any aggregation. This was especially true for the 1Lt/4 YCS and Capt/7 YCS pairs. To avoid masking the results of low inventory thresholds by actually using large inventory cells, the service component/commissioning source parameters for test cases 26, 27 and 29 were changed. Rather than accepting all classifications of these parameters, only one classification for each was accepted. Thus test case 26 was executed with regular/USNA, test case 27 was executed with augmented regular/PLC-ground, and test case 29 was executed with regular/NROTC-scholarship.

We now focus our attention on the results of these test cases with respect to the MOEs. The weighted average MAD figures vary little within each test case over the five methods. This suggests that the total deviation from the validation year empirical attrition rate was the same for all methods. However, this figure does not identify whether the deviations were overestimations or underestimations. The fraction of MAD from underage (not listed in the results summaries) was studied to gain more insight into this important consideration. For each of the 29 test cases (no results for test case 12), a weighted average fraction of MAD from underage was computed for each of the five estimation methods (weighted by the number of cells just as the weighted averages for the MOEs). A weighted average of these 29 values was then computed. This overall weighted average indicates the tendency of the method to underestimate or overestimate--averages above 0.5 indicate a tendency to underestimate; averages below 0.5 indicate a tendency to overestimate. The author is unaware of any information comparing the relative costs of underage and overage. Hence, as a default, we look for values of 0.5, which is a balance between overestimation and underestimation. The averages calculated were: TS1 = 0.426; TS2 = 0.436; OS1 = 0.481; OS2 = 0.512; and EM = 0.452. Although the MAD figures were generally the same for all methods, these averages indicate that the tendencies to overestimate or underestimate may not be the same. The original scale methods seem to have achieved more balance than the transformed scale methods.

The chi square results were not entirely consistent across test cases nor across methods within a test case. These results are discussed first by comparisons between test cases; then by comparisons within test cases.

Of the first ten test cases, only three (Nos. 3, 5 and 8) had weighted average chi square values within the acceptable range. These three test cases expanded only into the large MOS group, whereas of the seven test cases which were unacceptable, all but one (No. 10) expanded into the major MOS group. Of the last 20 test cases, only four had chi square values outside the acceptable range (Nos. 13, 14, 15, and 18). Of these four, two expanded into the large MOS group, and two into the major MOS group. All the test cases with unacceptable values had either 1Lt/4 YCS or Capt/7 YCS pairs. They were fairly well spread across MOS groups. None of the test cases with lower thresholds (Nos. 19-30) had unacceptable chi square values. This suggests that lower thresholds, which result in less expansion, achieve more acceptable results with respect to this MOE.

To investigate this claim further, different combinations of threshold levels for test cases seven and nine were used. The results are contained in Table 8. These results reinforce the claim that lower thresholds are in fact better, since in both cases the chi square results improved as the thresholds, and therefore the level of expansion, were reduced. When comparing these extra test cases, keep in mind that the chi square values for each set of threshold values should be compared to the acceptable range for that specific number of cells; comparisons across test cases with different values of K are not valid. An important aspect of the argument for lower thresholds is that the thresholds must be considered jointly. For example, in test case seven, with a T_0/K pair of 10.0/6, the chi square values were nearly acceptable, whereas with 5.0/19 they were clearly unacceptable. Thus we should be most aware of the value $T_0 \times K_0$.

We now turn our attention to comparing the chi square values within a test case. Several test cases had chi square values that varied significantly over the estimation methods (Nos. 4, 6 and 22). These three all had 1Lt/4 YCS pairs and were large MOS group four. In test cases four and six the chi square values for the transformed scale methods were not too much larger than the desired maximum; the values for the original scale methods were significantly larger than the desired maximum. In test case 22 the chi square values for the transformed scale methods were acceptable, however the values for the original scale methods were again significantly larger than the desired maximum.

Several other test cases had varying chi square values, but to a lesser degree. In test case eight, only the transformed scale methods had acceptable chi square values, the original scale methods exceeded the desired maximum, although not by a significant margin. In test case 19, only the OS2 method exceeded the desired maximum. All methods for test cases 16, 25, and 27 were within the desired maximum, however the chi square values varied to a large degree over the five methods. Thus, using the chi square

MOE, it appears that the transformed scale methods were generally the same, and as a group outperformed the original scale methods.

The MSE was used only with the transformed scale methods, and thus no comparison with original scale methods can be made. The values for this MOE were generally equal between methods within a test case, and acceptable overall.

The results for the vector method test cases are summarized in Table 9. The table lists the value $K \times P$ (instead of K) because this is the number of estimates obtained and compared to the validation year empirical attrition rates with this method.

Test case two with commissioning source as the vector component had to be modified because only seven aggregated cells were obtained. As a result, $K = P + 2$, and the vector method could not be conducted. Therefore, commissioning source three (Platoon Leader Class-ground) was deleted as a vector component and the test case run with only four commissioning sources (1, 2, 5 and 11). Test case 20 with service component as the vector component was infeasible. By starting with a low cell inventory threshold (5.0), when the cells were broken out into the vector components their inventory became extremely low. As a result, when validating year five, two of the cells had zero inventory for all of the remaining nine years for service component three (reserve). Thus the value for XTB_{ij} , given by Equation (45), becomes undefined and the method cannot be completed.

The results of the vector method with respect to the MOEs is similar to the results of the previous five estimation methods. This method produced acceptable MAD and MSE values, but its chi square values were fairly inconsistent. Test cases two and ten had unacceptable chi square values for both vector components; test case six had an unacceptable chi square value with service component as the vector component. Recall that these test cases also had unacceptable values with the vector component collapsed.

No fair comparison with the first five estimation methods can be made using the summarized results. Obviously the MAD and MSE quantities will be larger since we are comparing three to five times as many estimates to empirical rates with the vector method. Thus a different evaluation technique must be used.

The vector method is designed to take advantage of any correlation between the cells when broken out into vector components. To see if this is occurring we must look at the matrix \tilde{S}^{-1} as given by Equation (54). In all of the vector test cases, this matrix was essentially diagonal, indicating little correlation between the vector components. In addition, all of the eigenvalues, which become the elements of the diagonal matrix E, were less than $(K - P - 2)$. Therefore, the eigenvalues were replaced by this quantity and the

Table 5. SUMMARY OF RESULTS (CASES 1-10)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
1	30.0	24	S:(4,5) L:(4,5) M:(4,5)	MAD X(37.9) MSE	0.102 98.79 0.079	0.101 99.28 0.078	0.102 100.99	0.102 100.96	0.103 101.23 0.080
2	30.0	8	S:(7) L:(7) M:(7)	MAD X(16.0) MSE	0.091 28.16 0.077	0.090 27.68 0.076	0.092 28.71	0.091 28.68	0.091 27.73 0.076
3	20.0	31	S:(1-3,6-19) L:(6-8)	MAD X(46.7) MSE	0.056 37.49 0.062	0.056 37.80 0.062	0.055 39.58	0.055 42.85	0.055 38.38 0.062
4	20.0	23	S:(1-5,8-19) L:(1-5,8-19) M:(1-5,8-19)	MAD X(36.6) MSE	0.029 39.34 0.035	0.029 47.36 0.037	0.026 95.41	0.024 139.14	
5	20.0	20	S:(1-3,6-19) L:(7)	MAD X(32.6) MSE	0.048 20.75 0.048	0.049 20.83 0.049	0.047 24.34	0.047 24.20	0.048 21.41 0.049
6	20.0	22	S:(1-5,8-19) L:(1-5,8-19) M:(3-5)	MAD X(35.3) MSE	0.029 40.42 0.037	0.029 50.70 0.039	0.027 90.93	0.025 127.86	0.029 65.20 0.040
7	10.0	32	S:(4,5) L:(4,5) M:(4)	MAD X(48.0) MSE	0.129 111.67 0.137	0.130 113.23 0.137	0.130 112.64	0.130 113.64	0.133 114.28 0.140
8	10.0	28	S:(1-3,6-19) L:(1-3,6-11)	MAD X(43.0) MSE	0.039 34.37 0.039	0.038 34.70 0.040	0.039 45.16	0.038 49.60	0.039 35.54 0.040
9	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
10	10.0	27	S:(4,5) L:(4,5)	MAD X(41.7) MSE	0.128 64.33 0.137	0.129 65.92 0.137	0.129 65.62	0.128 66.61	0.127 62.64 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

matrix E always had $(K - P - 2)$ as its diagonal elements. Because these results indicated no worthwhile improvements over the first five methods, no further testing of the vector method was conducted.

Finally, the performance of the heuristic aggregation algorithm listed in Appendix A was also evaluated. For each test case, the total inventory of cells below T_0 was summed and this value divided by T_0 . The integer part of this number provides an upper bound on the number of aggregated cells that can be obtained by any aggregation technique. This upper bound was compared to the actual number of aggregated cells produced by the algorithm. The algorithm achieved the maximum in 71.4% (20 of 28) of the test cases. It achieved one less than the maximum in 21.4% (6 of 28) of the test cases, and two less than the maximum in 7.2% (2 of 28) of the test cases (only 28 test cases required aggregation: No. 12 was infeasible; No. 14 all cells were above T_0). This performance is acceptable for our application.

Table 6. SUMMARY OF RESULTS (CASES 11-20)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
11	10.0	11	S:(20-25) L:(20-25)	MAD X(20.4) MSE	0.109 18.79 0.141	0.106 19.75 0.142	0.108 19.96	0.107 20.53	0.107 18.99 0.139
12	10.0	0	S:(26) L:(26) M:(26)	MAD X(0.0) MSE					
13	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
14	10.0	10	S:(4.5) L:(4,5)	MAD X(18.9) MSE	0.113 57.80 0.102	0.110 60.07 0.103	0.113 57.71	0.113 57.80	0.115 59.36 0.104
15	5.0	32	S:(4,5) L:(4,5)	MAD X(48.0) MSE	0.137 69.96 0.156	0.140 70.72 0.158	0.139 70.27	0.139 72.01	0.139 68.15 0.155
16	5.0	32	S:(20-25) L:(20-25) M:(20-22)	MAD X(48.0) MSE	0.122 39.41 0.146	0.122 40.38 0.146	0.121 44.35	0.121 47.84	0.121 42.27 0.148
17	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.0189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
18	5.0	29	S:(6,7) L:(6,7) M:(7)	MAD X(44.2) MSE	0.141 79.04 0.176	0.141 78.23 0.176	0.142 78.61	0.141 81.29	0.141 78.84 0.177
19	5.0	24	S:(2,3,6-10)	MAD X(37.9) MSE	0.085 28.95 0.122	0.082 29.28 0.123	0.080 30.91	0.084 43.36	0.080 35.44 0.132
20	5.0	19	S:(20-25) L:(20-25) M:(20)	MAD X(31.3) MSE	0.111 17.29 0.113	0.113 17.29 0.114	0.113 18.92	0.106 23.37	0.110 18.28 0.114

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 7. SUMMARY OF RESULTS (CASES 21-30)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
21	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.167 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
22	5.0	22	S:(1-5,8-19) L:(3,4)	MAD X(35.3) MSE	0.032 23.56 0.059	0.042 15.03 0.041	0.024 63.10	0.022 92.85	0.032 22.56 0.056
23	5.0	9	S:(20-25) L:(20)	MAD X(17.5) MSE	0.121 8.12 0.141	0.121 8.19 0.141	0.119 8.65	0.121 9.25	0.120 8.17 0.137
24	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
25	5.0	10	S:(1-6,8-19) L:(1-6)	MAD X(18.9) MSE	0.050 5.09 0.044	0.051 4.78 0.037	0.020 15.35	0.020 16.54	0.048 4.85 0.039
26	5.0	11	S:(1-3,6-19) L:(6,7)	MAD X(20.4) MSE	0.138 13.61 0.184	0.138 13.65 0.186	0.138 14.09	0.135 16.10	0.135 14.28 0.189
27	5.0	6	S:(6-8)	MAD X(12.9) MSE	0.070 4.64 0.075	0.069 4.55 0.074	0.055 6.88	0.050 9.41	0.068 4.60 0.074
28	5.0	7	S:(20,21)	MAD X(14.5) MSE	0.114 7.59 0.140	0.116 7.67 0.143	0.118 7.99	0.113 8.74	0.116 8.37 0.147
29	5.0	5	S:(4,5)	MAD X(11.3) MSE	0.170 6.36 0.211	0.169 6.23 0.210	0.168 7.64	0.167 8.25	0.169 8.06 0.281
30	5.0	6	S:(1-6,8-19) L:(17-19)	MAD X(12.9) MSE	0.112 6.15 0.136	0.110 6.40 0.136	0.110 7.31	0.104 8.73	0.108 6.42 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 8. SUMMARY OF RESULTS (CASES 7 AND 9 EXPANDED)

No.	T_0	K	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
7-1	10.0	32	S:(4,5) L:(4,5) M:(4)	X(48.0)	111.67	113.23	112.64	113.64	114.28
7-2	10.0	17	S:(4,5) L:(4)	X(28.7)	45.31	45.99	45.90	46.58	43.68
7-3	10.0	6	S:(4,5)	X(12.9)	13.08	12.98	13.41	13.53	13.03
7-4	5.0	19	S:(4,5) L:(4)	X(31.3)	49.28	49.53	49.23	50.84	46.91
7-5	5.0	7	S:(4,5)	X(18.9)	14.42	14.27	14.82	14.93	14.18
7-6	5.0	4	S:(4)	X(9.7)	9.20	8.88	9.22	9.20	9.49
9-1	10.0	14	S:(7) L:(7) M:(7)	X(24.6)	38.85	37.50	39.59	39.62	40.26
9-2	10.0	4	S:(7)	X(9.7)	10.35	10.14	10.58	10.57	10.11
9-3	5.0	17	S:(7) L:(7) M:(7)	X(28.7)	44.95	42.87	44.40	46.03	46.15
9-4	5.0	5	S:(7)	X(11.3)	11.91	11.69	12.16	12.15	11.64

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

Table 9. SUMMARY OF RESULTS (VECTOR METHOD)

No.	T_0	KP	Vector Component	MOE	Vector Method
2	30.0	24	SC	MAD X(37.9) MSE	0.149 61.03 0.229
2	30.0	28	CS	MAD X(43.0) MSE	0.222 115.34 0.398
3	20.0	93	SC	MAD X(120.3) MSE	0.158 110.96 0.219
3	20.0	155	CS	MAD X(190.2) MSE	0.157 132.37 0.201
6	20.0	66	SC	MAD X(89.0) MSE	0.062 109.19 0.074
6	20.0	100	CS	MAD X(128.3) MSE	0.083 58.58 0.081
10	10.0	81	SC	MAD X(106.5) MSE	0.212 251.63 0.368
10	10.0	120	CS	MAD X(151.0) MSE	0.321 707.85 0.625
11	10.0	42	SC	MAD X(60.3) MSE	0.193 44.86 0.214
11	10.0	60	CS	MAD X(81.9) MSE	0.222 53.55 0.225
20	5.0	72	SC	MAD X(0.0) MSE	
20	5.0	100	CS	MAD X(128.3) MSE	0.254 55.92 0.245

SC - service component

CS - commissioning source

V. CONCLUSIONS AND RECOMMENDATIONS

A. CONCLUSIONS

The results indicate that the desired stability in estimating attrition rates for low inventory cells has been achieved with the aggregation and estimation methods presented in this study. The use of "shrinkage" methods applied to well selected groups of cells allows for the achievement of quality estimates of attrition in the face of low inventory numbers for the individual cells.

None of the six estimation methods stood out as a clear favorite. The vector method did not provide any additional benefits using service component or commissioning source as vector components. Since it is a more complicated method and has the potential to become unsolvable with zero inventory vector components, it appears to be the least favorite. Perhaps more success would be obtained with alternative classifications for the vector component.

The Efron-Morris method also involves more computational effort than the first four empirical Bayes methods. Its performance was very much similar to the transformed scale, time dependent variance method since the only difference between them is the iterative algorithm used to determine the amount of shrinkage. The Efron-Morris method has the potential to become unsolvable when a cell has zero attrition for every year--a distinct possibility when dealing with low inventory cells. This suggests that it is the least favorite of the first five methods.

Of the remaining four methods, there seems to be only small difference between the time dependent variance and the time independent variance methods on the same scale. In test cases where the chi square values were marginal or unacceptable, the time dependent variance methods were usually better. In these same test cases, the transformed scale methods performed better than the original scale methods. Therefore, if one method was to be singled out as best, it would be the first method: transformed scale, time dependent variance.

The tendency to overestimate or underestimate as shown by the weighted average fraction of MAD from underage may also be a consideration when selecting a method. An analysis of this type must weigh the costs of overestimating versus the costs of underestimating, which generally are not the same. This type of an analysis is beyond

the scope of this study. In addition, further testing of the methods would be required to gain a more accurate estimate of this tendency.

The threshold levels also seem to strongly influence the performance of the estimation methods. It appears that expansion past the large MOS group begins to detract from homogeneous attrition behavior. While further study would be required to identify optimal threshold levels, it is apparent that both thresholds should not exceed 20.0, and the value of $T_0 \times K_0$ should not exceed 100.

A method for dealing with cells whose inventory is much greater than T_0 must be developed. In some test cases, cells with inventory three or more times as large as T_0 were obtained and used in the estimation process. This did not seem to affect the results, as they were present in almost all test cases. These cells could be disaggregated into multiple cells with inventory closer to the threshold, although the effect of this has not been determined.

B. RECOMMENDATIONS

The proposed aggregation method should be implemented as a method of identifying additional cells to be used in the attrition rate estimation process. This method provides greater homogeneity of attrition behavior among cells over the current method.

The empirical Bayes estimation methods developed in this study are recommended for use in estimating the attrition rates for low personnel inventory cells.

Overall, the empirical Bayes estimation methods when combined with the proposed aggregation method have achieved the stability in attrition rate estimation that is required to provide a foundation for manpower planning.

APPENDIX A. AGGREGATION ALGORITHMS

A. HEURISTIC ALGORITHM

The heuristic algorithm for aggregating cells is as follows:

- Given a set of cells, S , and the (time average) inventory of each cell, INV_c , partition S into two subsets as follows:

$$\begin{aligned}S_1 &= \{c : c \in S; INV_c \geq T_0\} \\S_2 &= \{c : c \in S; INV_c < T_0\}\end{aligned}$$

- Put the cells in S_1 into the set of aggregated cells, K .

- Order the cells in S_2 according to size of their inventory:

$$INV_1 \leq INV_2 \leq \dots \leq INV_n \quad n = |S_2|$$

- Start with c_n , the cell in S_2 with the largest inventory. Find the smallest cell in S_2 , c' , that when united with c_n the resulting total inventory will meet or exceed T_0 . Combine its data with c_n , put c_n into K , and remove c' from S_2 (the modified set S_2 will now be referred to as S_2^-). Repeat the procedure with c_{n-1} , and so forth.

- If no cell in S_2^- when combined with the current largest cell, c_{n-i} , exceeds T_0 , use the next largest cell, c_{n-i-1} , and remove c_{n-i-1} from S_2^- . This will create an aggregated cell that is still below threshold. Return to the procedure in Step 4 of trying to find c' . If no such cell is contained in S_2^- , use c_{n-i-2} , and so forth.

- Continue this procedure until the sum of all the cells remaining in S_2^- is less than T_0 . These cells are sequentially added to the aggregated cells in K in Step 7.

- Add the largest cell in S_2^- to the smallest cell in K , and update its average inventory. Add the next largest cell in S_2^- to the current smallest cell in K , and update the inventory. Continue until all cells in S_2^- have been used.

We now have $|K|$ aggregated cells which exceed the threshold, T_0 , to use in the attrition rate estimation procedure.

B. INTEGER LINEAR PROGRAM

The formulation as an integer linear program is as follows:

Index Use

c cell (before aggregation)

a aggregated cell

Given Data

INV_c average inventory of cell c

T_0 threshold cell inventory

Binary Variables

$X_{c,a}$ 1 indicates use cell c in aggregated cell a

Z_a 1 indicates use cell a for aggregation

Formulation

$$\text{MAX } \sum_a Z_a$$

subject to

$$\sum_a X_{c,a} \leq 1 \quad \forall c \quad \text{(each cell used at most once)}$$

$$\sum_c INV_c \cdot X_{c,a} \geq T_0 \cdot Z_a \quad \forall a \quad \text{(aggregated cell must have size} \geq T_0 \text{)}$$

$$X_{c,a}, Z_a \in \{0,1\}$$

APPENDIX B. COMPUTER PROGRAMS

A. GENERAL

A computer program written in FORTRAN is used to conduct the cross validation using the methods developed in this thesis. Although the program consists of 33 subroutines, 6 function subroutines, and over 2000 lines of code, it can be easily summarized by breaking it into the two areas of the thesis: cell aggregation and estimation methods.

The main program and aggregation subroutines (listed in paragraph B) read the input parameters and execute the expansion and aggregation methods discussed in Chapter II. An existing program written by Luis Uribe, an independent contractor under the direction of Professor Read, underwent extensive modification to fulfill these requirements. The input parameters-- T_0 , K_0 , MOS, YCS, grade, service component(s), and commissioning source(s)--are read by Subroutine GETPAR either in the interactive mode via the terminal or by using MC87 EXEC (listed in paragraph E). Uribe uses an innovative method to estimate the amount of expansion required to meet the threshold parameters. This approach precludes the requirement to read the data base after each step in the expansion process which would be extremely computer time intensive. Inventory information is extracted from the data base and stored in a separate data file for each pay grade (a sample data file and the program used to create it are listed in paragraph F). The data file is accessed via the user's A-disk which is significantly faster than accessing the data base through MVS. Subroutine READET reads the appropriate data file for the specified grade and constructs a table of cells for those records that are in the same major MOS group as the user defined MOS, and meet the service component and commissioning source parameters. All YCSs are accepted, since the extent of expansion is not yet determined. Function NCEVAL screens this table using the current level of expansion and estimates the number of aggregated cells with average inventory greater than or equal to T_0 that will be obtained. If this number is less than K_0 , Subroutine EXPAND begins the expansion stages as described in paragraph II.C.. After each increment of expansion, NCEVAL screens the table and estimates the number of aggregated cells that will be obtained. This loop through EXPAND and NCEVAL continues until the estimated number of aggregated cells meets the threshold, K_0 . The estimated number of cells and the level of expansion are then displayed on the terminal screen.

The user may elect to go forth and read the data base to determine the actual number of aggregated cells obtained, or may elect to change the level of expansion.

The level of expansion is changed through the variable AGGPCT. This variable estimates the effectiveness of the heuristic aggregation method listed in Appendix A. To estimate the number of aggregated cells that will be obtained, NCEVAL compares the cells which meet the expansion criteria to the minimum inventory threshold, T_0 . Those that are greater than T_0 will obviously produce one aggregated cell. The inventory of those that are less than T_0 is summed. The estimated number of cells is then the total of the number of cells greater than T_0 and AGGPCT times the sum of the cell inventory below T_0 divided by T_0 . The variable AGGPCT is initially set at 0.9, but can be interactively changed via the terminal. By increasing the value of AGGPCT we can decrease the level of expansion; by decreasing the value of AGGPCT we can increase the level of expansion.

Once we decide to go forth and read the actual data base, Subroutine READER extracts records meeting the expansion criteria developed using EXPAND and NCEVAL and pools them into cells. Subroutine AGGREG aggregates these cells to meet the average inventory threshold, T_0 . The actual number of aggregated cells obtained is then compared to the threshold number of cells, K_0 . Again, the user has the option of changing the level of expansion to obtain more or fewer cells, or continuing on to the estimation process.

The first five estimation methods are called by SUBROUTINE MC87BZ (listed in paragraph C). The estimation methods are contained in separate subroutines: EBTS1, EBTS2, EBOS1, EBOS2 and EMTS (EB-empirical Bayes; EM-Efron-Morris; TS-transformed scale; OS-original scale; 1-time dependent variance; 2-time independent variance). The iterations required by the first four methods are conducted in Subroutine EBITER; the Efron-Morris iterations are conducted in Subroutine EMITER. The MOEs are then computed by Subroutines MSE and OSMOE.

If the vector method is to be used, Subroutine BKDOWN then breaks the cells out by their vector components (a vector of length three for service component; a vector of length five for commissioning source). The vector estimation method is contained in Subroutine MC87V (listed in paragraph D). Since all of its computations are unique, this subroutine is self-contained with the exception of the transformation formula, which is contained in Function FTTV.

B. MAIN PROGRAM AND AGGREGATION SUBROUTINES

```

C --- PROGRAM TO CONDUCT AGGREGATION AND ESTIMATION METHODS MC800010
C MC800020
C --- PARAMETER MXY MUST BE UPDATED TO REFLECT EXACT NO. YEARS OF DATA MC800030
C --- PARAMETER MXP IS MAX LENGTH OF 3RD DIMENSION P-VECTOR MC800040
C --- PARAMETER MXK IS MAX NUMBER OF AGGREGATED CELLS (MAX NO) MC800050
C PARAMETER (MXX=600, MXY=10, MXP=6, MXK=50) MC800060
C PARAMETER (NMS=81, NG=14, NLG=6, NMG=4, NYB=4, NYE=18, NYEG=4) MC800070
C MC800080
C
C INTEGER ST1,ST2,LYR MC800090
C INTEGER SYCS(31), NYCS MC800100
C INTEGER SYCSG(31),SYCSL(31),SYCSM(31),NYCSG,NYCSL,NYCSM MC800110
C INTEGER SMOS(30), NMOS MC800120
C INTEGER SVCMP(5), NSC MC800130
C INTEGER SCSR(16),NCSR MC800140
C INTEGER SGRD MC800150
C INTEGER*2 MOSGR(2,NMS), YCSB(NYE,NYB,NYEG), VYC(NYE) MC800160
C INTEGER*2 LGRP(NG), MGRP(NLG) MC800170
C REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY) MC800180
C INTEGER DATA(MXY) MC800190
C --- ARRAYS FOR MC87BZ MC800200
C REAL XTB(MXX),VXTB(MXX),XEB(MXX),A(MXX) MC800210
C --- ARRAYS FOR MC87V MC800220
C REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK) MC800230
C REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK) MC800240
C REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP) MC800250
C REAL XBBJ(MXP), EVAL(MXP) MC800260
C MC800270
C
C INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX), RETTBL(MXX,3) MC800280
C INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3) MC800290
C REAL AVINV(MXX), RETINV(MXX) MC800300
C DATA MKG/MXX*0/ MC800310
C --- ASSIGN MOS TO SMALL, LARGE AND MAJOR MOS GROUP MC800320
C DATA MOSGR/013,1, 020,2, 027,2, 038,2, 039,2,
C * 005,3, 007,3, 049,3, 052,3, MC800340
C * 074,4, 079,4, 085,4, 101,4, MC800350
C * 016,5, 060,5, 064,5, 076,5, 111,5, 116,5, MC800360
C * 132,6, 134,6, 135,6, 139,6, MC800370
C * 143,7, 147,7, 150,7, 153,7, 154,7, 155,7, 170,7, MC800380
C * 149,8, 151,8, MC800390
C * 160,9, 161,9, 164,9, 166,9, 167,9, 168,9, 178,9, MC800400
C * 173,10, 174,10, 175,10, 176,10, 177,10, 179,10, 144,10, MC800410
C * 145,10, 165,10, MC800420
C * 001,11, 006,11, 012,11, 015,11, 019,11, 026,11, 037,11, MC800430
C * 048,11, 051,11, 059,11, 070,11, 075,11, 078,11, 084,11, MC800440
C * 087,11, 100,11, 110,11, 115,11, 131,11, 138,11, 217,11, MC800450
C * 172,12, 187,12, 188,12, 189,12, MC800460
C * 142,13, 146,13, 148,13, 152,13, 156,13, 163,13, 169,13, MC800470
C * 088,14 /
C DATA LGRP/1,1,4*2,3,3,4,4,5,5,5,6/ MC800490
C DATA MGRP/1,1,2,2,3,4/ MC800500
C --- CREATE YCS EXPANSION BOUNDS MC800510
C DATA YCSB/1,2,3,4,5,6, 8,9,10,11,12,13,14,15,16,17,18,19, MC800520
C * 7,17*0, 20,21,22,23,24,25,12*0, 26,17*0, MC800530
C * 1,2,3,4,5, 8,9,10,11,12,13,14,15,16,17,18,19,1*0, MC800540

```

```

*      6,7,16*0,   20,21,22,23,24,25,12*0,   26,17*0,          MC800
*      1,2,3,4,5,6,   8,9,10,11,12,13,14,15,16,17,18,19,          MC800
*      7,17*0,   20,21,22,23,24,25,12*0,   26,17*0,          MC800
*      1,2,3,   6,7,8,9,10,11,12,13,14,15,16,17,18,19,1*0,          MC800
*      4,5,16*0,   20,21,22,23,24,25,12*0,   26,17*0   /
C --- INITIALIZE INVENTORY AND ATTRITION ARRAYS
DO 1 I=1,MXX
  DO 2 J=1,MXY
    SINV(I,J)=0
    SY(I,J)=0
    INV(I,J)=0
    Y(I,J)=0
 2 CONTINUE
1 CONTINUE
C --- DEFINE FILE FOR OUTPUT
CALL EXCMS('FILEDEF 11 DISK MC87 OUTPUT A')
C --- FIRST/LAST YEAR OF DATA ON TAPE. UPDATE WHEN NECESSARY
ST1=77
NYR=MXY
LYR=ST1+NYR-1
C --- INITIAL VALUE FOR AGGREGATION ESTIMATION PERCENTAGE
AGGPCT=0.9
ICYCLE=1
C --- GET INPUT PARAMETERS
CALL GETPAR(AIMIN,NO,NMOS,SMOS,NYCS,SYCS,SGRD,
*           NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG)
C --- MAJOR GROUP IS MG, LARGE GROUP LG, GROUP IGR, YCS BLOCK IY
LG=LGRP(IGR)
MG=MGRP(LG)
      WRITE(6,*) ' '
      WRITE(6,*) '---- GR,LG,MG=',IGR,LG,MG
      WRITE(6,*) ' '
C --- READ EVALUATION TABLE. SELECT ONLY RECS PASSING SELECTION CRITERIA
CALL READET(RETtbl,RETINV,MXX,NRET, SGRD, NSC,SVCMP, NCSR,SCSRC,
*           MG,LGRP,MGRP, MOSGR,NMS)
5  RC=0
  IGX=IGR
  LGX=0
  MGX=0
  NYCSG=1
  SYCSG(1)=SYCS(1)
  NYCSL=1
  SYCSL(1)=SYCS(1)
  NYCSM=1
  SYCSM(1)=SYCS(1)
  NCTOT=0
  NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETtbl,RETINV,NRET,MXX,
*           LGRP,MGRP,NMS,AGGPCT,IGR,LG)
C --- DO WHILE NCTOT<NO & RC=0 (EXPAND AS LONG AS NO NOT MET)
10 IF(NC .GE. NO) THEN
    WRITE(6,*) '$GG EVAL NC,SYCSG=',NC,(SYCSG(II),II=1,NYCSG)
    GO TO 60
  ENDIF
  IF(NYCSG.EQ.1) THEN
    CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)
    WRITE(6,*) '== VYC=',(VYC(I),I=1,NYE)

```

```

ENDIF MC801110
CALL EXPAND(NYCSG,SYCSG,VYC,NYE,IGX,LGX,MGX,LG,MG,RC) MC801120
IF(IGX .EQ. 0) GO TO 20 MC801130
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETTBL,RETINV,NRET,MXX, MC801140
* LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC801150
GO TO 10 MC801160
20 NCTOT=NC MC801170
WRITE(6,*) '$$G EVAL NC,SYCSG=' ,NCTOT,(SYCSG(II),II=1,NYCSG) MC801180
C MC801190
C --- EXPAND TO LARGE MOS GROUP MC801200
WRITE(6,*) '' MC801210
WRITE(6,*) '== EXPANDING BY LARGE GROUP: ',LGX MC801220
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX, MC801230
* LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC801240
30 IF((NCTOT+NC) .GE. NO) THEN MC801250
    WRITE(6,*) '$LL EVAL NC,SYCSL=' ,(NCTOT+NC),(SYCSL(II),II=1,NYCSL) MC801260
    GO TO 60 MC801270
ENDIF MC801280
IF(NYCSL.EQ.1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC) MC801290
CALL EXPAND(NYCSL,SYCSL,VYC,NYE,IGX,LGX,MGX,LG,MG,RC) MC801300
IF(LGX .EQ. 0) GO TO 40 MC801310
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX, MC801320
* LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC801330
GO TO 30 MC801340
40 NCTOT=NCTOT+NC MC801350
WRITE(6,*) '$$L EVAL NC,SYCSL=' ,NCTOT,(SYCSL(II),II=1,NYCSL) MC801360
C MC801370
C --- EXPAND TO MAJOR MOS GROUP MC801380
WRITE(6,*) '' MC801390
WRITE(6,*) '== EXPANDING BY MAJOR GROUP: ',MGX MC801400
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX, MC801410
* LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC801420
50 IF((NCTOT+NC) .GE. NO .OR. RC .NE. 0) THEN MC801430
    WRITE(6,*) '$MM EVAL NC,SYCSM=' ,(NC+NCTOT),(SYCSM(II),II=1,NYCSM) MC801440
    GO TO 60 MC801450
ENDIF MC801460
IF(NYCSM.EQ.1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC) MC801470
CALL EXPAND(NYCSM,SYCSM,VYC,NYE,IGX,LGX,MGX,LG,MG,RC) MC801480
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX, MC801490
* LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC801500
GO TO 50 MC801510
C MC801520
C --- EXPANSION FINISHED MC801530
60 IF(RC .NE. 0) THEN MC801540
    WRITE(5,*) '*** REQUIRED NO MAY NOT BE MET: NO,NC=' ,NO,(NC+NCTOT) MC801550
ENDIF MC801560
C --- ALLOW USER TO CHANGE EXPANSION LEVEL MC801570
WRITE(5,*) 'ESTIMATED NUMBER OF CELLS =' ,NC+NCTOT MC801580
70 WRITE(5,*) MC801590
WRITE(5,*) 'ENTER 1 TO CALL READER, 0 TO CHANGE EXPANSION' MC801600
READ(5,*) NPICK1 MC801610
IF(NPICK1 .EQ. 1) THEN MC801620
    GO TO 80 MC801630
ELSE MC801640
    WRITE(5,*) 'AGGPCT IS CURRENTLY =' , AGGPCT MC801650
    WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT' MC801660

```

```

      READ(5,*) AGGPCT
      GO TO 5
    ENDIF
  80  WRITE(5,*) 'CALLING READER'
C
C --- USER ELECTS TO READ THE DATA BASE - DETERMINE MOS EXPANSION LEVEL
    CALL GETMOS(SMOS,NMOS,MGX,MG,IGR,MOSGR,LGRP,MGRP,
    * NMS,NG,NLG)
C --- READ THE DATA BASE AND CREATE THE CELLS
    CALL READER(DATA,INV,Y,MXX,NMOS,NYCSG,NYCSL,NYCSM,NSC,NCSR,NYR,
    * SMOS,SYCSG,SYCSL,SYCSM,SGRD,SVCMP,SCSRC,NRC,PTRTBL,LGX,MGX,IGR,
    * LG,MGRP,LGRP,MOSGR,NMS,NG,NLG,ICYCLE,NPT,PTBL,ISFLAG,SINV,SY)
C --- PERFORM CELL AGGREGATION TO MEET INVENTORY THRESHOLD
    CALL AGGREG( INV,Y,MXX,NYR,SMOS,SYCSG,
    * NRC, NRCOLD,PTRTBL,INDX,AVINV,AIMIN,MKG)
C --- ALLOW USER TO CHANGE EXPANSION LEVEL
    WRITE(5,*) 'NUMBER OF CELLS =',NRC
  90  WRITE(5,*) 
    WRITE(5,*) 'ENTER 1 TO CONTINUE, 0 TO CHANGE EXPANSION'
    READ(5,*) NPICK2
    IF(NPICK2 .EQ. 1) THEN
      GO TO 100
    ELSE
      WRITE(5,*) 'AGGPCT IS CURRENTLY =', AGGPCT
      WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT'
      READ(5,*) AGGPCT
      ICYCLE=ICYCLE+1
      GO TO 5
    ENDIF
C
C --- USER ELECTS TO CONDUCT ESTIMATION
  100 CONTINUE
    WRITE(11,201)'EXPANSION INFORMATION: '
    WRITE(11,203)'ACTUAL NO. OF CELLS USED= ',NRC
    WRITE(11,202)'MOS GROUP #',IGR,' YCS ''S USED=',
    * (SYCSG(I),I=1,NYCSG)
    IF(LGX .GT. 0) THEN
      WRITE(11,204)'LARGE MOS GROUP #',LG,' YCS ''S USED=',
      * (SYCSL(I),I=1,NYCSL)
    ELSE IF(MGX .GT. 0) THEN
      WRITE(11,204)'LARGE MOS GROUP #',LG,' YCS ''S USED=',
      * (SYCSL(I),I=1,NYCSL)
      WRITE(11,204)'MAJOR MOS GROUP #',MG,' YCS ''S USED=',
      * (SYCSM(I),I=1,NYCSM)
    ENDIF
C --- PERFORM ALL BUT VECTOR ESTIMATION METHODS IN MC87BZ
    CALL MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)
C --- VECTOR METHOD--BREAK CELLS INTO VECTOR, CONDUCT ESTIMATION
    IF(ISFLAG .GT. 0) THEN
      CALL BKDOWN(PTBL,NPT,PTRTBL,NRCOLD,INDX,MKG,MXX,MXY,
      * SINV,SY,INV,Y,BKTBL,NBK)
      CALL MC87V( INV,Y,MXX,NYR,NRC,XTBJI,DELTA,X,XVYR,VYRINV,VYRY,
      * BSTAR,S,GAMMA,XBBJ,EVAL,MXP,MXK,BKTBL,NBK,NSC,NCSR,ISFLAG)
    ENDIF
C
  201 FORMAT(/1X,A)

```

```

202 FORMAT(1X,A,I2,A/1X,18(I3)) MC802230
203 FORMAT(1X,A,I2) MC802240
204 FORMAT(1X,A,I1,A/1X,18(I3)) MC802250
END MC802260
C MC802270
*****MC802280
C MC802290
SUBROUTINE EXPAND(NYCSX,SYCSX,VYC,NYE,IGX,LGX,MGX,LG,MG,RC) MC802300
C --- EXPAND YCS IF FEASIBLE, ELSE EXPAND MOS TO LG/MG MC802310
INTEGER SYCSX(31), NYCSX MC802320
INTEGER*2 VYC(NYE) MC802330
C --- FIND POSITION OF ORIGINALLY REQUESTED SYCS(1) MC802340
IY=0 MC802350
DO 10 I=1,NYE MC802360
  IF(SYCSX(1) .EQ. VYC(I)) IY=I MC802370
10 CONTINUE MC802380
IF(IY.EQ.0) GO TO 30 MC802390
C --- FIND NEAREST NON-ZERO YCS TO USE FOR EXPANSION MC802400
DO 20 I=1,NYE MC802410
  J=IY-I MC802420
  IF(J.GE.1) THEN MC802430
    IF(VYC(J).GT.0) GO TO 50 MC802440
  ENDIF MC802450
  J=IY+I MC802460
  IF(J.LE.NYE) THEN MC802470
    IF(VYC(J).GT.0) GO TO 50 MC802480
  ENDIF MC802490
20 CONTINUE MC802500
30 CONTINUE MC802510
C --- NO MORE YCS EXPANSION POSSIBLE. SEE IF MOS EXP. FEASIBLE MC802520
IF(IGX.GT.0) THEN MC802530
C --- EXPAND FROM GROUPS TO LARGE GROUP LGX MC802540
  IGX=0 MC802550
  LGX=LG MC802560
ELSE IF(LGX.GT.0) THEN MC802570
C --- EXPAND FROM LARGE GROUP LGX TO MAJOR GROUP MGX MC802580
  LGX=0 MC802590
  MGX=MG MC802600
ELSE MC802610
  RC=1 MC802620
ENDIF MC802630
RETURN MC802640
C MC802650
C --- EXPAND WITH YCS IN POSITION J & CLEAR VYC(J) MC802660
50 CONTINUE MC802670
  NYCSX=NYCSX+1 MC802680
  SYCSX(NYCSX)=VYC(J) MC802690
  VYC(J)=0 MC802700
END MC802710
C MC802720
*****MC802730
C MC802740
FUNCTION NCEVAL(AIMIN,IGX,LGX,MGX,NYCSX,SYCSX,RETTBL,RETINV, MC802750
*      NRET,MXX,LGRP,MGRP,NMS,AGGPCT,IGR,LG) MC802760
C --- COMPUTE ESTIMATED NO. CELLS TO BE OBTAINED WITH CURRENT EXPANSION MC802770
  INTEGER SYCSX(31),NYCSX MC802780

```

```

INTEGER*2 LGRP(14),MGRP(6) MC8021
INTEGER*2 RETTBL(MXX, 3) MC8022
REAL RETINV(MXX) MC8023
NCEVAL=0 MC8024
IF(IGX.EQ.0 .AND. LGX.EQ.0 .AND. MGX.EQ.0) RETURN MC8025
TAINV=0.0 MC8026
DO 100 I=1,NRET MC8027
C --- SCREEN ON YCS MC8028
    DO 10 J=1,NYCSX MC8029
        IF(RETTBL(I,2) .EQ. SYCSX(J)) GO TO 15 MC802A
10 CONTINUE MC802B
    GO TO 100 MC802C
C --- SCREEN ON MOS BY GROUP, L.GRP OR MG DEPENDING ON IGX,LGX,MGX MC802D
15 CONTINUE MC802E
    MOS=RETTBL(I,1) MC802F
    IGP=RETTBL(I,3) MC802G
    LGP=LGRP(IGP) MC802H
    IF(MGX .GT. 0) THEN MC802I
        IF(MGRP(LGP) .EQ. MGX) THEN MC802J
            IF(LGP .NE. LG) GO TO 80 MC802K
        ENDIF MC802L
    ELSE IF(LGX .GT. 0) THEN MC802M
        IF(LGP .EQ. LGX) THEN MC802N
            IF(IGP .NE. IGR) GO TO 80 MC802O
        ENDIF MC802P
    ELSE MC802Q
        IF(IGP .EQ. IGX) GO TO 80 MC802R
    ENDIF MC802S
    GO TO 100 MC802T
80 CONTINUE MC802U
C --- ACCEPTED MC802V
    IF(RETINV(I) .GE. AIMIN) THEN MC802W
        NCEVAL=NCEVAL+1 MC802X
    ELSE MC802Y
        TAINV=TAINV+RETINV(I) MC802Z
    ENDIF MC8031
100 CONTINUE MC8031
C --- FINAL ESTIMATE IS NCEVAL MC8031
    IF(AIMIN.GT.0) NCEVAL=NCEVAL + AGGPCT*TAINV/AIMIN MC8031
END MC8031
C *****SUBROUTINE GETVYC(SYCS, LG, YCSB,NYE,NYB,NYEG, VYC)***** MC8032
C
SUBROUTINE GETVYC(SYCS, LG, YCSB,NYE,NYB,NYEG, VYC) MC8032
    INTEGER*2 YCSB(NYE,NYB,NYEG), VYC(NYE), LGEX(6) MC8032
    INTEGER SYCS MC8032
    DATA LGEX/4,4,1,2,4,3/ MC8032
C --- L INDICATES LAST DIMENSION IN YCS EXPANSION TABLE MC8032
    L=LGEX(LG) MC8032
C --- FIND TO WHICH YCS BLOCK SYCS BELONGS AND MAKE COPY IN VYC MC8032
    DO 10 J=1,NYB MC8032
        DO 20 I=1,NYE MC8033
            IF(SYCS .EQ. YCSB(I,J,L)) THEN MC8033
                DO 30 K=1,NYE MC8033
                    VYC(K)=YCSB(K,J,L) MC8033
30            CONTINUE MC8033

```

```

        RETURN
      ENDIF
20   CONTINUE
10   CONTINUE
      WRITE(6,*)
      **** YCS NOT FOUND IN YCSB TABLE YCS=' ,SYCS
      END
C
***** MC803400
C
C
      SUBROUTINE READET(RETBL,RETINV,MXX,NRET, SGRD, NSC,SVCMP,
      * NCSR,SCSRC, MG,LGRP,MGRP, MOSGR,NMS)
C --- READ TABLE WITH ALL EXISTING COMBINATIONS FOR SELECTION CRITERIA
C --- ACCEPT RECS WITH MATCHING PG, MG, CS, SVC. ACCEPT ALL YCS
      INTEGER SVCMP(5), NSC, SVC
      INTEGER SCSRC(16),NCSR, CS
      INTEGER SGRD, PG
      INTEGER MOS,YCS
      INTEGER*2 MOSGR(2,NMS), MGRP(*),LGRP(*)
      INTEGER*2 RETTBL(MXX, 3)
      REAL RETINV(MXX), AI
      NRET=0
      DO 10 I=1,999999
      READ(10+SGRD,100,END=999) PG,MOS,YCS,SVC,CS, NRECS,AI
      IF(PG .NE. SGRD) GO TO 10
      IGR=IGFIND(MOS, MOSGR,NMS)
      LG=LGRP(IGR)
      IF(MGRP(LG) .NE. MG) GO TO 10
      DO 20 J=1,NSC
          IF(SVC .EQ. SVCMP(J)) GO TO 21
20   CONTINUE
      GO TO 10
21   CONTINUE
      DO 30 J=1,NCSR
          IF(CS .EQ. SCSRC(J)) THEN
              CALL ACCEPT(MOS,YCS,IGR,RETBL,MXX,NRET,RETINV,AI)
              GO TO 10
          ENDIF
30   CONTINUE
C
10   CONTINUE
999  CONTINUE
      IF(NRET .GT. MXX) THEN
          WRITE(6,*)
          **** ERROR - TOO MANY RECORDS IN RETTBL'
          STOP
      ENDIF
100  FORMAT(I2,I4,I3,I2,I3,I4,F7.2)
      END
C
***** MC803830
C
C
      SUBROUTINE ACCEPT(MOS,YCS,IGR, RETTBL,MXX,NRET,RETINV,AI)
C --- ACCEPT ENTRY. ACCUMULATE IF ALREADY SAME COMBINATION IS PRESENT
      INTEGER MOS,YCS
      INTEGER*2 RETTBL(MXX, 3)
      REAL RETINV(MXX), AI
      DO 10 I=1,NRET

```

```

        IF(MOS.EQ.RETTBL(I,1) .AND. YCS.EQ.RETTBL(I,2) ) THEN      MC8039
            RETINV(I)=RETINV(I) + AI
            RETURN
        ENDIF
10    CONTINUE
C --- NEW COMBINATION                                     MC8039
NRET=NRET+1                                              MC8039
RETTBL(NRET,1)=MOS                                      MC8039
RETTBL(NRET,2)=YCS                                      MC8039
RETTBL(NRET,3)=IGR                                      MC8040
RETINV(NRET)=AI                                         MC8040
END                                                       MC8040
C                                                       MC8040
*****                                                       MC8040
C                                                       MC8040
        SUBROUTINE GETPAR(AIMIN,NO,NMOS,SMOS,SYCS,SGRD,          MC8040
*                           NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG) MC8040
C --- GET SELECTION CRITERIA FROM USER AND VALIDATE      MC8040
        INTEGER SYCS(31), NYCS                                MC8040
        INTEGER SMOS(20), NMOS                               MC8041
        INTEGER SVCMP(5), NSC                                MC8041
        INTEGER SCSR(16),NCSR                             MC8041
        INTEGER SGRD                                    MC8041
        INTEGER*2 MOSGR(2,NMS)                            MC8041
        WRITE(5,*) ' ENTER THRESHOLD MIN. FOR AVERAGE INVENTORY' MC8041
        READ(5,*) AIMIN                                 MC8041
        WRITE(5,*) ' ENTER THRESHOLD MIN. FOR NUMBER OF CELLS' MC8041
        READ(5,*) NO                                    MC8041
        WRITE(5,*) ' THRESHOLDS TO USE AIMIN, NO=' ,AIMIN,NO MC8041
C                                                       MC8042
        WRITE(5,*) ' ENTER MOS (ONLY 1 ACCEPTED)'          MC8042
        NMOS=1                                         MC8042
        READ(5,*) SMOS(1)                                MC8042
        WRITE(6,*) ' MOS SELECTED: ', SMOS(1)           MC8042
        IGR=IGFIND(SMOS(1), MOSGR,NMS)                  MC8042
        WRITE(6,*) ' GROUP TO USE: ', IGR              MC8042
        IF(IGR.EQ.0) THEN
            WRITE(5,*) '***** ERROR - INVALID MOS SELECTED: ',SMOS(1) MC8042
            STOP                                         MC8042
        ENDIF                                         MC8043
C                                                       MC8043
        WRITE(5,*) ' ENTER YCS (ONLY 1 ACCEPTED)'          MC8043
        NYCS=1                                         MC8043
        READ(5,*) SYCS(1)                                MC8043
        WRITE(6,*) ' YCS SELECTED: ', SYCS(1)           MC8043
C                                                       MC8043
        WRITE(5,*) ' ENTER GRADE'                         MC8043
        READ(5,*) SGRD                                  MC8043
        WRITE(6,*) ' GRADE SELECTED', SGRD             MC8043
C                                                       MC8044
        WRITE(5,*) ' ENTER NO. OF SVC. COMPS & ARRAY (1-3, 4=1+2, 5=ALL)' MC8044
        READ(5,*) NSC, (SVCMP(I), I=1,NSC)             MC8044
C --- EXPAND 4 TO 1,2 AND 5 TO 1,2,3                  MC8044
        DO 10 I=1,NSC
        IF(SVCMP(I).EQ.4 .OR. SVCMP(I).EQ.5) THEN      MC8044
            NSC=SVCMP(I)-2                          MC8044

```

```

      DO 15 J=1,NSC          MC804470
      SVCMP(J)=J             MC804480
15    CONTINUE              MC804490
      GO TO 11               MC804500
      ENDIF                 MC804510
10    CONTINUE              MC804520
11    CONTINUE              MC804530
      WRITE(6,*) ' SERVICE COMPONENTS SELECTED', (SVCMP(I), I=1,NSC) MC804540
C
      WRITE(5,*) ' ENTER NO. COMM. SOURCES AND ARRAY (1-15, 16=ALL)' MC804550
      READ(5,*) NCSR, (SCSRC(I), I=1,NCSR)                         MC804560
C --- IF 16 IS SELECTED THEN EXPAND ARRAY TO COVER ALL 1-15      MC804570
      DO 20 I=1,NCSR          MC804580
      IF(SCSRC(I) .EQ. 16) THEN                                     MC804590
      NCSR=15              MC804600
      DO 25 J=1,NCSR          MC804610
      SCSRC(J)=J             MC804620
25    CONTINUE              MC804630
      GO TO 26               MC804640
      ENDIF                 MC804650
20    CONTINUE              MC804660
26    CONTINUE              MC804670
      WRITE(5,*) ' COMM. SOURCES SELECTED:', (SCSRC(I), I=1,NCSR) MC804680
C
C --- FLAG TO DETERMINE WHICH OF SVC OR CS WILL BE USED AS 3RD DIMENSIONMC804710
      WRITE(5,*) 'SELECT 3RD DIM. TO USE: 0=NONE, 1=SVC, 2=COMM. SOURCE' MC804720
      READ(5,*) ISFLAG          MC804730
C --- WRITE INPUT PARAMETER INFO TO OUTPUT FILE                  MC804740
      WRITE(11,101) 'TEST CASE INPUT PARAMETERS:'                   MC804750
      WRITE(11,102) 'INVENTORY THRESHOLD= ',AIMIN,                MC804760
      *                  'THRESHOLD NO. OF CELLS= ',NO            MC804770
      WRITE(11,103) 'MOS= ',SMOS(1), 'YCS= ',SYCS(1), 'GRADE= ',SGRD MC804780
      WRITE(11,104) 'SERVICE COMPONENTS= ',(SVCMP(I),I=1,NSC)     MC804790
      WRITE(11,104) 'COMM SOURCES= ',(SCSRC(I),I=1,NCSR)         MC804800
      WRITE(6,*) '3RD DIMENSION= ',ISFLAG                         MC804810
C
101   FORMAT(1X,A)           MC804820
102   FORMAT(1X,A,F4.1,7X,A,I2)        MC804830
103   FORMAT(1X,A,I3,2(5X,A,I2))     MC804840
104   FORMAT(1X,A,15(I3))           MC804850
      END                         MC804860
C
*****SUBROUTINE GETMOS(SMOS,NMOS,MGX,LGX,MG,LG,IGR,MOSGR,LGRP,MGRP,MC804880
*   NMS,NG,NLG)               MC804890
C --- BUILD SMOS ARRAY BASED UPON EXPANSION                  MC804900
      INTEGER SMOS(30)           MC804910
      INTEGER*2 MOSGR(2,NMS), LGRP(NG), MGRP(NLG)      MC804920
      NMOS=0                     MC804930
      IF(MGX .GT. 0) THEN       MC804940
C --- HAVE EXPANDED TO MAJOR MOS GROUP                      MC804950
      DO 10 I=1,NMS           MC804960
      IGP=MOSGR(2,I)           MC804970
      LGP=LGRP(IGP)             MC804980
      IF(MGRP(LGP) .EQ. MG) THEN MC804990
      MC805000
      MC805010
      MC805020

```

```

        NMOS=NMOS+1          MC8050
        SMOS(NMOS)=MOSGR(1,I) MC8050
    ENDIF
10     CONTINUE
    RETURN
    ELSE IF(LGX .GT. 0) THEN MC8050
C --- HAVE EXPANDED TO LARGE MOS GROUP MC8050
    DO 20 I=1,NMS           MC8051
        IGP=MOSGR(2,I)      MC8051
        IF(LGRP(IGP) .EQ. LG) THEN MC8051
            NMOS=NMOS+1       MC8051
            SMOS(NMOS)=MOSGR(1,I) MC8051
        ENDIF
20     CONTINUE
    RETURN
    ELSE MC8051
C --- HAVE EXPANDED TO SMALL MOS GROUP MC8051
    DO 30 I=1,NMS           MC8052
        IF(MOSGR(2,I) .EQ. IGR) THEN MC8052
            NMOS=NMOS+1       MC8052
            SMOS(NMOS)=MOSGR(1,I) MC8052
        ENDIF
30     CONTINUE
    RETURN
ENDIF
END                                     MC8052

C
*****                                         MC8053
C
FUNCTION IGFIND(MOS, MOSGR,NMS)          MC8053
C --- FIND LOCATION OF MATCHING MOS IN GROUP TABLE. RETURN GROUP NO MC8053
INTEGER*2 MOSGR(2,NMS)                  MC8053
DO 10 I=1,NMS                         MC8053
    IF(MOSGR(1,I) .EQ. MOS) THEN        MC8053
        IGFIND=MOSGR(2,I)             MC8053
        RETURN                         MC8053
    ENDIF
10 CONTINUE
IGFIND=0
END                                     MC8054

C
*****                                         MC8054
C
SUBROUTINE READER(DATA,INV,Y,MXX,NMOS,NYCSG,NYCSL,NYCSM,NSC,NCSR, MC80546
* NYR,SMOS,SYCSG,SYCSL,SYCSM,SGRD,SVCMP,SCSRC,NRC,PTRTBL,LGX,MGX, MC80547
* IGR,LG,MGRP,LGRP,MOSGR,NMS,NG,NLG,ICYCLE,NPT,PTBL,ISFLAG,SINV,SY)MC80548
REAL INV(MXX,NYR),Y(MXX,NYR),SINV(MXX,NYR),SY(MXX,NYR)          MC80549
INTEGER*2 PTRTBL(MXX, 2), PTBL(MXX,3)                           MC80550
INTEGER SYCSG(*), SYCSL(*), SYCSM(*)                            MC80551
INTEGER SMOS(*), NMOS                                         MC80552
INTEGER SVCMP(*), NSC                                         MC80553
INTEGER SCSR(*),NCSR                                         MC80554
INTEGER SGRD                                         MC80555
INTEGER TYPE ,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,RACE   MC80556
INTEGER DATA(NYR)                                         MC80557
CHARACTER*7 CITLS                                         MC80558

```

```

C           INTEGER*2 MOSGR(2,NMS),LGRP(NG),MGRP(NLG)          MC805590
C --- REWIND DATA FILE AND RESET INV,Y IF CYCLING THRU READER   MC805600
IF(ICYCLE .GT. 1) THEN                                         MC805610
    REWIND 1
    DO 6 I=1,MXX
        DO 5 J=1,NYR
            INV(I,J)=0.0
            Y(I,J)=0.0
            SINV(I,J)=0.0
            SY(I,J)=0.0
5     CONTINUE
6     CONTINUE
ENDIF
C --- READ RECORD AND STORE IN MATRIX
ICR=0
NRC=0
NPT=0
ICNT=0
IYNO=0
IYR=0
C
1 READ(1,101,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,
*          RACE,CITLS,DATA
    ICR=ICR+1
C --- CHECK IF RECORD MEETS SELECTION CRITERIA. OTHERWISE REJECT. MC805840
C --- COLLECT TYPES 0=INVENTORY, AND 1-5 ALL LOSSES                MC805850
    IF(TYPE.GT.5) GO TO 999
C
C --- SCREEN FOR GRADE                                         MC805870
    IF(PG .NE. SGRD) GO TO 1
C
C --- SCREEN FOR MOS                                          MC805900
    IGP=IGFIND(MOS,MOSGR,NMS)
    IF(IGP.EQ.0) GO TO 1
    LGP=LGRP(IGP)
    IF(MGX .GT. 0) THEN                                         MC805910
C --- HAVE EXPANDED TO MAJOR MOS GROUP                         MC805920
        IF(LGP .EQ. LG) THEN                                     MC805930
            DO 10 I=1,NYCSL
                IF(YCS .EQ. SYCSL(I)) THEN                      MC805940
                    IY=I
                    GO TO 60
                ENDIF
10    CONTINUE
                GO TO 1
        ELSE IF(MGRP(LGP) .EQ. MGX) THEN                         MC805950
            DO 20 I=1,NYCSM
                IF(YCS .EQ. SYCSM(I)) THEN                      MC805960
                    IY=I
                    GO TO 60
                ENDIF
20    CONTINUE
                GO TO 1
        ELSE
            GO TO 1
    ENDIF

```

```

        ENDIF MC8061
        ELSE IF(LGX .GT. 0) THEN MC8061
C --- HAVE EXPANDED TO LARGE MOS GROUP MC8061
        IF(IGP .EQ. IGR) THEN MC8061
          DO 30 I=1,NYCSG MC8061
            IF(YCS .EQ. SYCSG(I)) THEN MC8062
              IY=I MC8062
              GO TO 60 MC8062
            ENDIF MC8062
30      CONTINUE MC8062
      GO TO 1 MC8062
      ELSE IF(LGP .EQ. LGX) THEN MC8062
        DO 40 I=1,NYCSL MC8062
          IF(YCS .EQ. SYCSL(I)) THEN MC8062
            IY=I MC8062
            GO TO 60 MC8063
          ENDIF MC8063
40      CONTINUE MC8063
      GO TO 1 MC8063
      ELSE MC8063
        GO TO 1 MC8063
      ENDIF MC8063
    ELSE MC8063
C --- HAVE EXPANDED TO SMALL MOS GROUP MC8063
        IF(IGP .EQ. IGR) THEN MC8063
          DO 50 I=1,NYCSG MC8064
            IF(YCS .EQ. SYCSG(I)) THEN MC8064
              IY=I MC8064
              GO TO 60 MC8064
            ENDIF MC8064
50      CONTINUE MC8064
      GO TO 1 MC8064
      ELSE MC8064
        GO TO 1 MC8064
      ENDIF MC8064
    ENDIF MC8065
60      CONTINUE MC8065
C
      DO 70 I=1,NMOS MC8065
        IF(MOS .EQ. SMOS(I)) THEN MC8065
          IM=I MC8065
          GO TO 80 MC8065
        ENDIF MC8065
70      CONTINUE MC8065
      WRITE(6,*) '**** ERROR IN MOS SCREENING ****',MOS MC8065
      WRITE(6,*) 'NMOS,SMOS=' ,NMOS,(SMOS(I),I=1,NMOS) MC8066
      GO TO 1 MC8066
C
C --- SCREEN FOR SERVICE COMPONENT MC8066
80      CONTINUE MC8066
      DO 90 I=1,NSC MC8066
        IF(SVC .EQ. SVCMP(I)) THEN MC8066
          IS=I MC8066
          GO TO 100 MC8066
        END IF MC8066
90      CONTINUE MC8067

```

```

      GO TO 1                                MC806710
C
C --- SCREEN FOR COMMISSIONING SOURCE      MC806720
100  CONTINUE                               MC806730
      DO 110 I=1,NCSR                         MC806740
          IF(CS .EQ. SCSRC(I)) THEN           MC806750
              IR=I                            MC806760
              GO TO 120                      MC806770
          END IF                           MC806780
110   CONTINUE                               MC806790
      GO TO 1                                MC806800
C
120   CONTINUE                               MC806820
C
C --- RECORD ACCEPTED - INSTALL IT IN INV,Y,SINV,SY, PTRTBL AND PTBL
ICNT=ICNT+1                                MC806840
IF(ISFLAG.EQ.1) THEN                         MC806850
    IW=IS                                MC806860
ELSE IF(ISFLAG.EQ.2) THEN                   MC806870
    IW=IR                                MC806880
ELSE                                         MC806890
    IW=-99                                MC806900
ENDIF                                         MC806910
MINV=GINV(PTRTBL, MXX,NRC, IM,IY,-99)       MC806920
MV=GINV(PTBL, MXX,NPT,IM,IY,IW)             MC806930
IF(TYPE.EQ.0) THEN                          MC806940
    CALL INSINV(PTRTBL,MXX,NYR,NRC,MINV,IM,IY,-99,INV,DATA) MC806950
    CALL INSINV(PTBL, MXX,NYR,NPT,MV, IM,IY, IW,SINV,DATA) MC806960
ELSE                                         MC806970
    CALL INSY(MXX,NYR,MINV,Y,DATA)          MC807000
    CALL INSY(MXX,NYR,MV, SY,DATA)          MC807010
    IYR=IYR+1                            MC807020
    IF(MINV.EQ.0) THEN                     MC807030
        WRITE(6,*) '*** ERROR IN DATA BASE. LOSS W/O INV. REG.' MC807040
        WRITE(6,122) 'Y**:', MOS,YCS,PG,EDLV,SVC,RACE,          MC807050
*                                         (DATA(IT), IT=1,NYR) MC807060
        IYNO=IYNO+1                        MC807070
    ENDIF                                 MC807080
ENDIF                                         MC807090
C
GO TO 1                                    MC807100
C
999  CONTINUE                               MC807110
WRITE(6,*)                                     MC807120
WRITE(6,*) 'TOTAL RECORDS READ                =', ICR     MC807130
WRITE(6,*) 'TOTAL INV. MOS/YCS    COMBINATIONS=' ,NRC    MC807140
WRITE(6,*) 'TOTAL INV. MOS/YCS/IW COMBINATIONS=' ,NPT    MC807150
WRITE(6,*) 'TOTAL RECORDS ACCEPTED            =', ICNT    MC807160
WRITE(6,*) 'TOTAL LOSS RECORDS ACCEPTED        =', IYR     MC807170
WRITE(6,*) 'TOTAL LOSS RECORDS NOT MATCHED     =', IYNO    MC807180
C --- TERMINATE IF NO DATA COLLECTED        MC807190
IF(NRC .EQ. 0) THEN                         MC807200
    WRITE(6,*) '***** NO DATA MEETS SELECTION REQS' MC807210
    STOP                                     MC807220
ENDIF                                         MC807230
C

```

```

101 FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4) MC807:
121 FORMAT(A8,13I6) MC807:
122 FORMAT(A8,7I6, 5X, 12I6) MC807:
131 FORMAT(I4, 2I6) MC807:
132 FORMAT(I4, 3I6, 10F7.2) MC807:
END MC807:
C MC807:
***** MC807:
C MC807:
C FUNCTION GINV(PTBL, MXX,NPT, IM,IY,IW) MC807:
C --- FIND LOCATION OF INVENTORY ENTRY FOR MOS,YCS,SVC/GS COMBINATIONS MC807:
C --- 3RD DIMENSION CHECKED ONLY IN CASE IW>0 MC807:
INTEGER*2 PTBL(MXX, *) MC807:
DO 10 I=1,NPT MC807:
    IF(PTBL(I, 1) .EQ. IM .AND. MC807:
* PTBL(I, 2) .EQ. IY ) THEN MC807:
        IF(IW.LT.0 .OR. (IW.GT.0 .AND. PTBL(I, 3).EQ.IW)) THEN MC807:
            GINV=I MC807:
            RETURN MC807:
        ENDIF MC807:
    ENDIF MC807:
10 CONTINUE MC807:
GINV=0 MC807:
END MC807:
C MC807:
***** MC807:
C MC807:
C SUBROUTINE INSINV(PT,MXX,NYR,N,K,IM,IY,IW,INV,DATA) MC807:
C --- ACCUMM INTO KTH ENTRY. INSTALL IN POINTER TABLE IF NOT PRESENT MC807:
REAL INV(MXX, NYR) MC807:
INTEGER*2 PT(MXX, *) MC807:
INTEGER DATA(NYR) MC807:
IF(K .EQ. 0) THEN MC807:
C --- ADD NEW ENTRY MC807:
N=N+1 MC807:
IF(N .GT. MXX) THEN MC807:
    WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',N MC807:
    STOP MC807:
ENDIF MC807:
K=N MC807:
PT(K, 1)=IM MC807:
PT(K, 2)=IY MC807:
IF(IW.GT.0) PT(K, 3)=IW MC807:
ENDIF MC807:
DO 130 IT=1,NYR MC807:
    INV(K,IT)=INV(K,IT) + .25*FLOAT(DATA(IT)) MC807:
130 CONTINUE MC807:
END MC807:
C MC807:
***** MC807:
C MC807:
C SUBROUTINE INSY(MXX,NYR,K,Y,DATA) MC807:
C --- ACCUMM INTO KTH ENTRY FOR LOSS MC807:
REAL Y(MXX, NYR) MC807:
INTEGER DATA(NYR) MC807:
IF(K .EQ. 0) RETURN MC807:

```

```

      DO 10 IT=1,NYR          MC807830
      Y(K,IT)=Y(K,IT) + DATA(IT)
10   CONTINUE
      END
C                                         MC807870
*****                                         MC807880
C                                         MC807890
      SUBROUTINE AGGREG( INV,Y,MXX,NYR,SMOS,SYCSG,
*                           NRC,NRCOLD,PTRTBL,INDX,AVINV, AIMIN,MKG) MC807900
C --- COMP. AVERAGE INV. & SORT          MC807920
      REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)          MC807930
      INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX)          MC807940
      INTEGER SYCSG(*), SMOS(*)          MC807950
      REAL*8 TINV, TY          MC807960
C                                         MC807970
C --- RESET MKG (NECESSARY WHEN CYCLING THRU AGGPCT VALUES) MC807980
      DO 10 I=1,MXX          MC807990
      MKG(I)=0          MC808000
10   CONTINUE          MC808010
      TINV=0          MC808020
      TY=0          MC808030
      DO 100 I=1,NRC          MC808040
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES & COMP. AVG INV. MC808050
      AI=0          MC808060
      DO 201 J=1,NYR          MC808070
      TINV=TINV+INV(I,J)          MC808080
      TY=  TY+  Y(I,J)          MC808090
      IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J)          MC808100
      AI=AI+INV(I,J)          MC808110
201   CONTINUE          MC808120
      AVINV(I)=AI/NYR          MC808130
      INDX(I)=I          MC808140
100  CONTINUE          MC808150
      WRITE(6,*) '===== TOTAL INV,Y=' ,TINV,TY          MC808160
C                                         MC808170
C --- SORT ASCENDING BY AVG INVENTORY          MC808180
      CALL SORT2(AVINV,INDX,NRC)          MC808190
C                                         MC808200
      NS1=0          MC808210
C --- DISPLAY TABLE IN SORT SEQUENCE          MC808220
      CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,
*                           SYCSG,SMOS )          MC808230
      MC808240
C                                         MC808250
      DO 200 K=NRC,1,-1          MC808260
      IF(AVINV(K) .GE. AIMIN) THEN          MC808270
C ---           MARK AS MEMBER OF SET S0          MC808280
      MKG(K)=32767          MC808290
      ELSE          MC808300
C ---           INITIAL COUNT OF MEMBERS OF SET S1          MC808310
      NS1=K          MC808320
      GO TO 202          MC808330
      ENDIF          MC808340
200  CONTINUE          MC808350
202  CONTINUE          MC808360
C --- DO AGGREGATIONS WITHIN SET S1 UNTIL NO MORE POSSIBLE (KF GE 0) MC808370

```

```

        KF=-1          MC8081
C --- DO WHILE KF<0          MC8081
  300 IF(KF.GE.0) GO TO 310    MC8084
      CALL AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)
      GO TO 300               MC8084
  310 CONTINUE                MC8084
C --- DISPLAY TABLE AFTER 1ST AGGREGATION   MC8084
      CALL DSPTBL( INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,
*           SYCSG,SMOS )          MC8084
      IF(NS1.EQ.NRC) THEN       MC8084
          WRITE(6,*) '***** SET S0 EMPTY. NO CELLS ABOVE THRESHOLD'
          STOP                   MC8084
      ENDIF                     MC8085
C --- DO AGGREGATIONS FROM SET S1 INTO SET S0 UNTIL NO MORE POSSIBLE
      KF=1                      MC8085
C --- DO WHILE KF>0          MC8085
  320 IF(KF.LE.0) GO TO 330    MC8085
      CALL AGG2(AVINV,INDX,MKG,NS1,NRC,INV,Y,MXX,NYR, KF)
      GO TO 320               MC8085
  330 CONTINUE                MC8085
C --- DISPLAY TABLE AFTER 2ND AGGREGATION   MC8085
      CALL DSPTBL( INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,
*           SYCSG,SMOS )          MC8085
C --- MOVE VALUES GE AIMIN TO BEGINNING OF ARRAYS   MC8086
      CALL CMPRS(INV,Y,MXX,NYR,NRC,NRCOLD,AIMIN,AVINV)  MC8086
C --- DISPLAY TABLE AFTER MOVING VALUES.          MC8086
      DO 400 K=1,NRC            MC8086
          WRITE(6,122)K,AVINV(K), (INV(K,J),J=1,NYR)    MC8086
          WRITE(6,123)           ( Y(K,J),J=1,NYR)    MC8086
  400 CONTINUE                MC8086
  122 FORMAT(/I5,14X,F8.3, 6X,      10F7.2)          MC8086
  123 FORMAT(     33X, 10F7.2)          MC8086
      END                      MC8087
C ***** SUBROUTINE AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)  MC8087
C --- DO ONE PASS OF AGGREGATION          MC8087
      REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)      MC8087
      INTEGER*2 INDX(MXX), MKG(MXX)                  MC8087
      KF=0                      MC8087
      CI=0                      MC8087
      DO 10 I=NS1,1,-1          MC8087
          IF(MKG(I).EQ.0) THEN          MC8087
              IF(KF.EQ.0) THEN          MC8088
                  THIS WILL BE THE COLLECTING CELL  MC8088
                  KF=I                  MC8088
                  CI=AVINV(I)          MC8088
              ELSE                      MC8088
                  IF(CI+AVINV(I).LT.AIMIN) THEN  MC8088
                      ACCUM. WITH CELL KF TEMPORARILY. SET TEMP. POINTER -KF  MC8088
                      CI=CI+AVINV(I)          MC8088
                      MKG(I)=-KF            MC8088
                  ELSE                      MC8088
                      FIND SMALLEST CELL TO ADD  MC8089
                      CALL AGG1A(AVINV,MKG,I,CI,AIMIN,KF,MXX)  MC8089
                  ENDIF                     MC8089
  10 CONTINUE

```

```

      IF(CI.GE.AIMIN) THEN MC808930
C ---      MAKE THIS AGGREGATION PERMANENT AND EXIT MC808940
      AVINV(KF)=CI MC808950
      CALL AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX) MC808960
      NS1=NS1-1 MC808970
      MKG(KF)=32767 MC808980
      KF=-1 MC808990
      RETURN MC809000
      ENDIF MC809010
      ENDIF MC809020
      ENDIF MC809030
10 CONTINUE MC809040
C MC809050
      IF(KF.EQ.0) RETURN MC809060
C --- CLEAR TEMPORARY POINTERS LEFT. THIS WAS AN UNSUCCESSFUL AGGREG. MC809070
      DO 20 I=1,NS1 MC809080
         IF(MKG(I).LT.0) MKG(I)=0 MC809090
20 CONTINUE MC809100
      END MC809110
C *****
      SUBROUTINE AGG1A(AVINV,MKG,ILAST,CI,AIMIN,KF,MXX) MC809120
C --- FIND SMALLEST CELL TO ADD AND SET TEMPORARY POINTER MC809130
      REAL AVINV(MXX) MC809140
      INTEGER*2 MKG(MXX) MC809150
      DO 10 I=1,ILAST MC809160
         IF(MKG(I).EQ.0) THEN MC809170
            IF(CI+AVINV(I).GE.AIMIN) THEN MC809180
               CI=CI+AVINV(I) MC809190
               MKG(I)=-KF MC809200
               RETURN MC809210
            ENDIF MC809220
         ENDIF MC809230
10 CONTINUE MC809240
      WRITE(6,*) '*** ERROR IN AGG1A. NO VALUE FOUND ***' MC809250
      STOP MC809260
      END MC809270
C *****
      SUBROUTINE AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX) MC809280
C --- MAKE AGGREGATION PERMANENT MC809290
      REAL INV(MXX, NYR), Y(MXX, NYR) MC809300
      INTEGER*2 INDX(MXX), MKG(MXX) MC809310
      K=INDX(KF) MC809320
      DO 10 I=1,KF-1 MC809330
         IF(MKG(I).LT.0) THEN MC809340
            IF(MKG(I).NE.-KF) STOP 777 MC809350
            MKG(I)=KF MC809360
            L=INDX(I) MC809370
            DO 20 J=1,NYR MC809380
               INV(K,J)=INV(K,J)+INV(L,J) MC809390
               Y(K,J)= Y(K,J)+ Y(L,J) MC809400
20 CONTINUE MC809410
         ENDIF MC809420
10 CONTINUE MC809430
      END MC809440
C *****

```

```

SUBROUTINE AGG2(AVINV, INDX, MKG, NS1, NRC, INV, Y, MXX, NYR, KF) MC8094
C --- DO ONE PASS OF AGGREGATION FROM SET S1 TO SET S0 MC8094
C --- ON EACH PASS ONE ELEMENT OF S1 IS TAKEN & ADDED TO SMALLEST OF S0 MC8095
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX) MC8095
INTEGER*2 INDX(MXX), MKG(MXX) MC8095
KF=0 MC8095
C --- FIND ELEMENT OF S1 (ONLY THOSE WITH POINTER MKG(I)=0) MC8095
DO 10 I=1,NS1 MC8095
  IF(MKG(I).EQ.0) THEN MC8095
    KF=I MC8095
    GO TO 12 MC8095
  ENDIF MC8095
10 CONTINUE MC8096
12 CONTINUE MC8096
C --- IF KF STILL 0 THEN NO MORE ELEMENTS IN S1 LEFT MC8096
IF(KF.EQ.0) RETURN MC8096
C MC8096
C --- FIND SMALLEST ELEMENT OF S0 AND ADD TO IT. ONLY WITH MKG(I)=32767 MC8096
ISM=NRC MC8096
SMALL=AVINV(ISM) MC8096
DO 20 I=1, NRC MC8096
  IF(MKG(I).EQ.32767) THEN MC8096
    IF(AVINV(I).LT.SMALL) THEN MC8097
      ISM=I MC8097
      SMALL=AVINV(I) MC8097
    ENDIF MC8097
  ENDIF MC8097
20 CONTINUE MC8097
C --- JOIN ELEMENT KF TO ELEMENT ISM MC8097
AVINV(ISM)=AVINV(ISM) + AVINV(KF) MC8097
MKG(KF)=ISM MC8097
L=INDX(KF) MC8097
K=INDX(ISM) MC8098
DO 30 J=1,NYR MC8098
  INV(K,J)=INV(K,J)+INV(L,J) MC8098
  Y(K,J)= Y(K,J)+ Y(L,J) MC8098
30 CONTINUE MC8098
END MC8098
C *****
SUBROUTINE CMPRS(INV, Y, MXX, NYR, NRC, NRCOLD, AIMIN, AVINV) MC8098
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX) MC8098
C --- COMPRESS INV,Y IN PLACE. MOVE ALL ROWS GE AIMIN TO TOP MC8098
NRCOLD=NRC MC80990
NRC=0 MC80991
DO 10 I=1,NRCOLD MC80992
  AI=CAINV(INV, I, MXX, NYR) MC80993
  IF(AI .GE. AIMIN) THEN MC80994
C --- TRANSFER ACTIVE CELL I ---> NRC MC80995
    NRC=NRC+1 MC80996
    AVINV(NRC)=AI MC80997
    DO 20 J=1,NYR MC80998
      INV(NRC,J)=INV(I,J) MC80999
      Y(NRC,J)= Y(I,J) MC81000
20 CONTINUE MC81001
ENDIF MC81002
10 CONTINUE MC81003

```

```

        END MC810040
C ****
      FUNCTION CAINV( INV,I,MXX,NYR) MC810050
      REAL INV(MXX, NYR) MC810060
C --- COMPUTE AVERAGE INVENTORY FOR ROW I MC810070
      CAINV=0 MC810080
      DO 10 J=1,NYR MC810090
         CAINV=CAINV+INV(I,J) MC810100
10    CONTINUE MC810110
      CAINV=CAINV/NYR MC810120
      END MC810130
C ****
      SUBROUTINE DSPTBL( INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR, MC810140
      *          SYCSG,SMOS) MC810150
C --- DISPLAY TABLE IN SORT SEQUENCE MC810160
      REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX) MC810170
      INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX)
      INTEGER SYCSG(*)
      INTEGER SMOS(*)
      INTEGER IATT(2)
      CHARACTER*1 STI
      WRITE(6,121)
      WRITE(6,*) ' INV. THRESHOLD MIN. VALUE=' ,AIMIN MC810180
C
      WRITE(6,*) ' I   INDX     AVG           MKG           INVENTORY/LOSSES' MC810190
      DO 200 K=1,NRC MC810200
         STI=' '
         I=INDX(K)
         AI=AVINV(K)
         IF(AI .LT. AIMIN) STI='$'
         IATT(1)=SMOS(PTRTBL(I,1))
         IATT(2)=SYCSG(PTRTBL(I,2))
         WRITE(6,122)K,I,AI,MKG(K),STI,(INV(I,J),J=1,NYR),(IATT(J),J=1,2),MC810210
         *                  PTRTBL(I,1),PTRTBL(I,2)
         WRITE(6,123)          ( Y(I,J),J=1,NYR) MC810220
200  CONTINUE MC810230
C
      121 FORMAT(///)
      122 FORMAT(/2I5,F8.3,I9,1X,A2, 10F7.2, 5X, 6I5) MC810240
      123 FORMAT( 30X, 10F7.2) MC810250
      END MC810260
C ****
      SUBROUTINE SORT2(Y,INDX, N) MC810270
C --- INPLACE SORT USING SHELL ALGORITHM *****
C --- SORTS ON Y AND DOES SAME REORDERING ON INDEXES INDX MC810280
      REAL Y(N),TEMP MC810290
      INTEGER GAP MC810300
      INTEGER*2 INDX(N), ITEMP MC810310
      LOGICAL EXCH MC810320
C
      GAP=(N/2) MC810330
5     IF (.NOT.(GAP.NE.0)) GO TO 500 MC810340
10    CONTINUE MC810350
         EXCH=. TRUE.
         K=N-GAP MC810360
         DO 200 I=1,K MC810370

```

```

        KK=I+GAP          MC8106
        IF(. NOT. (Y(I). GT. Y(KK))) GO TO 100   MC8106
            TEMP=Y(I)          MC8106
            Y(I)=Y(KK)          MC8106
            Y(KK)=TEMP          MC8106
            ITEMP=INDX(I)       MC8106
            INDX(I)=INDX(KK)    MC8106
            INDX(KK)=ITEMP      MC8106
            EXCH=. FALSE.       MC8106
100     CONTINUE          MC8106
200     CONTINUE          MC8107
        IF (. NOT. (EXCH)) GO TO 10      MC8107
        GAP=(GAP/2)                MC8107
        GO TO 5                  MC8107
500     CONTINUE          MC8107
        RETURN                 MC8107
        END                   MC8107
C                                     MC8107
*****                                     MC8107
C                                     MC8107
        SUBROUTINE BKDOWN(PTBL,NPT,PTRTBL,NRC,INDX,MKG,MXX,MXY,
*           SINV,SY,INV,Y,BKTBL,NBK )          MC8108
C --- BREAKDOWN AGGREGATED VALUES BY THE 3RD DIMENSION SVC/CS   MC8108
        REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)   MC8108
        INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX)             MC8108
        INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)                      MC8108
        REAL*8 TINV,TY                                         MC8108
        NBK=0                                         MC8108
C --- TRAVERSE MKG ARRAY AND BUILD BKTBL                         MC8108
        DO 10 I=1,NRC                                         MC8108
            IF(MKG(I). NE. 32767) THEN                      MC8109
                ICELL=MKG(I)                                MC8109
            ELSE                                           MC8109
                ICELL=I                                    MC8109
            ENDIF                                         MC8109
            IX=INDX(I)                                  MC8109
            IM=PTRTBL( IX,1)                            MC8109
            IY=PTRTBL( IX,2)                            MC8109
            CALL BLDBK(ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)    MC8109
10      CONTINUE          MC8109
C --- DISPLAY BKTBL PRIOR TO SORTING                           MC8110
        WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)        MC8110
        CALL SORT3(BKTBL,NBK,MXX)                          MC8110
        WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)        MC8110
C --- SUMMARIZE SINV,SY INTO INV,Y FOR MATCHING ENTRIES IN BKTBL   MC8110
        CALL SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)        MC8110
        WRITE(6,102) (I,(INV(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)  MC8110
        WRITE(6,102) (I,( Y(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)  MC8110
101    FORMAT(I4, 3I6)          MC81108
102    FORMAT(I4, 10F7.2,10X,2I4)    MC81109
103    FORMAT(/I5,10F7.2)          MC81110
104    FORMAT( 5X,10F7.2)          MC81111
        END                  MC81112
C ****                                     MC81113
        SUBROUTINE BLDBK(ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)    MC81114

```

```

      INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)          MC811150
C --- RECORD ALL ENTRIES IN PTBL WITH MATCHING IM,IY IN BKTBL   MC811160
      DO 10 I=1,NPT                                MC811170
         IF(PTBL(I,1).EQ. IM . AND. PTBL(I,2).EQ. IY) THEN    MC811180
C ---           INSTALL WITH CELL ID, IW & POINTER    MC811190
         NBK=NBK+1                                    MC811200
         BKTBL(NBK,1)=ICELL                         MC811210
         BKTBL(NBK,2)=PTBL(I,3)                      MC811220
         BKTBL(NBK,3)=I                            MC811230
      ENDIF                                         MC811240
10    CONTINUE                                     MC811250
      END                                           MC811260
C *****
      SUBROUTINE SORT3(T,N,MXX)                     MC811280
C --- INPLACE SORT USING SHELL ALGORITHM *****
C --- SORTS ON 1ST 2 COLS. OF T & DOES SAME REORDERING ON 3RD COLUMN MC811290
      INTEGER*2 T(MXX,3), ITEMP                      MC811300
      INTEGER GAP                                     MC811310
      LOGICAL EXCH                                   MC811320
      LOGICAL EXCH                                   MC811330
C
      GAP=(N/2)                                      MC811340
      5    IF (GAP.EQ.0) GO TO 500                  MC811350
10    CONTINUE                                     MC811360
      EXCH=. FALSE.                                MC811370
      K=N-GAP                                     MC811380
      DO 200 I=1,K                                MC811390
      KK=I+GAP                                    MC811400
      IF(T(I,1).GT. T(KK,1) . OR.                 MC811410
      *             (T(I,1).EQ. T(KK,1) . AND. T(I,2).GT. T(KK,2)) ) THEN MC811420
      IT1=T(I,1)                                    MC811430
      IT2=T(I,2)                                    MC811440
      IT3=T(I,3)                                    MC811450
      T(I,1)=T(KK,1)                               MC811460
      T(I,2)=T(KK,2)                               MC811470
      T(I,3)=T(KK,3)                               MC811480
      T(KK,1)=IT1                                  MC811490
      T(KK,2)=IT2                                  MC811500
      T(KK,3)=IT3                                  MC811510
      EXCH=. TRUE.                                MC811520
      ENDIF                                         MC811530
200   CONTINUE                                     MC811540
      IF (EXCH) GO TO 10                           MC811550
      GAP=(GAP/2)                                 MC811560
      GO TO 5                                     MC811570
500   CONTINUE                                     MC811580
      RETURN                                       MC811590
      END                                           MC811600
C *****
      SUBROUTINE SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)    MC811620
C --- CREATE AGGREGATED ARRAYS INV,Y FROM CELL & 3RD DIM. INFO. IN BKTBLMC811640
      REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)  MC811650
      INTEGER*2 BKTBL(MXX,3)                          MC811660
      REAL*8 TINV,TY                                MC811670
      IP=0                                         MC811680
      I1=-1                                       MC811690
      I2=-1                                       MC811700

```

```

TINV=0 MC811
TY=0 MC811
DO 10 I=1,NBK MC811
    IF(BKTBL(I,1).NE.I1 .OR. BKTBL(I,2).NE.I2) THEN MC811
C ---          CHANGE OF CELL,IW IDENTIFIERS MC811
                IP=IP+1 MC811
                I1=BKTBL(I,1) MC811
                I2=BKTBL(I,2) MC811
                DO 15 J=1,MXY MC811
                    INV(IP,J)=0 MC811
                    Y(IP,J)=0 MC811
15             CONTINUE MC811
                BKTBL(IP,1)=I1 MC811
                BKTBL(IP,2)=I2 MC811
            ENDIF MC811
C --- ACCUMULATE MC811
            I3=BKTBL(I,3) MC811
            DO 20 J=1,MXY MC811
                INV(IP,J)=INV(IP,J)+SINV(I3,J) MC811
                Y(IP,J)= Y(IP,J)+ SY(I3,J) MC811
                TINV=TINV+SINV(I3,J) MC811
                TY= TY+ SY(I3,J) MC811
20         CONTINUE MC811
10         CONTINUE MC811
            WRITE(6,*) '==== TOTAL INV,Y AFTER BREAKDOWN=' ,TINV,TY MC811
C
            NBK=IP MC811
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES MC811
            DO 40 I=1,NBK MC811
                DO 30 J=1,MXY MC811
                    IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J) MC811
30         CONTINUE MC811
40         CONTINUE MC811
        END MC811

```

C. ESTIMATION SUBROUTINES

```

      SUBROUTINE MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY) MC800010
C --- CONDUCTS FIRST FIVE ESTIMATION METHODS MC800020
C MC800030
      REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC800040
      REAL XTB(MXX), VXTB(MXX), A(MXX) MC800050
C MC800060
      CALL EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC800070
      PRINT *, 'COMPLETED EBTS1' MC800080
C MC800090
      CALL EBTS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC800100
      PRINT *, 'COMPLETED EBTS2' MC800110
C MC800120
      CALL EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC800130
      PRINT *, 'COMPLETED EBOS1' MC800140
C MC800150
      CALL EBOS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC800160
      PRINT *, 'COMPLETED EBOS2' MC800170
C MC800180
      CALL EMTS(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY) MC800190
      PRINT *, 'COMPLETED EMTS' MC800200
C MC800210
      END MC800220
C MC800230
*****MC800240
C MC800250
      SUBROUTINE EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC800260
C --- TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD MC800270
      REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC800280
      REAL XTB(MXX), VXTB(MXX) MC800290
      REAL MAXL,MINL,L,MAXCHI,MINCHI MC800300
      INTEGER T, VYR MC800310
      DATA AA/1.6835/, B1/- .8934/, B2/.9881/ MC800320
      MAXL= -1000.0 MC800330
      MINL= 1000.0 MC800340
      SUML= 0.0 MC800350
      KLSUM=0 MC800360
      MAXCHI= -1000.0 MC800370
      MINCHI= 1000.0 MC800380
      SUMCHI= 0.0 MC800390
      KSUM=0 MC800400
      SUMMAD=0.0 MC800410
      KPSUM=0 MC800420
      WRITE(11,32)' ' MC800430
      WRITE(11,21)'EMP BAYES TRANS SCALE - TIME DEP VAR:' MC800440
      WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):' MC800450
      WRITE(11,28)'FRACTION CELLS','FRACTION MAD' MC800460
      WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD' MC800470
      WRITE(11,30) MC800480
C MC800490
C --- LOOP THROUGH VALIDATION YEARS MC800500
      DO 280 VYR=1, NYR MC800510
C --- LOOP THROUGH CELLS MC800520
      DO 260 IN=1, NRC MC800530

```

```

T=0 MC8005
SUMXT=0 MC8005
SUMVAR=0 MC8005
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB) MC8005
DO 200 IT=1, NYR MC8005
    IF(IT .NE. VYR) THEN MC8005
        IF( INV(IN,IT) .NE. 0) THEN MC8006
            X=FTT( INV(IN,IT), Y(IN,IT)) MC8006
            C=SQRT(0.5+INV(IN,IT)) MC8006
            XX=X+C*(3.141592654/2.0) MC8006
            XT=X/C MC8006
            T=T+1 MC8006
            SUMXT=SUMXT+XT MC8006
            IF(XX .LT. 1.001) XX=1.001 MC8006
            VARX=AA*(XX**B1)*(XX-1)**B2 MC8006
            IF(VARX .GT. 1.0) VARX=1.0 MC8006
            VARXT=VARX/(0.5+INV(IN,IT)) MC8007
            SUMVAR=SUMVAR+VARXT MC8007
        ENDIF MC8007
    ENDIF MC8007
200 CONTINUE MC80074
    XTB(IN)=SUMXT/T MC80075
    VXTB(IN)=SUMVAR/T**2 MC80076
260 CONTINUE MC80077
C MC80078
C --- CONDUCT ALGORITHM TO FIND XEB MC80079
    CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR) MC80080
C MC80081
C --- COMPUTE MEAN SQUARED ERROR MC80082
    CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL) MC80083
        IF(L .LT. MINL) THEN MC80084
            MINL=L MC80085
            MINLK=KL MC80086
            MINLYR=VYR MC80087
        ELSE IF(L .GT. MAXL) THEN MC80088
            MAXL=L MC80089
            MAXLK=KL MC80090
            MAXLYR=VYR MC80091
        ENDIF MC80092
        SUML=SUML+L*KL MC80093
        KLSUM=KLSUM+KL MC80094
C MC80095
C --- INVERT XEB TO ORIGINAL SCALE MC80096
    CALL INVERT(NRC,XEB,MXX) MC80097
C MC80098
C --- COMPUTE MAD AND CHI SQUARE MC80099
    CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,
    *          FCELLU,FMADU,PMAD,KP) MC80100
        IF(CHI .LT. MINCHI) THEN MC80101
            MINCHI=CHI MC80102
            MNCHIK=K MC80103
            MNCHYR=VYR MC80104
        ELSE IF(CHI .GT. MAXCHI) THEN MC80105
            MAXCHI=CHI MC80106
            MXCHIK=K MC80107
            MXCHYR=VYR MC80108
    ENDIF MC80109

```

```

ENDIF
SUMCHI=SUMCHI+CHI*K
KSUM=KSUM+K
KPSUM=KPSUM+KP
SUMMAD=SUMMAD+PMAD*KP
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD
280 CONTINUE
C
C --- WRITE RESULTS TO OUTPUT FILE
AVGL=SUML/KLSUM
AVGCHI=SUMCHI/KSUM
AVGMAD=SUMMAD/KPSUM
WRITE(11,19)'AVG MAD = ',AVGMAD
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC801240
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC801250
WRITE(11,26)'AVG CHI = ',AVGCHI
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR
WRITE(11,27)'AVG MSE = ',AVGL
19 FORMAT(38X,A,F5. 3)
21 FORMAT(/1X,A)
25 FORMAT(1X,A,F6. 3,5X,A,I3,5X,A,I2)
26 FORMAT(1X,A,F9. 3,5X,A,I3,5X,A,I2)
27 FORMAT(1X,A,F6. 3/)
28 FORMAT(17X,A,2X,A)
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)
30 FORMAT(1X,8(' -'),2X,4(' -'),2X,14(' -'),2X,13(' -'),2X,5(' -'))
31 FORMAT(1X,I5,I8,8X,F5. 3,10X,F5. 3,6X,F5. 3)
32 FORMAT(1X,A)
RETURN
END
C
SUBROUTINE EBTS2( INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)
C --- TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)
REAL XTB(MXX), VXTB(MXX)
REAL MAXL,MINL,L,MAXCHI,MINCHI
INTEGER T, VYR
MAXL= -1000. 0
MINL= 1000. 0
SUML= 0. 0
KLSUM=0
MAXCHI= -1000. 0
MINCHI= 1000. 0
SUMCHI= 0. 0
KSUM=0
SUMMAD=0. 0
KPSUM=0
WRITE(11,21)'EMP BAYES TRANS SCALE - TIME INDEP VAR: '
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'
MC801100
MC801110
MC801120
MC801130
MC801140
MC801150
MC801160
MC801170
MC801180
MC801190
MC801200
MC801210
MC801220
MC801230
MC801240
MC801250
MC801260
MC801270
MC801280
MC801290
MC801300
MC801310
MC801320
MC801330
MC801340
MC801350
MC801360
MC801370
MC801380
MC801390
MC801400
MC801410
MC801420
MC801430
MC801440
MC801450
MC801460
MC801470
MC801480
MC801490
MC801500
MC801510
MC801520
MC801530
MC801540
MC801550
MC801560
MC801570
MC801580
MC801590
MC801600
MC801610
MC801620
MC801630
MC801640
MC801650

```

```

      WRITE(11,30)                                MC8016
C
C --- LOOP THROUGH VALIDATION YEARS           MC8016
      DO 380  VYR=1, NYR                         MC8016
C --- LOOP THROUGH CELLS                      MC8017
      DO 360  IN=1, NRC                          MC8017
          T=0                                     MC8017
          SUMXT=0                                 MC8017
          SUMXT2=0                               MC8017
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB) MC8017
      DO 300  IT=1, NYR                          MC8017
          IF(IT .NE. VYR) THEN                   MC8017
              IF(INV(IN,IT) .NE. 0) THEN         MC8017
                  X=FTT(INV(IN,IT), Y(IN,IT))   MC8017
                  XT=X/SQRT(0.5+INV(IN,IT))     MC8018
                  T=T+1                         MC8018
                  SUMXT=SUMXT+XT                MC8018
                  SUMXT2=SUMXT2+XT**2            MC8018
              ENDIF                           MC8018
          ENDIF                           MC8018
 300    CONTINUE                                MC8018
          XTB(IN)=SUMXT/T                     MC8018
          VXTB(IN)=((T*SUMXT2)-(SUMXT**2))/((T-1)*T**2)  MC8018
 360    CONTINUE                                MC8018
C
C --- CONDUCT ALGORITHM TO FIND XEB          MC8019
      CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)    MC8019
C
C --- COMPUTE MEAN SQUARED ERROR             MC8019
      CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)  MC8019
          IF(L .LT. MINL) THEN                 MC8019
              MINL=L                         MC8019
              MINLK=KL                      MC8019
              MINLYR=VYR                    MC8019
          ELSE IF(L .GT. MAXL) THEN          MC8020
              MAXL=L                         MC8020
              MAXLK=KL                      MC8020
              MAXLYR=VYR                    MC8020
          ENDIF                           MC8020
          SUML=SUML+L*KL                  MC8020
          KLSUM=KLSUM+KL                  MC8020
C
C --- INVERT XEB TO ORIGINAL SCALE          MC8020
      CALL INVERT(NRC,XEB,MXX)                 MC8020
C
C --- COMPUTE MAD AND CHI SQUARE            MC8021
      CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,  MC8021
      *          FCELLU,FMADU,PMAD,KP)        MC8021
          IF(CHI .LT. MINCHI) THEN          MC8021
              MINCHI=CHI                  MC8021
              MNCHIK=K                  MC8021
              MNCHYR=VYR                MC8021
          ELSE IF(CHI .GT. MAXCHI) THEN    MC8021
              MAXCHI=CHI                MC8021
              MXCHIK=K                  MC8022
              MXCHYR=VYR                MC8022

```

```

ENDIF MC802220
SUMCHI=SUMCHI+CHI*K MC802230
KSUM=KSUM+K MC802240
KPSUM=KPSUM+KP MC802250
SUMMAD=SUMMAD+PMAD*KP MC802260
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD MC802270
380 CONTINUE MC802280
C MC802290
C --- WRITE OUTPUT TO FILE MC802300
AVGL=SUML/KLSUM MC802310
AVGCHI=SUMCHI/KSUM MC802320
AVGMAD=SUMMAD/KPSUM MC802330
WRITE(11,19)'AVG MAD = ',AVGMAD MC802340
WRITE(11,21)'CHI SQUARE (ORIG SCALE):' MC802350
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC802360
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC802370
WRITE(11,26)'AVG CHI = ',AVGCHI MC802380
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE):' MC802390
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR MC802400
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR MC802410
WRITE(11,27)'AVG MSE = ',AVGL MC802420
19 FORMAT(38X,A,F5.3) MC802430
21 FORMAT(/1X,A) MC802440
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2) MC802450
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2) MC802460
27 FORMAT(1X,A,F6.3/) MC802470
28 FORMAT(17X,A,2X,A) MC802480
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A) MC802490
30 FORMAT(1X,8('-'),2X,4('-'),2X,14('-'),2X,13('-'),2X,5('-')) MC802500
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3) MC802510
      RETURN MC802520
      END MC802530
C MC802540
***** MC802550
C MC802560
      SUBROUTINE EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC802570
C --- ORIGINAL SCALE, TIME DEPENDENT VARIANCE METHOD MC802580
      REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC802590
      REAL XTB(MXX), VXTB(MXX) MC802600
      REAL MAXCHI, MINCHI MC802610
      INTEGER T, VYR MC802620
      MAXCHI= -1000.0 MC802630
      MINCHI= 1000.0 MC802640
      SUMCHI= 0.0 MC802650
      KSUM=0 MC802660
      SUMMAD=0.0 MC802670
      KPSUM=0 MC802680
      WRITE(11,21)'EMP BAYES ORIG SCALE - TIME DEP VAR:' MC802690
      WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):' MC802700
      WRITE(11,28)'FRACTION CELLS','FRACTION MAD' MC802710
      WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD' MC802720
      WRITE(11,30) MC802730
C MC802740
C --- LOOP THROUGH VALIDATION YEARS MC802750
      DO 480 VYR=1, NYR MC802760
C --- LOOP THROUGH CELLS MC802770

```

```

DO 460 IN=1, NRC          MC802
    T=0                      MC802
    SUMXT=0                  MC802
    SUMVAR=0                  MC802
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB) MC802
DO 400 IT=1, NYR          MC802
    IF(IT .NE. VYR) THEN    MC802
        IF(INV(IN,IT) .NE. 0) THEN MC802
            PHAT=Y(IN,IT)/INV(IN,IT) MC802
            T=T+1                  MC802
            SUMXT=SUMXT+PHAT      MC802
            IF(PHAT .GT. 0.0) THEN MC802
                SUMVAR=SUMVAR+PHAT*(1-PHAT)/INV(IN,IT) MC802
            ELSE                   MC802
                SUMVAR=SUMVAR+1/(INV(IN,IT)+1)**2     MC802
            ENDIF                  MC802
        ENDIF                  MC802
    ENDIF                  MC802
400  CONTINUE              MC802
    XTB(IN)=SUMXT/T          MC802
    VXTB(IN)=SUMVAR/T**2      MC802
460  CONTINUE              MC802
C
C --- CONDUCT ALGORITHM TO FIND XEB          MC803
    CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR) MC803
C
C --- COMPUTE MAD AND CHI SQUARE          MC803
    CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY, MC803
    *           FCELLU,FMADU,PMAD,KP) MC803
    IF(CHI .LT. MINCHI) THEN MC803
        MINCHI=CHI          MC803
        MNCHIK=K             MC803
        MNCHYR=VYR           MC8031
    ELSE IF(CHI .GT. MAXCHI) THEN MC8031
        MAXCHI=CHI           MC8031
        MXCHIK=K             MC8031
        MXCHYR=VYR           MC8031
    ENDIF                  MC8031
    SUMCHI=SUMCHI+CHI*K       MC8031
    KSUM=KSUM+K              MC8031
    KPSUM=KPSUM+KP           MC8031
    SUMMAD=SUMMAD+PMAD*KP   MC8031
    WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD   MC8032
480  CONTINUE              MC8032
C
C --- WRITE OUTPUT TO FILE          MC8032
    AVGCHI=SUMCHI/KSUM         MC8032
    AVGMAD=SUMMAD/KPSUM       MC8032
    WRITE(11,19)'AVG MAD = ',AVGMAD      MC8032
    WRITE(11,21)'CHI SQUARE (ORIG SCALE):' MC8032
    WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC8032
    WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC8032
    WRITE(11,27)'AVG CHI = ',AVGCHI        MC8033
19   FORMAT(38X,A,F5.3)        MC8033
21   FORMAT(/1X,A)           MC8033
26   FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)  MC8033

```

```

27 FORMAT(1X,A,F9.3/) MC803340
28 FORMAT(17X,A,2X,A) MC803350
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A) MC803360
30 FORMAT(1X,8(' -'),2X,4(' -'),2X,14(' -'),2X,13(' -'),2X,5(' -')) MC803370
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3) MC803380
      RETURN MC803390
      END MC803400
C MC803410
***** MC803420
C MC803430
C MC803440
C --- SUBROUTINE EBOS2( INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY) MC803450
C --- ORIGINAL SCALE, TIME INDEPENDENT VARIANCE METHOD MC803460
      REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)
      REAL XTB(MXX), VXTB(MXX)
      REAL MAXCHI, MINCHI
      INTEGER T, VYR
      MAXCHI= -1000.0
      MINCHI= 1000.0
      SUMCHI= 0.0
      KSUM=0
      SUMMAD=0.0
      KPSUM=0
      WRITE(11,21)'EMP BAYES ORIG SCALE - TIME INDEP VAR: ' MC803560
      WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): ' MC803570
      WRITE(11,28)'FRACTION CELLS','FRACTION MAD' MC803580
      WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD' MC803590
      WRITE(11,30) MC803600
C MC803610
C --- LOOP THROUGH VALIDATION YEARS MC803620
      DO 580 VYR=1, NYR MC803630
C --- LOOP THROUGH CELLS MC803640
      DO 560 IN=1, NRC MC803650
          T=0
          SUMXT=0
          SUMVAR=0
          SUMY=0
          SUMINV=0
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB) MC803710
      DO 500 IT=1, NYR MC803720
          IF(IT .NE. VYR) THEN MC803730
              IF(INV(IN,IT) .NE. 0) THEN MC803740
                  PHAT=Y(IN,IT)/INV(IN,IT)
                  SUMXT=SUMXT+PHAT
                  SUMY=SUMY+Y(IN,IT)
                  SUMINV=SUMINV+INV(IN,IT)
                  T=T+1
                  SUMVAR=SUMVAR+1.0/INV(IN,IT)
              ENDIF MC803800
          ENDIF MC803810
      CONTINUE MC803820
      XTB(IN)=SUMXT/T MC803830
      IF(SUMY .GT. 0.0) THEN MC803840
          PTILDE=SUMY/SUMINV
          VXTB(IN)=(PTILDE*(1-PTILDE)*SUMVAR)/T**2 MC803850
      ELSE MC803860
          VXTB(IN)=SUMINV*SUMVAR/(((1+SUMINV)**2)*T**2) MC803870
      END MC803880
      MC803890

```

```

        ENDIF MC8039
560 CONTINUE MC8039
C MC8039
C --- CONDUCT ALGORITHM TO FIND XEB MC8039
    CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR) MC8039
C MC8039
C --- COMPUTE MAD AND CHI SQUARE MC8039
    CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY, MC8039
*          FCELLU,FMADU,PMAD,KP) MC8039
        IF(CHI .LT. MINCHI) THEN MC8039
            MINCHI=CHI MC8040
            MNCHIK=K MC8040
            MNCHYR=VYR MC8040
        ELSE IF(CHI .GT. MAXCHI) THEN MC8040
            MAXCHI=CHI MC8040
            MXCHIK=K MC8040
            MXCHYR=VYR MC8040
        ENDIF MC8040
        SUMCHI=SUMCHI+CHI*K MC8040
        KSUM=KSUM+K MC8040
        KPSUM=KPSUM+KP MC8041
        SUMMAD=SUMMAD+PMAD*KP MC8041
        WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD MC8041
580 CONTINUE MC8041
C MC8041
C --- WRITE OUTPUT TO FILE MC8041
    AVGCHI=SUMCHI/KSUM MC8041
    AVGMAD=SUMMAD/KPSUM MC8041
    WRITE(11,19)'AVG MAD = ',AVGMAD MC8041
    WRITE(11,21)'CHI SQUARE (ORIG SCALE):' MC8041
    WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC8042
    WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC8042
    WRITE(11,27)'AVG CHI = ',AVGCHI MC8042
19 FORMAT(38X,A,F5. 3) MC8042
21 FORMAT(/1X,A) MC8042
26 FORMAT(1X,A,F9. 3,5X,A,I3,5X,A,I2) MC8042
27 FORMAT(1X,A,F9. 3/) MC8042
28 FORMAT(17X,A,2X,A) MC8042
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A) MC8042
30 FORMAT(1X,8('-'),2X,4('-'),2X,14('-'),2X,13('-'),2X,5('-')) MC8042
31 FORMAT(1X,I5,I8,8X,F5. 3,10X,F5. 3,6X,F5. 3) MC8043
    RETURN MC8043
    END MC8043
C ***** MC8043
C MC8043
C SUBROUTINE EMTS( INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY) MC8043
C --- EFRON-MORRIS METHOD MC8043
    REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC8043
    REAL XTB(MXX), VXTB(MXX), A(MXX) MC8043
    REAL MAXL,MINL,L,MAXCHI,MINCHI MC8044
    INTEGER T, VYR MC8044
    DATA AA/1. 6835/, B1/- .8934/, B2/. 9881/ MC8044
    MAXL= -1000. 0 MC8044
    MINL= 1000. 0 MC8044
    SUML= 0. 0 MC8044

```

```

KLSUM=0 MC804460
MAXCHI= -1000.0 MC804470
MINCHI= 1000.0 MC804480
SUMCHI= 0.0 MC804490
KSUM=0 MC804500
SUMMAD=0.0 MC804510
KPSUM=0 MC804520
WRITE(11,21)'EFRON-MORRIS TRANS SCALE - TIME DEP VAR:' MC804530
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):' MC804540
WRITE(11,28)'FRACTION CELLS','FRACTION MAD' MC804550
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD' MC804560
WRITE(11,30) MC804570

C MC804580
C --- LOOP THROUGH VALIDATION YEARS MC804590
DO 280 VYR=1, NYR MC804600
C --- LOOP THROUGH CELLS MC804610
DO 260 IN=1, NRC MC804620
    T=0 MC804630
    SUMXT=0 MC804640
    SUMVAR=0 MC804650
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB) MC804660
DO 200 IT=1, NYR MC804670
    IF(IT .NE. VYR) THEN MC804680
        IF(INV(IN,IT) .NE. 0) THEN MC804690
            X=FTT(INV(IN,IT), Y(IN,IT)) MC804700
            C=SQRT(0.5+INV(IN,IT)) MC804710
            XX=X+C*(3.141592654/2.0) MC804720
            XT=X/C MC804730
            T=T+1 MC804740
            SUMXT=SUMXT+XT MC804750
            IF(XX .LT. 1.001) XX=1.001 MC804760
            VARX=AA*(XX**B1)*(XX-1)**B2 MC804770
            IF(VARX .GT. 1.0) VARX=1.0 MC804780
            VARXT=VARX/(0.5+INV(IN,IT)) MC804790
            SUMVAR=SUMVAR+VARXT MC804800
        ENDIF MC804810
    ENDIF MC804820
200    CONTINUE MC804830
        XTB(IN)=SUMXT/T MC804840
        VXTB(IN)=SUMVAR/T**2 MC804850
260    CONTINUE MC804860

C MC804870
C --- CONDUCT ALGORITHM TO FIND XEB MC804880
    CALL EMITER(NRC,XTB,VXTB,XEB,A,MXX,VYR) MC804890
C MC804900
C --- COMPUTE MEAN SQUARED ERROR MC804910
    CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL) MC804920
    IF(L .LT. MINL) THEN MC804930
        MINL=L MC804940
        MINLK=KL MC804950
        MINLYR=VYR MC804960
    ELSE IF(L .GT. MAXL) THEN MC804970
        MAXL=L MC804980
        MAXLK=KL MC804990
        MAXLYR=VYR MC805000
    ENDIF MC805010

```

```

SUML=SUML+L*KL MC8050
KLSUM=KLSUM+KL MC8050
C MC8050
C --- INVERT XEB TO ORIGINAL SCALE MC8050
    CALL INVERT(NRC,XEB,MXX) MC8050
C MC8050
C --- COMPUTE MAD AND CHI SQUARE MC8050
    CALL OSMOE( INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY, MC8050
*          FCELLU,FMADU,PMAD,KP) MC8051
        IF(CHI .LT. MINCHI) THEN MC8051
            MINCHI=CHI MC8051
            MNCHIK=K MC8051
            MNCHYR=VYR MC8051
        ELSE IF(CHI .GT. MAXCHI) THEN MC8051
            MAXCHI=CHI MC8051
            MXCHIK=K MC8051
            MXCHYR=VYR MC8051
        ENDIF MC8051
        SUMCHI=SUMCHI+CHI*K MC8052
        KSUM=KSUM+K MC8052
        KPSUM=KPSUM+KP MC8052
        SUMMAD=SUMMAD+PMAD*KP MC8052
        WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD MC8052
280 CONTINUE MC8052
C MC8052
C --- WRITE OUTPUT TO FILE MC8052
    AVGL=SUML/KLSUM MC8052
    AVGCHI=SUMCHI/KSUM MC8052
    AVGMAD=SUMMAD/KPSUM MC8053
    WRITE(11,19)'AVG MAD = ',AVGMAD MC8053
    WRITE(11,21)'CHI SQUARE (ORIG SCALE):' MC8053
    WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC8053
    WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC8053
    WRITE(11,26)'AVG CHI = ',AVGCHI MC80535
    WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE):' MC80536
    WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR MC80537
    WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR MC80538
    WRITE(11,27)'AVG MSE = ',AVGL MC80539
19 FORMAT(38X,A,F5. 3) MC80540
21 FORMAT(/1X,A) MC80541
25 FORMAT(1X,A,F6. 3,5X,A,I3,5X,A,I2) MC80542
26 FORMAT(1X,A,F9. 3,5X,A,I3,5X,A,I2) MC80543
27 FORMAT(1X,A,F6. 3) MC80544
28 FORMAT(17X,A,2X,A) MC80545
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A) MC80546
30 FORMAT(1X,8(' -'),2X,4(' -'),2X,14(' -'),2X,13(' -'),2X,5(' -')) MC80547
31 FORMAT(1X,I5,I8,8X,F5. 3,10X,F5. 3,6X,F5. 3) MC80548
    RETURN MC80549
    END MC80550
C **** MC80552
C MC80553
SUBROUTINE EBITER(NRC,XTB,VXTB,XEB,MXX,VYR) MC80554
C --- ITERATIVE ALGORITHM TO SOLVE FOR XEB MC80555
    REAL XTB(MXX), VXTB(MXX), XEB(MXX) MC80556
    INTEGER VYR MC80557

```

```

A=0 MC805580
ITER=0 MC805590
100 CONTINUE MC805600
ITER=ITER+1 MC805610
IF(ITER .GT. 100) PRINT *, 'EBITER GT 100' MC805620
AO=A MC805630
SUMALK=0 MC805640
C MC805650
C --- SUM THE ALPHAS MC805660
DO 200 I=1,NRC MC805670
    SUMALK=SUMALK+1/(A+VXTB(I)) MC805680
200 CONTINUE MC805690
C MC805700
C --- COMPUTE XBB MC805710
XBB=0 MC805720
DO 300 I=1,NRC MC805730
    ALPHA=1/(A+VXTB(I)) MC805740
    GAMMA=ALPHA/SUMALK MC805750
    XBB=XBB+GAMMA*XTB(I) MC805760
300 CONTINUE MC805770
C MC805780
C --- UPDATE VALUE OF A MC805790
SUMNUM=0 MC805800
SUMDEN=0 MC805810
DO 400 I=1,NRC MC805820
    ALPHA=1/(A+VXTB(I)) MC805830
    SUMNUM=SUMNUM+ALPHA**((XTB(I)-XBB)**2) MC805840
    SUMDEN=SUMDEN+((XTB(I)-XBB)**2)*ALPHA**2 MC805850
400 CONTINUE MC805860
A=A-(NRC-1-SUMNUM)/SUMDEN MC805870
IF(A .LE. 0) THEN MC805880
    A=0 MC805890
    GO TO 500 MC805900
ENDIF MC805910
IF(ABS(A-A0) .GT. 0.0001) GO TO 100 MC805920
500 CONTINUE MC805930
C MC805940
C --- ITERATIONS CONVERGED, COMPUTE XEB MC805950
DO 600 I=1,NRC MC805960
    X=XTB(I) MC805970
    V=VXTB(I) MC805980
    XEB(I)=(A*X)/(A+V)+(V*XBB)/(A+V) MC805990
600 CONTINUE MC806000
RETURN MC806010
END MC806020
C MC806030
*****MC806040
C MC806050
SUBROUTINE EMITER(NRC,XTB,VXTB,XEM,A,MXX,VYR) MC806060
C --- ITERATIVE ALGORITHM TO SOLVE FOR XEB FOR EFRON-MORRIS METHOD MC806070
REAL XTB(MXX), VXTB(MXX), XEM(MXX), A(MXX) MC806080
INTEGER VYR MC806090
DO 100 I=1,NRC MC806100
    A(I)=0 MC806110

```

```

100 CONTINUE MC8061
C MC8061
C --- SUM THE ALPHAS MC8061
SUMALK=0 MC8061
DO 200 I=1,NRC MC8061
    SUMALK=SUMALK+1/(A(I)+VXTB(I)) MC8061
200 CONTINUE MC8061
C MC8061
C --- COMPUTE XHAT MC8062
XHAT=0 MC8062
DO 300 I=1,NRC MC8062
    ALPHA=1/(A(I)+VXTB(I)) MC8062
    GAMMA=ALPHA/SUMALK MC8062
    XHAT=XHAT+GAMMA*XTB(I) MC8062
300 CONTINUE MC8062
311 XHATP=XHAT MC8062
I=1 MC8062
333 AP=A(I) MC8062
S=(XTB(I)-XHAT)**2 MC8063
C MC8063
C --- COMPUTE SN AND SD MC8063
SN=0 MC8063
SD=0 MC8063
DO 400 J=1,NRC MC8063
    IF(J .NE. I) THEN MC8063
        DEN=(A(J)+VXTB(J))**2 MC8063
        SN=SN+((XTB(J)-XHAT)**2-VXTB(J))/DEN MC8063
        SD=SD+1/DEN MC8063
    ENDIF MC8064
400 CONTINUE MC8064
C MC8064
C --- NEWTON-RAPHSON ITERATIONS TO SOLVE FOR A MC8064
444 AD=A(I)+VXTB(I) MC8064
    GNUM=S-3*VXTB(I)+SN*AD**2 MC8064
    GDEN=3+SD*AD**2 MC8064
    GPRM=2*AD*SN/GDEN-2*GNUM*AD*SD/GDEN**2 MC8064
    G=GNUM/GDEN MC8064
    A(I)=A(I)-((A(I)-G)/(1-GPRM)) MC8064
    IF(A(I) .LE. 0.) THEN MC8065
        A(I)=0.0 MC8065
        I=I+1 MC8065
        IF(I .LE. NRC) THEN MC8065
            GO TO 333 MC8065
        ELSE MC8065
            GO TO 555 MC8065
        ENDIF MC8065
    ENDIF MC8065
    IF(ABS(A(I)-AP) .LE. 0.0001) THEN MC8065
        I=I+1 MC8066
        IF(I .LE. NRC) THEN MC8066
            GO TO 333 MC8066
        ELSE MC8066
            GO TO 555 MC8066
        ENDIF MC8066
    ELSE MC8066
        AP=A(I) MC8066
    ENDIF MC8067

```

```

        GO TO 444                                MC806680
      ENDIF                                         MC806690
C
C --- TEST FOR CONVERGENCE: ABS(S-SP) LT EPSILON   MC806700
 555  SUMALK=0                                    MC806710
      DO 600  J=1,NRC                            MC806720
          SUMALK=SUMALK+1/(A(J)+VXTB(J))          MC806730
 600  CONTINUE                                     MC806740
          XHAT=0                                     MC806750
          DO 700  J=1,NRC                            MC806760
              ALPHA=1/(A(J)+VXTB(J))                MC806770
              GAMMA=ALPHA/SUMALK                     MC806780
              XHAT=XHAT+GAMMA*XTB(J)                 MC806790
 700  CONTINUE                                     MC806800
          DO 800  J=1,NRC                            MC806810
              S=(XTB(J)-XHAT)**2                    MC806820
              SP=(XTB(J)-XHATP)**2                   MC806830
              IF(ABS(S-SP) .GT. 0.0001) GO TO 311    MC806840
 800  CONTINUE                                     MC806850
C
C --- ITERATIONS CONVERGED, COMPUTE XEM           MC806860
  DO 950  K=1,NRC                                MC806870
      SD=0                                         MC806880
      DO 900  J=1,NRC                            MC806890
          IF(J .NE. K) SD=SD+1/(A(J)+VXTB(J))**2  MC806900
 900  CONTINUE                                     MC806910
          AD=A(K)+VXTB(K)                         MC806920
          DSTAR=3+(AD**2)*SD                      MC806930
          B=(1.-4./DSTAR)*VXTB(K)/AD            MC806940
          IF(B .GT. 1.0) B=1.0                     MC806950
          IF(B .LT. 0.0) B=0.0                     MC806960
          XEM(K)=XHAT+(1-B)*(XTB(K)-XHAT)         MC806970
 950  CONTINUE                                     MC806980
      END                                           MC806990
C
*****SUBROUTINE MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)***MC807000
C
C --- COMPUTES MEAN SQUARED ERROR MOE             MC807010
  REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)        MC807020
  REAL L,MU                                         MC807030
  INTEGER VYR                                       MC807040
  SUMSE=0                                         MC807050
  KL=0                                            MC807060
  DO 100  I=1,NRC                                MC807070
      IF(INV(I,VYR) .GT. 0.0) THEN               MC807080
          X=FTT(INV(I,VYR),Y(I,VYR))            MC807090
          MU=X/SQRT(0.5+INV(I,VYR))              MC807100
          SUMSE=SUMSE+(XEB(I)-MU)**2              MC807110
          KL=KL+1                                 MC807120
      ENDIF                                         MC807130
 100  CONTINUE                                     MC807140
      L=SUMSE/KL                                    MC807150
      RETURN                                         MC807160
  END                                             MC807170
C

```

```

***** MC8072
C
      SUBROUTINE OSMOE( INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,
      *                      FCELLU,FMADU,PMAD,KP) MC8072
C --- COMPUTES MAD AND CHI SQUARE MOES MC8072
      REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC8072
      INTEGER VYR MC8073
      CHI=0.0 MC8073
      K=0 MC8073
      SUMPMO=0.0 MC8073
      SUMPMU=0.0 MC8073
      KPMO=0 MC8073
      KPMU=0 MC8073
      DO 100 I=1,NRC MC8073
          P=XEB(I) MC8073
          E=P*INV(I,VYR) MC8073
          A=Y(I,VYR) MC8074
C
C --- COMPUTE MAD FOR THIS CELL MC8074
      IF( INV(I,VYR) .GT. 0.0) THEN MC8074
          PA=A/INV(I,VYR) MC8074
          IF(P .GT. PA) THEN MC8074
              SUMPMO=SUMPMO+(P-PA) MC8074
              KPMO=KPMO+1 MC8074
          ELSE MC8074
              SUMPMU=SUMPMU+(PA-P) MC8074
              KPMU=KPMU+1 MC8075
          ENDIF MC8075
      ENDIF MC8075
C
C --- COMPUTE CHI SQUARE FOR THIS CELL MC8075
      IF(E .NE. 0.0 .AND. P .NE. 1.0) THEN MC8075
          K=K+1 MC8075
          CHI=CHI+((A-E)**2)/(E*(1-P)) MC8075
      ENDIF MC8075
100 CONTINUE MC8075
C
C --- COMPUTE WEIGHTED AVERAGES MC8076
      KP=KPMO+KPMU MC8076
      FCELLU=REAL(KPMU)/REAL(KP) MC8076
      FMADU=SUMPMU/(SUMPMU+SUMPMO) MC8076
      PMAD=(SUMPMU+SUMPMO)/KP MC8076
      RETURN MC8076
      END MC8076
C
***** MC8076
C
      SUBROUTINE INVERT(NRC,XEB,MXX) MC8077
C --- INVERT XEB TO ORIGINAL SCALE MC8077
      REAL XEB(MXX) MC8077
      DO 100 I=1, NRC MC8077
          P=0.5*(1+SIN(XEB(I))) MC8077
          IF (P .LT. 0.0) THEN MC8077
              P=0.0 MC8077
          ELSE IF (P .GT. 1.0) THEN MC8077
              P=1.0 MC8077

```

```

ENDIF MC807800
XEB(I)=P MC807810
100 CONTINUE MC807820
      RETURN MC807830
      END MC807840
C MC807850
*****MC807860
C MC807870
C MC807880
C --- CONDUCTS FREMAN-TUKEY TRANSFORM MC807890
REAL INV,Y MC807900
TEMP =-1. + 2.*Y/(1.+INV) MC807910
TEMP1=-1. + 2.*(1.+Y)/(1.+INV) MC807920
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN MC807930
    WRITE(6,*) 'FTT ERROR INV,Y=',INV,Y,TEMP,TEMP1 MC807940
    FTT=1 MC807950
    RETURN MC807960
ENDIF MC807970
FTT=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1)) MC807980
END MC807990

```

D. VECTOR METHOD SUBROUTINE

```

        SUBROUTINE MC87V( INV, Y, MXX, NYR, NRC, XTBJI, DELTA, X, XVYR, VYRINV,      MC8000
*      VYRY, BSTAR, S, GAMMA, XBBJ, EVAL, MXP, MXK, BKTBL, NBK, NSC, NCSR, ISFLAG) MC8000
C --- VECTOR METHOD
        REAL INV(MXX,NYR), Y(MXX,NYR)                                         MC8000
        REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK)                         MC8000
        REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK)                      MC8000
        REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP)                          MC8000
        REAL XBBJ(MXP), EVAL(MXP)                                                 MC8000
        INTEGER*2 BKTBL(MXX,3)                                                 MC8000
C
        REAL MAXL,MINL,L,MAXCHI,MINCHI,MO,MU,MAD
        INTEGER T, VYR, P
C
        MAXL= -1000.0
        MINL= 1000.0
        SUML= 0.0
        KPSUM=0
        MAXCHI= -1000.0
        MINCHI= 1000.0
        SUMCHI= 0.0
        KCsum=0
        WRITE(11,32) ' '
        WRITE(11,21)'EMP BAYES TRANS SCALE - VECTOR CASE: '
        IF (ISFLAG .EQ. 1) THEN
          P=NSC
          WRITE(11,21)'VECTOR IS BY SERVICE COMPONENT'
        ELSE
          P=NCSR
          WRITE(11,21)'VECTOR IS BY COMMISSIONING SOURCE'
        ENDIF
        WRITE(11,22)'K=',NRC,'P=',P,'KP= ',(NRC*P)
        WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '
        WRITE(11,28)'FRACTION CELLS','FRACTION MAD'
        WRITE(11,29)'VALID YR','KP','WITH UNDERAGE','FROM UNDERAGE','MAD'
        WRITE(11,30)
        K=NRC
        IF(K .LE. (P+2)) THEN
          WRITE(6,*)'*** ERROR IN VECTOR CASE: P+2 GT K ***'
          STOP
        ENDIF
C
C --- CONDUCT VALIDATION
        DO 999 VYR=1, NYR
        DO 90 J=1,MXP
          DO 80 I=1,MXK
            XTBJI(J,I)=0.0
            DELTA(J,I)=0.0
            XVYR(J,I)=0.0
80      CONTINUE
90      CONTINUE
      KMKG=BKTBL(1,1)
      NRC=1
C --- LOOP THROUGH CELLS IN VECTOR FORM

```

```

DO 130 I=1,NBK MC800540
  IF(BKTBL(I,1) .NE. KMKG) NRC=NRC+1 MC800550
  DO 100 J=1,P MC800560
    IF(BKTBL(I,2) .EQ. J) THEN MC800570
      JP=J MC800580
      GO TO 110 MC800590
    ENDIF MC800600
100  CONTINUE MC800610
  WRITE(6,*) '*** ERROR IN P VECTOR ASSIGNMENT ***' MC800620
110  T=0 MC800630
  SUMXT=0 MC800640
  SUMVAR=0 MC800650
C --- LOOP THROUGH YEARS OF DATA TO SOLVE FOR XTB AND VAR(XTB) MC800660
  DO 120 IT=1, NYR MC800670
    IF(IT .NE. VYR) THEN MC800680
      IF(INV(I,IT) .NE. 0) THEN MC800690
        XIJ=FTTV( INV(I,IT), Y(I,IT)) MC800700
        C=0.5+INV(I,IT) MC800710
        XT=XIJ/SQRT(C) MC800720
        SUMXT=SUMXT+XT MC800730
        SUMVAR=SUMVAR+1/C MC800740
        T=T+1 MC800750
      ENDIF MC800760
    ENDIF MC800770
120  CONTINUE MC800780
  XTBJI(JP,NRC)=SUMXT/T MC800790
C --- STORE VARIANCE MATRIX IN DELTA MATRIX (TEMPORARY) MC800800
  DELTA(JP,NRC)=SUMVAR/T**2 MC800810
C --- GET VALIDATION YEAR ESTIMATE, INVENTORY AND ATTRITION INFO MC800820
  IF( INV(I,VYR) .GT. 0.0) THEN MC800830
    XIJ=FTTV( INV(I,VYR), Y(I,VYR)) MC800840
    XT=XIJ/SQRT(0.5+INV(I,VYR)) MC800850
    XVYR(JP,NRC)=XT MC800860
  ENDIF MC800870
  VYRINV(JP,NRC)=INV(I,VYR) MC800880
  VYRY(JP,NRC)=Y(I,VYR) MC800890
  KMKG=BKTBL(I,1) MC800900
130  CONTINUE MC800910
  IF(K .NE. NRC) THEN MC800920
    WRITE(6,*) '*** ERROR IN VECTOR CASE: K NE NRC ***' MC800930
  ENDIF MC800940
C
C --- COMPUTE XBB SUB J MC800950
  DO 210 J=1,P MC800960
    SUMXTB=0.0 MC800970
    DO 200 I=1,K MC800980
      SUMXTB=SUMXTB+XTBJI(J,I) MC800990
    200  CONTINUE MC801000
    XBBJ(J)=SUMXTB/K MC801010
  210  CONTINUE MC801020
C
C --- COMPUTE X SUB JI MATRIX, MAKE A COPY IN DELTA MATRIX (TEMPORARY) MC801030
  DO 230 J=1,P MC801040
    DO 220 I=1,K MC801050
      X(J,I)=(XTBJI(J,I)-XBBJ(J))*SQRT(DELTA(J,I)) MC801060
      DELTA(J,I)=X(J,I) MC801070
    220  CONTINUE MC801080
  230  CONTINUE MC801090

```

```

220 CONTINUE MC8011
230 CONTINUE MC8011
C MC8011
C --- COMPUTE S MATRIX MC8011
CALL MXYTF(P,K,X,MXP,P,K,DELTA,MXP,P,P,S,MXP) MC8011
C MC8011
C --- DO EIGENANALYSIS OF S MC8011
C --- PUT EIGENVALUES INTO EVAL, EIGENVECTORS INTO GAMMA MC8011
CALL EVCSF(P,S,MXP,EVAL,GAMMA,MXP) MC8011
C MC8011
C --- CREATE ESTAR INVERSE MC8012
KP2=K-P-2 MC8012
DO 240 J=1,P MC8012
    IF(EVAL(J) .LT. KP2) THEN MC8012
        EVAL(J)=KP2 MC8012
    ENDIF MC8012
    EVAL(J)=1.0/EVAL(J) MC8012
240 CONTINUE MC8012
DO 260 I=1,P MC8012
    DO 250 J=1,P MC8012
        IF(I .EQ. J) THEN MC8013
            BSTAR(I,J)=EVAL(J) MC8013
        ELSE MC8013
            BSTAR(I,J)=0.0 MC8013
        ENDIF MC8013
250 CONTINUE MC8013
260 CONTINUE MC8013
C MC8013
C --- CREATE BSTAR = I - (K-P-2) S TILDE INVERSE MC8013
CALL MRRRR(P,P,GAMMA,MXP,P,P,BSTAR,MXP,P,P,S,MXP) MC8013
CALL MXYTF(P,P,S,MXP,P,P,GAMMA,MXP,P,P,BSTAR,MXP) MC8014
DO 280 I=1,P MC8014
    DO 270 J=1,P MC8014
        BSTAR(I,J)=KP2*BSTAR(I,J) MC8014
        IF(I .EQ. J) THEN MC8014
            BSTAR(I,J)=1.0-BSTAR(I,J) MC8014
        ELSE MC8014
            BSTAR(I,J)=0.0-BSTAR(I,J) MC8014
        ENDIF MC8014
270 CONTINUE MC8014
280 CONTINUE MC8015
C MC8015
C --- COMPUTE DELTA SUB JI MC8015
DO 300 J=1,P MC8015
    DO 290 I=1,K MC8015
        X(J,I)=XTBJI(J,I)-XBBJ(J) MC8015
290 CONTINUE MC8015
300 CONTINUE MC8015
CALL MRRRR(P,P,BSTAR,MXP,P,K,X,MXP,P,K,XTBJI,MXP) MC8015
DO 320 J=1,P MC8015
    DO 310 I=1,K MC8016
        DELTA(J,I)=XBBJ(J)+XTBJI(J,I) MC8016
310 CONTINUE MC8016
320 CONTINUE MC8016
C MC8016
C --- COMPUTE MSE MC8016

```



```

        ENDIF
        ENDIF
        IF(E.NE.0.0 . AND. PHAT.NE.1.0) THEN
            KCHI=KCHI+1
            CHI=CHI+((A-E)**2)/(E*(1-PHAT))
        ENDIF
400    CONTINUE
410    CONTINUE
        KMAD=KPMO+KPMU
        FCELLU=REAL(KPMU)/REAL(KMAD)
        FMADU=SUMPNU/(SUMPNU+SUMPNO)
        PMAD=(SUMPNU+SUMPNO)/KMAD
        IF(CHI .LT. MINCHI) THEN
            MINCHI=CHI
            MNCHIK=KCHI
            MNCHYR=VYR
        ELSE IF(CHI .GT. MAXCHI) THEN
            MAXCHI=CHI
            MXCHIK=KCHI
            MXCHYR=VYR
        ENDIF
        SUMCHI=SUMCHI+CHI*KCHI
        KCSUM=KCSUM+KCHI
        WRITE(11,31) VYR, KMAD, FCELLU, FMADU, PMAD
999    CONTINUE
        AVGL=SUML/KPSUM
        AVGCHI=SUMCHI/KCSUM
        WRITE(11,21)'CHI SQUARE (ORIG SCALE): '
        WRITE(11,26)'MIN CHI = ',MINCHI,'KP = ',MNCHIK,
        *           'VALID YR = ',MNCHYR
        WRITE(11,26)'MAX CHI = ',MAXCHI,'KP = ',MXCHIK,
        *           'VALID YR = ',MXCHYR
        WRITE(11,26)'AVG CHI = ',AVGCHI
        WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '
        WRITE(11,25)'MIN MSE = ',MINL,'KP = ',MINLKP,'VALID YR = ',MINLYR MC8025
        WRITE(11,25)'MAX MSE = ',MAXL,'KP = ',MAXLKP,'VALID YR = ',MAXLYR MC8025
        WRITE(11,27)'AVG MSE = ',AVGL
21    FORMAT(/1X,A)
22    FORMAT(1X,3(A,I3,5X))
25    FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)
26    FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)
27    FORMAT(1X,A,F6.3/)
28    FORMAT(17X,A,2X,A)
29    FORMAT(1X,A,3X,A,3X,A,2X,A,3X,A)
30    FORMAT(1X,8(' -'),2X,4(' -'),2X,14(' -'),2X,13(' -'),2X,5(' -')) MC8026
31    FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)
32    FORMAT(1X,A)
        WRITE(6,*)'COMPLETED VECTOR CASE'
        END
C *****MC8027*****
C
C          FUNCTION FTTV(INV,Y)
C --- CONDUCTS FREEMAN-TUKEY TRANSFORM
        REAL INV,Y
        TEMP =-1. + 2.*Y/(1.+INV)

```

```
TEMP1=-1. + 2.* (1.+Y)/(1.+INV) MC802780
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN MC802790
    WRITE(6,*) 'FTT ERROR INV,Y=',INV,Y,TEMP,TEMP1
    FTT=1
    RETURN
ENDIF MC802800
FTTV=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1)) MC802810
END MC802820
MC802830
MC802840
MC802850
```

E. EXEC PROGRAM

```
CP LINK MVS 103 103 RR
ACC 103 K
*****
FIL * CLEAR
FIL 01 K DSN F0968 MCOR87 DATA (RECFM FB LRECL 69 BLOCK 17940
FIL 02 DISK MC87 TEMP
FIL 06 &1 (RECFM FBA LRECL 150
FIL 25 DISK MCLASS PG15      (RECFM F LRECL 25
FIL 27 DISK MCLASS PG17      (RECFM F LRECL 25
FIL 29 DISK MCLASS PG19      (RECFM F LRECL 25
FIL 30 DISK MCLASS PG20      (RECFM F LRECL 25
FIL 31 DISK MCLASS PG21      (RECFM F LRECL 25
FIL 32 DISK MCLASS PG22      (RECFM F LRECL 25
&BEGSTACK
30.0      /* AVG INV THRESHOLD T */
30      /* NO. CELLS THRESHOLD K */
13      /* MOS (ONLY 1) */
4      /* YCS (ONLY 1) */
15      /* GRADE (ONLY 1) */
3 1 2 3  /* NO. SVC COMPS AND ARRAY(1-REG,2-AUGREG,3-RES,4=1+2,5=ALL */
1 16     /* NO. COMM SRCS AND ARRAY(1-15, 16=ALL)
1      /* 3RD DIMENSION (0=NONE, 1=SVC, 2=CS)
&END
LOAD MC87 (START CLEAR
```

F. SAMPLE DATA FILE

1	2	3	4	5	6	7
--	-	-	-	--	-	----
15	0	1	1	15	1	0.02
15	0	3	2	9	5	0.42
15	0	3	3	9	6	0.75
15	0	3	2	10	4	0.15
15	0	3	1	11	1	0.10
15	0	3	3	10	2	0.15
15	0	3	3	3	1	0.02
15	0	3	3	4	1	0.02
15	0	4	2	9	6	0.87
15	0	4	2	10	2	0.20
15	0	4	3	9	2	0.07
15	0	4	1	11	1	0.10
15	0	4	3	4	2	0.05
15	0	4	3	10	1	0.10
15	0	5	2	9	3	0.27
15	0	5	2	10	2	0.20
15	0	5	1	11	1	0.07
15	0	6	2	9	1	0.02
15	1	2	3	15	1	0.05
15	1	3	1	1	2	0.20
15	1	3	3	15	1	0.05
15	1	3	3	10	1	0.10
15	1	3	3	7	3	0.12
15	1	3	3	3	5	0.30
15	1	3	3	5	2	0.65
15	1	3	3	2	5	0.45
15	1	3	3	9	3	0.12
15	1	3	2	15	1	0.05
15	1	3	1	11	3	0.12
15	1	3	1	10	2	0.10
15	1	3	2	7	1	0.02
15	1	3	3	6	1	0.10
15	1	4	3	5	2	0.12
15	1	4	3	2	5	0.40
15	1	4	2	3	2	0.12
15	1	4	1	1	1	0.02
15	1	4	2	9	2	0.07
15	1	4	3	9	1	0.02
15	1	4	3	7	5	0.25
15	1	4	3	10	1	0.02
15	1	4	3	3	2	0.05
15	1	4	1	10	1	0.02
15	1	4	3	12	1	0.02
15	1	4	2	12	1	0.07

(remaining entries omitted)

Column descriptions:

- | | |
|-----------------------|-----------------------------|
| 1 - grade | 5 - commissioning source |
| 2 - MOS | 6 - number of records |
| 3 - YCS | 7 - total average inventory |
| 4 - service component | |

```

C --- PROGRAM TO CREATE INVENTORY DATA FILE BY GRADE MC8000
      PARAMETER (MXX=20000, MXY=10) MC8000
C --- CLASSIF. TABLE: GRADE, MOS, YCS, SVC, CS MC8000
      INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX) MC8000
      REAL AINV(MXX) MC8000
      INTEGER TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,RACE MC8000
      INTEGER DATA(MXY), SPG MC8000
      CHARACTER*7 CITLS MC8000
      DATA AINV/MXX*0./, NRECS/MXX*0/ MC8000
C
      WRITE(5,*) 'ENTER PG' MC8001
      READ(5,*) SPG MC8001
      WRITE(5,*) 'PG TO USE=' ,SPG MC8001
      ICR=0 MC8001
      NRC=0 MC8001
      NG=0 MC8001
      DO 10 I=1,999999 MC8001
      READ(1,100,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2, MC8001
      * RACE,CITLS,DATA MC8001
      ICR=ICR+1 MC8002
C --- CLASSIFY ALL RECORDS TYPE 0 MC8002
      IF(TYPE.GT. 0) GO TO 999 MC8002
C --- ADD NEW RECORD TO TABLE MC8002
      IF(PG.EQ.SPG) CALL ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL, MC8002
      * MXX, NRC,AINV,NRECS) MC8002
      IF(PG.EQ.SPG) NG=NG+1 MC8002
      IF(MOD(ICR,5000).EQ.0) WRITE(6,*) 'ICR,NRC=' ,ICR,NRC MC8002
10 CONTINUE MC8002
C
      999 CONTINUE MC8002
      WRITE(6,*) ' ' MC8003
      WRITE(6,*) 'TOTAL RECORDS READ      =' ,ICR MC8003
      WRITE(6,*) 'TOTAL RECORDS ACCEPTED   =' ,NG MC8003
      WRITE(6,*) 'TOTAL INVENTORY COMBINATIONS = ' ,NRC MC8003
      DO 20 I=1,NRC MC8003
      WRITE(2,101) (PTRTBL(I,J),J=1,5), NRECS(I),AINV(I) MC8003
20 CONTINUE MC8003
100 FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4) MC80038
101 FORMAT(I2,I4,I3,I2,I3, I4, F7.2) MC80039
      END MC80040
C
      SUBROUTINE ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL,MXX, NRC, MC80041
      * AINV,NRECS) MC80042
C --- SET INVENTORY POINTER FOR THIS ENTRY AND ACCUMULATE MC80043
      INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX) MC80044
      REAL AINV(MXX) MC80045
      INTEGER YCS,PG,MOS,CS,SVC MC80046
      INTEGER DATA(MXY) MC80047
      MINV=GETINV(PTRTBL, MXX,NRC, PG,MOS,YCS,SVC,CS) MC80049
      IF(MINV .EQ. 0) THEN MC80050
C ---      NEW COMBINATION MC80051
      NRC=NRC+1 MC80052
      IF(NRC .GT. MXX) THEN MC80053
          WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',NRC MC80054
          STOP MC80055
      ENDIF MC80056

```

```

      MINV=NRC          MC800570
      PTRTBL(MINV, 1)=PG MC800580
      PTRTBL(MINV, 2)=MOS MC800590
      PTRTBL(MINV, 3)=YCS MC800600
      PTRTBL(MINV, 4)=SVC MC800610
      PTRTBL(MINV, 5)=CS MC800620
      NRECS(MINV)=0      MC800630
ENDIF          MC800640
AI=0          MC800650
DO 110 IT=1,MXY MC800660
  AI=AI + FLOAT(DATA(IT)) MC800670
110 CONTINUE    MC800680
AINV(MINV)=AINV(MINV) + .25*AI/MXY MC800690
NRECS(MINV)=NRECS(MINV) + 1 MC800700
END          MC800710
C ---          MC800720
C --- FUNCTION GETINV(PTRTBL, MXX,NRC, PG,MOS,YCS,SVC,CS) MC800730
C --- FIND LOCATION OF MATCHING INVENTORY ENTRY FOR A LOSS MC800740
  INTEGER*2 PTRTBL(MXX, 5) MC800750
  INTEGER YCS,PG,MOS,CS,SVC MC800760
  DO 10 I=1,NRC MC800770
    IF(PTRTBL(I, 1) .EQ. PG .AND. MC800780
*      PTRTBL(I, 2) .EQ. MOS .AND. MC800790
*      PTRTBL(I, 3) .EQ. YCS .AND. MC800800
*      PTRTBL(I, 4) .EQ. SVC .AND. MC800810
*      PTRTBL(I, 5) .EQ. CS ) THEN MC800820
      GETINV=I          MC800830
      RETURN            MC800840
    ENDIF          MC800850
10 CONTINUE    MC800860
GETINV=0      MC800870
END          MC800880

```

APPENDIX C. SAMPLE OUTPUT

A. GENERAL

This appendix contains sample output from the computer program. A sample output for test cases one through 30 which use the first five estimation methods is shown in paragraph B. A sample output for the vector test cases is shown in paragraph C. These examples show the output that is produced by the WRITE statements for file definition 11, e.g., WRITE(11,101). The program also contains several WRITE and PRINT statements that provide interactive information to the user via the terminal screen, e.g., WRITE(6,*), WRITE(5,*) and PRINT *. This interactive output is omitted.

B. SAMPLE OUTPUT (TEST CASES 1-30)

TEST CASE INPUT PARAMETERS:

INVENTORY THRESHOLD= 30.0 THRESHOLD NO. OF CELLS= 30
MOS= 13 YCS= 4 GRADE= 15
SERVICE COMPONENTS= 1 2 3
COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

EXPANSION INFORMATION:

ACTUAL NO. OF CELLS USED= 24
MOS GROUP # 1 YCS'S USED=
 4 5
LARGE MOS GROUP #1 YCS'S USED=
 4 5
MAJOR MOS GROUP #1 YCS'S USED=
 4 5

EMP BAYES TRANS SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID	YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1		24	0.458	0.478	0.127
2		24	0.250	0.187	0.099
3		24	0.542	0.441	0.098
4		24	0.333	0.375	0.069
5		24	0.417	0.352	0.072
6		24	0.125	0.053	0.082
7		24	0.208	0.138	0.099
8		24	0.417	0.472	0.077
9		24	0.833	0.943	0.181
10		24	0.833	0.952	0.113
				AVG MAD =	0.102

CHI SQUARE (ORIG SCALE):

MIN CHI = 48.590 K = 24 VALID YR = 8
MAX CHI = 329.334 K = 24 VALID YR = 9
AVG CHI = 98.791

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.033 K = 24 VALID YR = 4
MAX MSE = 0.205 K = 24 VALID YR = 9
AVG MSE = 0.079

EMP BAYES TRANS SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS	FRACTION	MAD
		WITH UNDERAGE	FROM UNDERAGE	MAD
1	24	0.458	0.504	0.127
2	24	0.250	0.204	0.094
3	24	0.583	0.477	0.101
4	24	0.375	0.432	0.071
5	24	0.417	0.396	0.073
6	24	0.083	0.061	0.076
7	24	0.250	0.152	0.094
8	24	0.458	0.517	0.075
9	24	0.792	0.952	0.183
10	24	0.875	0.961	0.118
AVG MAD = 0.101				

CHI SQUARE (ORIG SCALE):

MIN CHI = 45.452 K = 24 VALID YR = 6
MAX CHI = 344.445 K = 24 VALID YR = 9
AVG CHI = 99.284

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.036 K = 24 VALID YR = 4
MAX MSE = 0.213 K = 24 VALID YR = 9
AVG MSE = 0.078

EMP BAYES ORIG SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS	FRACTION	MAD
		WITH UNDERAGE	FROM UNDERAGE	MAD
1	24	0.458	0.478	0.127
2	24	0.250	0.195	0.097
3	24	0.542	0.461	0.093
4	24	0.333	0.397	0.070
5	24	0.417	0.375	0.074
6	24	0.125	0.057	0.079
7	24	0.208	0.161	0.102
8	24	0.417	0.488	0.079
9	24	0.833	0.944	0.185
10	24	0.833	0.952	0.117
AVG MAD = 0.102				

CHI SQUARE (ORIG SCALE):

MIN CHI = 49.207 K = 24 VALID YR = 6
 MAX CHI = 340.035 K = 24 VALID YR = 9
 AVG CHI = 100.985

EMP BAYES ORIG SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.479	0.127
2	24	0.250	0.196	0.097
3	24	0.542	0.462	0.093
4	24	0.333	0.399	0.070
5	24	0.417	0.377	0.075
6	24	0.125	0.056	0.079
7	24	0.208	0.161	0.101
8	24	0.417	0.490	0.079
9	24	0.833	0.945	0.185
10	24	0.833	0.953	0.117
AVG MAD = 0.102				

CHI SQUARE (ORIG SCALE):

MIN CHI = 48.836 K = 24 VALID YR = 6
 MAX CHI = 339.835 K = 24 VALID YR = 9
 AVG CHI = 100.960

EFRON-MORRIS TRANS SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.475	0.126
2	24	0.250	0.172	0.095
3	24	0.583	0.451	0.102
4	24	0.375	0.365	0.076
5	24	0.333	0.348	0.076
6	24	0.083	0.046	0.082
7	24	0.208	0.135	0.098
8	24	0.458	0.469	0.076
9	24	0.708	0.938	0.185
10	24	0.875	0.960	0.115
AVG MAD = 0.103				

CHI SQUARE (ORIG SCALE):

MIN CHI = 46.301 K = 24 VALID YR = 8
 MAX CHI = 340.712 K = 24 VALID YR = 9
 AVG CHI = 101.231

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.042 K = 24 VALID YR = 4
 MAX MSE = 0.211 K = 24 VALID YR = 9
 AVG MSE = 0.080

C. SAMPLE OUTPUT (VECTOR TEST CASES)

TEST CASE INPUT PARAMETERS:

INVENTORY THRESHOLD= 30.0 THRESHOLD NO. OF CELLS= 30
MOS= 151 YCS= 7 GRADE= 17
SERVICE COMPONENTS= 1 2 3
COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

EXPANSION INFORMATION:

ACTUAL NO. OF CELLS USED= 8
MOS GROUP # 8 YCS'S USED=
7
LARGE MOS GROUP #3 YCS'S USED=
7
MAJOR MOS GROUP #2 YCS'S USED=
7

EMP BAYES TRANS SCALE - VECTOR CASE:

VECTOR IS BY SERVICE COMPONENT
K= 8 P= 3 KP= 24

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	KP	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.375	0.219	0.186
2	24	0.458	0.375	0.179
3	24	0.458	0.417	0.130
4	24	0.458	0.422	0.127
5	24	0.542	0.708	0.146
6	24	0.292	0.310	0.142
7	24	0.250	0.193	0.126
8	24	0.375	0.434	0.092
9	24	0.458	0.705	0.161
10	24	0.792	0.912	0.202

CHI SQUARE (ORIG SCALE):

MIN CHI = 27.827 KP = 24 VALID YR = 8
MAX CHI = 165.694 KP = 24 VALID YR = 10
AVG CHI = 61.025

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.089 KP = 24 VALID YR = 8
MAX MSE = 0.483 KP = 24 VALID YR = 10
AVG MSE = 0.229

REFERENCES

Amin Elseramegy, H., *CART Program: Implementation of the CART Program and Its Application to Estimating Attrition Rates*, Master's Thesis, Naval Postgraduate School, Monterey, California, December 1985.

Carter, G.M. and Rolph, J.E., "Empirical Bayes Methods Applied to Estimating Fire Alarm Probabilities," *Journal of the American Statistical Association*, v.69, pp. 880-885, December 1974.

Casella, G., "An Introduction to Empirical Bayes Data Analysis," *The American Statistician*, v.39, pp. 83-87, May 1985.

Decision System Associates, Inc., *Functional Description for the Development of the Officer Planning and Utilization System (OPUS)*, Rockville, Maryland, 1986.

Dickinson, C.R., *Refinement and Extension of Shrinkage Techniques in Loss Rate Estimation of Marine Corps Officer Manpower Models*, Master's Thesis, Naval Postgraduate School, Monterey, California, March 1988.

Efron, B. and Morris, C., "Empirical Bayes on Vector Observations: An Extension of Stein's Method," *Biometrika*, v.59, pp. 335-347, 1972.

Efron, B. and Morris, C., "Stein's Estimation Rule and Its Competitors - An Empirical Bayes Approach," *Journal of the American Statistical Association*, v.68, pp. 117-130, March 1973.

Efron, B. and Morris, C., "Data Analysis Using Stein's Estimator and Its Generalizations," *Journal of the American Statistical Association*, v.70, pp. 311-319, June 1975.

Hogan, D.L. Jr., *The Use of Exponential Smoothing to Produce Yearly Updates of Loss Rates Estimates in Marine Corps Manpower Models*, Master's Thesis, Naval Postgraduate School, Monterey, California, June 1986.

Larsen, R.W., *The Aggregation of Population Groups to Improve the Predictability of Marine Corps Officer Attrition Estimation*, Master's Thesis, Naval Postgraduate School, Monterey, California, December 1987.

Marine Corps Order P1200.7G, *Military Occupational Specialties Manual (MOS Manual)*, Chapter 1, 1 April 1988.

Naval Postgraduate School Report NPS55-88-006, *The Use of Shrinkage Techniques in the Estimation of Attrition Rates for Large Scale Manpower Models*, R.R. Read, 27 July 1988.

Navy Personnel Research and Development Center, *System Design for the Marine Corps Officer Rate Projector (MCORP)*, San Diego, California, 1985.

Robinson, J.R., *Limited Translation Shrinkage Estimation of Loss Rates in Marine Corps Manpower Models*, Master's Thesis, Naval Postgraduate School, Monterey, California, March 1986.

Siegel, B., *Methods for Forecasting Officer Loss Rates*, Navy Personnel Research and Development Center, San Diego, California, 1983.

Tucker, D.D., *Loss Rate Estimation in Marine Corps Officer Manpower Models*, Master's Thesis, Naval Postgraduate School, Monterey, California, September 1985.

Yacin, N., *Application of Logistic Regression to the Estimation of Manpower Attrition Rates*, Master's Thesis, Naval Postgraduate School, Monterey, California, March 1987.

INITIAL DISTRIBUTION LIST

	No. Copies
1. Defense Technical Information Center Cameron Station Alexandria, VA 22304-6145	2
2. Library, Code 0142 Naval Postgraduate School Monterey, CA 93943-5002	2
3. Professor Robert R. Read, (Code 55Re) Naval Postgraduate School Monterey, CA 93943-5000	5
4. Professor Gerald G. Brown, (Code 55Bw) Naval Postgraduate School Monterey, CA 93943-5000	1
5. Major John M. Misiewicz MAGTF Warfighting Center (WF13) Marine Corps Combat Development Command Quantico, VA 22134-5001	5
6. Commanding Officer Attn: Carol Mullins Navy Personnel Research and Development Center San Diego, CA 92152	1
7. Mr. R. Morton Decision System Associates, Inc. 350 Fortune Terrace Rockville, MD 20854-2995	1
8. Commandant of the Marine Corps Code MI Attn: Major D. O'Dell Headquarters, U.S. Marine Corps Washington, D.C. 20380-0001	1
9. Commandant of the Marine Corps Code MPP-31 Attn: Major R.W. Larsen Headquarters, U.S. Marine Corps Washington, D.C. 20380-0001	1

- | | |
|---|---|
| 10. Director
Center for Naval Analysis
4401 Ford Avenue
Alexandria, VA 22302 | 1 |
| 11. Commandant of the Marine Corps
Code TE06
Headquarters, U.S. Marine Corps
Washington, D.C. 20380-0001 | 1 |
| 12. Captain Charles R. Dickinson
Staff USCINCPAC Box 15(J55)
Camp H.M. Smith, HI 96861 | 1 |
| 13. Captain Michael J. Streff
HQDA
Attn: DAPE-MBB-P (Room 2D669)
Washington, D.C. 20310 | 1 |

Thesis

M63653 Misiewicz

c.1 Extension of aggregation and shrinkage techniques used in the estimation of Marine Corps Officer attrition rates.

Thesis

M63653 Misiewicz

c.1 Extension of aggregation and shrinkage techniques used in the estimation of Marine Corps Officer attrition rates.



thesM63653
Extension of aggregation and shrinkage t



3 2768 000 85719 7
DUDLEY KNOX LIBRARY